NASA MEMO 2-20-59L

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MEMORANDUM

TABLES FOR THE RAPID ESTIMATION OF DOWNWASH AND SIDEWASH
BEHIND WINGS PERFORMING VARIOUS MOTIONS

AT SUPERSONIC SPEEDS

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NATIONAL AERONAUTICS AND SPACE ADMINISTRATION

WASHINGTON

May 1959

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SUMMARY

Equations for the downwash and sidewash due to supersonic yawed and unswept horseshoe vortices have been utilized in formulating tables and charts to permit a rapid estimation of the flow velocities behind wings performing various steady motions. Tabulations are presented of the downwash and sidewash in the wing vertical plane of symmetry due to a unit-strength yawed horseshoe vortex located at 20 equally spaced spanwise positions along lifting lines of various sweeps. (The bound portion of the yawed vortex is coincident with the lifting line.) Charts are presented for the purpose of estimating the spanwise variations of the flow-field velocities and give longitudinal variations of the downwash and sidewash at a number of vertical and spanwise locations due to a unit-strength unswept horseshoe vortex. Use of the tables and charts to calculate wing downwash or sidewash requires a knowledge of the wing spanwise distribution of circulation.

Sample computations for the rolling sidewash and angle-of-attack downwash behind a typical swept wing are presented to demonstrate the use of the tables and charts.

INTRODUCTION

The ability of a designer to predict the flow characteristics behind wings of aircraft performing various motions is important in estimating the forces and moments acting on the tail configuration and the associated aircraft stability. Naturally, then, since the advent of supersonic flight, methods for determining theoretically the flow velocity components, downwash and sidewash, behind wings traveling in this speed range have received appreciable attention. Lifting-surface methods utilizing the concepts of conical superposition, doublet distributions, and vortices have been developed and applied in references 1 to 5 and lifting-line and approximate lifting-line (horseshoe vortices) formulas have been derived and utilized in references 6 to 9.

Each of the two types of methods has certain disadvantages when applied to specific wings. In the case of lifting-surface methods the disadvantage is the complexity of the integrals involved and for liftingline methods it is the difficulty in obtaining accurate values close behind the trailing edge or near the vortex sheet. The lifting-line difficulties in most cases can be minimized or overcome by using more than one lifting line and by determining from previously derived expressions the exact value at the trailing edge or in the plane of the vortex sheet. The difficulty associated with lifting-surface methods, on the other hand, is much more restrictive and has been overcome for only a few simple plan-form shapes. Certainly, for ease of application, liftingline and horseshoe-vortex methods are to be preferred since they may be applied to wings of any plan form with equal ease and require only numerical calculations in cases where spanwise circulation distributions are available. Some indication of the ability of the lifting-line approach to approximate lifting-surface results can be had by noting the comparisons made in references 4, 7, 8, and 9.

Though the usefulness of the lifting-line methods is clear, it has not been fully exploited. One important reason for this situation is that the use of lifting-line and horseshoe-vortex expressions to calculate the flow velocities at a number of points behind a wing can involve a great deal of computing labor. At subsonic speeds the same situation existed and was eliminated by the preparation and use of tables and charts giving the downwash and sidewash at various points in the flow field contributed by a unit-strength horseshoe vortex (see ref. 10). The purpose of the present paper is to present, for the supersonic speed range, similar tables and charts which will allow a rapid calculation of the flow field behind wings of arbitrary plan form at an angle of attack or performing steady rolling, pitching, and sileslip motions. The tables give tabulations of the downwash and sidewash in the vertical plane of symmetry due to a unit-strength yawed horseshoe vortex located at 20 equally spaced positions along lifting lines of various sweeps. The charts give longitudinal variations at a number of vertical and spanwise locations of the downwash and sidewash due to a unit-strength unswept horseshoe vortex and are used primarily to predict the spanwise variations of the flowfield velocities. In application, the known spanwise distribution of wing circulation strength (see refs. 11 to 13) is used to weight the downwash and sidewash contributed by each unit horseshoe vortex and the total downwash or sidewash at a point is obtained by summing up the contributions of the weighted horseshoe vortices. The tables cover a large range of lifting-line sweep angles, Mach numbers, and longitudinal, spanwise, and vertical distances behind the wing.

Illustrative downwash and sidewash computations, comprising primarily a two-column multiplication plus a summation, are presented to demonstrate the use of the tables and the rapidity with which answers can be obtained.

SYMBOLS

| x,y,z | rectangular Cartesian coordinates of field point |
|--|--|
| x_1, y_1 | rectangular Cartesian coordinates of points along a lifting line |
| x _i ,y _i | rectangular Cartesian coordinates of corner of a particular vortex in a distribution of vortices |
| A | wing aspect ratio, b ² /S |
| ъ | wing span |
| $e_{\mathbf{r}}$ | wing root chord |
| c_1 | lifting-line chord (see fig. 8) |
| .h ₁ ,h ₂ | limits of y_1 integration |
| i | variable index used in summations |
| М | free-stream Mach number, $\frac{V_{\infty}}{V_{\infty}}$ |
| | Velocity of sound in free stream |
| m | velocity of sound in free stream slope of lifting line (absolute value) |
| m m _O | |
| | slope of lifting line (absolute value) |
| m_{O} | slope of lifting line (absolute value) slope of leading edge |
| m _O | slope of lifting line (absolute value) slope of leading edge slope of trailing edge value of i at left- and right-hand wing tips of a swept wing |
| m _O m ₁ n ₁ ,n ₂ | <pre>slope of lifting line (absolute value) slope of leading edge slope of trailing edge value of i at left- and right-hand wing tips of a swept wing looking from trailing edge to leading edge</pre> |
| m ₀ m ₁ n ₁ ,n ₂ p | <pre>slope of lifting line (absolute value) slope of leading edge slope of trailing edge value of i at left- and right-hand wing tips of a swept wing looking from trailing edge to leading edge angular velocity of roll, radians/sec</pre> |
| m ₀ m ₁ n ₁ ,n ₂ p | <pre>slope of lifting line (absolute value) slope of leading edge slope of trailing edge value of i at left- and right-hand wing tips of a swept wing looking from trailing edge to leading edge angular velocity of roll, radians/sec angular velocity of pitch, radians/sec</pre> |

$$X = x - x_1$$

$$X_i = x - x_i$$

$$x_{i,0} = \frac{mx_1}{b/2} = x_0 - x_{i,0} = x_0 \pm y_{i,0}$$

$$\bar{X}_{i} = \bar{x} \pm \frac{y_{i,0}}{\beta m}$$

$$x_0 = \frac{mx}{b/2} = \frac{x}{c_1}$$

$$x_{i,0} = \pm \frac{mx_i}{b/2} = \pm y_{i,0}$$
 (slope of lifting line determines plus or minus sign)

$$\bar{x} = \frac{x}{\beta b/2}$$
 (= $\frac{x_0}{\beta m}$ for swept lifting line)

$$Y = y - y_1$$

$$Y_i = y - y_i$$

$$Y_{i,0} = \frac{Y_i}{b/2} = y_0 - y_{i,0}$$

$$y_0 = \frac{y}{b/2}$$

$$y_{i,0} = \frac{y_i}{b/2}$$

$$z_0 = \frac{z}{b/2}$$

α angle of attack, radians

$$\beta = \sqrt{M^2 - 1}$$

Γ circulation at any spanwise station

 Γ_{O} circulation at $y_{i} = 0$

 λ taper ratio

σ local angle of attack

 ϕ perturbation velocity potential

 $F_{w,0}$ defined by equations (7) and (11)

$$\left[F_{w}(y_{i,0})\right]_{3}$$
, $\left[F_{w}(y_{i,0})\right]_{2}$ defined by equations (7) and (11)

$$\left[F_{v}(y_{i,0})\right]_{1}, \left[F_{v}(y_{i,0})\right]_{2}$$
 defined by equations (8) and (12)

$$\left\{ \begin{bmatrix} F_{\mathbf{w}}(\mathbf{y}_{\mathbf{i},0}) \end{bmatrix}_{\mathbf{1}} \right\}_{\mathbf{m}=\mathbf{\infty}}, \left\{ \begin{bmatrix} F_{\mathbf{w}}(\mathbf{y}_{\mathbf{i},0}) \end{bmatrix}_{\mathbf{2}} \right\}_{\mathbf{m}=\mathbf{\infty}} \quad \text{defined by equations (9)}$$

$$\left\{ \left[F_{v}(y_{i,0}) \right]_{1} \right\}_{m=\infty}, \left\{ \left[F_{v}(y_{i,0}) \right]_{2} \right\}_{m=\infty} \quad \text{defined by equations (10)}$$

 $F_{W}(Y_{1,0})$ defined by equations (5) and (15)

 $F_v(Y_{i,o})$ defined by equations (6) and (16)

$$F_{w}(|y_{i,o}|) = \frac{-|y_{i,o}|X_{i,o}^{3} + X_{i,o}(z_{o}^{2} - y_{i,o}^{2}) + \beta^{2}m^{2}|y_{i,o}|X_{i,o}(|y_{i,o}|^{2} + 2z_{o}^{2}) + \beta^{2}m^{2}|y_{i,o}|(z_{o}^{2} + |y_{i,o}|^{2})}{4\pi\sqrt{|X_{i,o}^{2} - \beta^{2}m^{2}(|y_{i,o}|^{2} + z_{o}^{2})\left[\left(|y_{i,o}|X_{i,o} + z_{o}^{2} + |y_{i,o}|^{2}\right)^{2} + z_{o}^{2}(X_{i,o}^{2} - \beta^{2}m^{2}|y_{i,o}|^{2} - \beta^{2}m^{2}z_{o}^{2})\right]}}$$

$$F_{\mathbf{v}}(|\mathbf{y}_{1,0}|) = \frac{z_{0}|\mathbf{y}_{1,0}|\left(2X_{1,0} - \beta^{2}m^{2}|\mathbf{y}_{1,0}|^{2} - \beta^{2}m^{2}z_{0}^{2}\right) + z_{0}X_{1,0}\left(X_{1,0}^{2} - \beta^{2}m^{2}z_{0}^{2}\right)}{4\pi\sqrt{X_{1,0}^{2} - \beta^{2}m^{2}\left(|\mathbf{y}_{1,0}|^{2} + z_{0}^{2}\right)\left[\left(|\mathbf{y}_{1,0}|X_{1,0} + z_{0}^{2} + |\mathbf{y}_{1,0}|^{2}\right)^{2} + z_{0}^{2}\left(X_{1,0}^{2} - \beta^{2}m^{2}|\mathbf{y}_{1,0}|^{2} - \beta^{2}m^{2}z_{0}^{2}\right)}\right]}$$

$$\left[F_{W}(|y_{i,o}|) \right]_{m=\infty} = \frac{-|y_{i,o}|\bar{x}^{3} + |y_{i,o}|\bar{x}(|y_{i,o}|^{2} + 2z_{o}^{2})}{4\pi \sqrt{\bar{x}^{2} - |y_{i,o}|^{2} - z_{o}^{2}[|y_{i,o}|^{2}\bar{x}^{2} + z_{o}^{2}(\bar{x}^{2} - |y_{i,o}|^{2} - z_{o}^{2})]}$$

$$\left[F_{V} \left(\left| y_{i,o} \right| \right) \right]_{m=\infty} = \frac{z_{o} \bar{x}}{4\pi \sqrt{\bar{x}^{2} - \left| y_{i,o} \right|^{2} - z_{o}^{2} \left(\left| y_{i,o} \right|^{2} + z_{o}^{2} \right)}$$

Subscripts:

te conditions at trailing edge

 y_i value of circulation strength at spanwise station y_i

Plus and minus signs used as exponents indicate positive or negative values, respectively, of a variable.

THEORY

Downwash and Sidewash Equations Jsed in Preparation

of Tables and Charts

Equations for downwash due to distributions of yawed and unswept horseshoe vortices may be found in references 8 and 9. An expression for the sidewash due to yawed horseshoe vortices distributed along a line to approximate a rolling span load distribution is given in reference 4. In this section, expressions for the sidewash due to distributions of yawed and unswept vortices approximating lifting lines with arbitrary span load distributions are presented in addition to the corresponding downwash formulas previously obtained.

The downwash and sidewash due to a swept lifting line with any prescribed lift distribution can be approximated through the use of the equations for the downwash and sidewash due to yawed horseshoe vortices (see fig. 1) of positive and negative slopes plus terms giving the effect of the break in the center of the lifting line. Rectangular horseshoe vortices can be used most easily to approximate the flow field of unswept lifting lines though they may also be used with certain modifications to approximate swept lifting lines. (See fig. 2.) Derivations of the necessary formulas for yawed and unswept horseshoe vortices are given in the appendix.

The lifting line or lines used to represent a wing are, in this paper, composed of two straight lines connecting some point on the wing root chord with the tip chord, for example, a pair of straight lines connecting the midpoint of the root chord with the midpoint of the tip chord. The slopes of the two straight lines are opposite in sign and have the magnitude $\frac{b/2}{c_1}(=m)$ where b/2 is the semispan of the wing and c_1 is the longitudinal distance from the intersection of the two straight lines on the wing root chord to the intersections of the straight lines with the wing tips.

The downwash and sidewash due to a swept lifting line approximated by a series of yawed vortices (see fig. 2(a)) are given, respectively, by

$$-\mathbf{v} = -\frac{\frac{1+0}{2}}{\frac{1+n_1}{2}} \frac{\Gamma_{\mathbf{y_{1+1}}} - \Gamma_{\mathbf{y_{1-1}}}}{\frac{b/2}} \frac{\left[\mathbf{Y_{1,o}}\mathbf{X_{1,o}^{2}} - \mathbf{X_{1,o}^{2}}\left(\mathbf{z^{2}} - \mathbf{Y_{1,o}^{2}}\right) - \beta^{2}m^{2}\mathbf{Y_{1,o}}\mathbf{X_{1,o}}\left(\mathbf{Y_{1,o}^{2}} + 2z_{0}^{2}\right) - \beta^{2}m^{2}\mathbf{Y_{1,o}^{2}}\left(z_{0}^{2} + \mathbf{Y_{1,o}^{2}}\right)\right]}{\frac{4\pi\sqrt{\mathbf{X_{1,o}^{2}} - \beta^{2}m^{2}\left(\mathbf{Y_{1,o}^{2}} + z_{0}^{2}\right)}\left[\left(\mathbf{Y_{1,o}} + \mathbf{X_{1,o}}\right)^{2} + z_{0}^{2}\left(1 - \beta^{2}m^{2}\right)\right]\left(\mathbf{Y_{1,o}^{2}} + z_{0}^{2}\right)}{\frac{2\pi\sqrt{\mathbf{X_{1,o}^{2}} - \beta^{2}m^{2}\left(\mathbf{Y_{1,o}^{2}} + \mathbf{X_{1,o}^{2}}\left(z_{0}^{2} - \mathbf{Y_{1,o}^{2}}\right) - \beta^{2}m^{2}\mathbf{Y_{1,o}^{2}}\mathbf{X_{1,o}^{2}}\left(\mathbf{Y_{1,o}^{2}} + 2z_{0}^{2}\right) + \beta^{2}m^{2}\mathbf{Y_{1,o}^{2}}\left(z_{0}^{2} + \mathbf{Y_{1,o}^{2}}\right)\right]}} + \frac{\frac{1-n_2}{b/2}}{\frac{1+n_2}{b/2}} \frac{\left[\mathbf{Y_{1,o}}\mathbf{X_{1,o}^{2}} + \mathbf{X_{1,o}^{2}}\left(z_{0}^{2} - \mathbf{Y_{1,o}^{2}}\right) - \beta^{2}m^{2}\mathbf{Y_{1,o}^{2}}\mathbf{X_{1,o}^{2}}\left(\mathbf{Y_{1,o}^{2}} + 2z_{0}^{2}\right) + \beta^{2}m^{2}\mathbf{Y_{1,o}^{2}}\left(z_{0}^{2} + \mathbf{Y_{1,o}^{2}}\right)\right]}{\frac{1+n_2}{b/2}} + \frac{1-n_2}{b/2} \frac{\left[\mathbf{Y_{1,o}}\mathbf{X_{1,o}^{2}} + \mathbf{X_{1,o}^{2}}\left(\mathbf{X_{1,o}^{2}} + \mathbf{X_{1,o}^{2}}\right)^{2} + \mathbf{X_{1,o}^{2}}\left(\mathbf{X_{1,o}^{2}} + \mathbf{X_{1,o}^{2}}\right)^{2}}{\frac{1+n_2}{b/2}} + \frac{1-n_2}{b/2} \frac{1-n_$$

and

$$v = -\frac{\sum_{i=n_{1}}^{i=0}}{\frac{r_{y_{i+1}} - r_{y_{i-1}}}{b/2}} \frac{\left[z_{o}Y_{1,o}\left(2X_{1,o}^{2} - \beta^{2}m^{2}Y_{1,o}^{2} - \beta^{2}m^{2}z_{o}^{2}\right) + z_{o}X_{1,o}\left(X_{1,o}^{2} - \beta^{2}m^{2}z_{o}^{2}\right)\right]}{4\pi\sqrt{x_{1,o}^{2} - \beta^{2}m^{2}\left(Y_{1,o}^{2} + z_{o}^{2}\right)\left[\left(Y_{1,o} + X_{1,o}\right)^{2} + z_{o}^{2}\left(1 - \beta^{2}m^{2}\right)\right]\left(Y_{1,o}^{2} + z_{o}^{2}\right)}} - \frac{\frac{1-n_{2}}{4\pi\sqrt{x_{1,o}^{2} - \beta^{2}m^{2}\left(2X_{1,o}^{2} - \beta^{2}m^{2}Y_{1,o}^{2} - \beta^{2}m^{2}z_{o}^{2}\right) - z_{o}X_{1,o}\left(X_{1,o}^{2} - \beta^{2}m^{2}z_{o}^{2}\right)}\left[\left(Y_{1,o}^{2} - \beta^{2}m^{2}z_{o}^{2}\right)\right]}}{4\pi\sqrt{x_{1,o}^{2} - \beta^{2}m^{2}\left(Y_{1,o}^{2} + z_{o}^{2}\right)\left[\left(Y_{1,o} - X_{1,o}\right)^{2} + z_{o}^{2}\left(1 - \beta^{2}m^{2}\right)\right]\left(Y_{1,o}^{2} + z_{o}^{2}\right)}} + \frac{r_{o}\left(y_{o} - x_{o}\right) - r_{o}\left(y_{o} - x_{o}}\right) - r_{o}\left(y_{o} - x_{o}\right) - r_{o$$

where $X_{i,0}$ in the first summation terms of v and w is equal to $x_0 + y_{i,0}$ and in the second terms to $x_0 - y_{i,0}$. Values of i from 0 to n_1 are associated with negative values of y_i and values from 0 to n_2 , with positive values of y_i . A value of i equal to n_1 corresponds to the vortex at the left wing tip and a value of i equal to n_2 , to the right wing tip. Note that with the vortices numbered in this manner the incremental circulation strength $\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}$ is approximately proportional to $d\Gamma/dy$ on the right-hand panel and to $-d\Gamma/dy$ on the left.

When the lifting line is inclined supersonically to the free-stream direction each of the n vortices of equations (1) and (2) may be considered as semi-infinite yawed horseshoe vortices of the type shown in figure 3. When inclined subsonically the bound portion of semi-infinite horseshoe vortices of the type shown in figures 3(a) and 3(b) has an additional contribution not given by these equations. (See ref. 7.) However, this additional contribution is ot required in the use of equations (1) and (2) for a practical case since the semi-infinite vortices distributed on swept or yawed lifting lires combine to form finite swept horseshoe vortices of the type shown in figure 4 or finite yawed horseshoe vortices of the type depicted in figure 1(b). The equations of finite swept or yawed horseshoe vortices with bound portions inclined subsonically or supersonically are the same. The last two terms in equations (1) and (2) give the effect of the break in the swept horseshoe vortices formed by these last two terms and the semi-infinite yawed horseshoe vortices of the first two terms. (See eqs. (A9) and (A10) of appendix A.)

The downwash and sidewash behind a ving approximated by an unswept lifting line and semi-infinite unswept horseshoe vortices are, respectively,

$$-w = -\frac{\sum_{i=n_{1}}^{i=0}}{\frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2}} \frac{Y_{i,o}\bar{x}^{3} - Y_{i,o}\bar{x}(Y_{i,o}^{2} + 2z_{o}^{2})}{4\pi\sqrt{\bar{x}^{2} - Y_{i,o}^{2} - z_{o}^{2}(\bar{x}^{2} - z_{o}^{2})(Y_{i,o}^{2} + z_{o}^{2})}} + \frac{\sum_{i=0}^{i=n_{2}}}{\frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2}} \frac{Y_{i,o}\bar{x}^{3} - Y_{i,o}\bar{x}(Y_{i,o}^{2} + 2z_{o}^{2})}{4\pi\sqrt{\bar{x}^{2} - Y_{i,o}^{2} - z_{o}^{2}(\bar{x}^{2} - z_{o}^{2})(Y_{i,o}^{2} + z_{o}^{2})}}$$

$$(3)$$

and

$$v = - \sum_{i=n_1}^{i=0} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} \frac{z_0 \bar{x}}{4\pi \sqrt{\bar{x}^2 - Y_{i,0}^2 - z_0^2 (Y_{i,0}^2 + z_0^2)}} +$$

$$\sum_{i=0}^{i=n_2} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} \frac{z_0 \bar{x}}{4\pi \sqrt{\bar{x}^2 - Y_{i,0}^2 - z_0^2 (Y_{i,0}^2 + z_0^2)}}$$
(4)

where $\bar{x} = \frac{x}{\beta \frac{b}{2}}$. Equations (3) and (4) may be written by inspection from equations (A6) and (A7) of appendix A.

As indicated previously the equations for rectangular horseshoe vortices may be used to approximate swept as well as unswept lifting lines. One approach to doing this is to replace \bar{x} in equations (3) and (4) with \overline{X}_i thereby approximating a swept lifting line with semiinfinite unswept horseshoe vortices in the manner shown in figures 2(b) and 2(c). A second method is to use finite unswept horseshoe vortices distributed along the lifting line in much the same way as is done subsonically (see fig. 2(d)). It appears from the limited number of calculations performed to establish which of the two approaches better approximates equations (1) and (2) (see fig. 2(a)) that the first approach is superior. Detailed examination of the calculations to determine the reasons for this superiority indicates that when a practical number of vortices are used to approximate a lifting line, it is more important to approximate accurately the trailing vortex system than the bound vortex system of equations (1) and (2). It can be seen from a comparison of figures 2(a) and 2(b) that the trailing vortex system of the first approach is exactly the same as that obtained using a distribution of yawed vortices. Although the combined bound vortices of the distribution of finite rectangular horseshoe vortices (fig. 2(d)) accurately approximate the bound vortex system of the yawed vortex distribution (coincident with the lifting line), the staggered trailing vortices do not represent a good approximation to the trailing vortex system of the yawed horseshoe vortex distribution. It should be mentioned that although neither method does particularly well in predicting magnitudes, spanwise variations of the flow-field velocities as computed by equations (1) and (2) are better predicted by the semi-infinite unswept horseshoe vortices. In view of the preceding discussion only the equations for the downwash and sidewash due to a distribution of semi-infinite unswept horseshoe

vortices will be given. Equations (3) and (4) with \bar{x} replaced by \bar{X}_1 become, respectively,

$$-w = -\sum_{i=n_{1}}^{O} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} \frac{\left[Y_{i,o}\overline{X}_{i}^{3} - Y_{i,o}\overline{X}_{i}\left(Y_{i,o}^{2} + 2z_{o}^{2}\right)\right]}{\mu_{\pi}\sqrt{\overline{X}_{i}^{2} - Y_{i,o}^{2} - z_{o}^{2}\left(\overline{X}_{i}^{2} - z_{o}^{2}\right)\left(Y_{i,o}^{2} + z_{o}^{2}\right)}} + \frac{i=n_{2}}{b/2} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} \frac{\left[Y_{i,o}\overline{X}_{i}^{3} - Y_{i,o}\overline{X}_{i}\left(Y_{i,o}^{2} + 2z_{o}^{2}\right)\right]}{\mu_{\pi}\sqrt{\overline{X}_{i}^{2} - Y_{i,o}^{2} - z_{o}^{2}\left(\overline{X}_{i}^{2} - z_{o}^{2}\right)\left(Y_{i,o}^{2} + z_{o}^{2}\right)}}$$

$$(5)$$

and

$$v = -\sum_{i=n_{\perp}}^{0} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} \frac{z_{o} \overline{x}_{i}}{4\pi \sqrt{\overline{x}_{i}^{2} - \beta^{2} (Y_{i,o}^{2} + z_{o}^{2}) (Y_{i,o}^{2} + z_{o}^{2})} +$$

$$\sum_{i=0}^{n_2} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} \frac{z_0 \overline{X}_i}{4\pi \sqrt{\overline{X}_i^2 - \beta^2 (Y_{i,0}^2 + z_0^2)} (Y_{i,0}^2 + z_0^2)}$$
 (6)

where \bar{X}_i on the left panel is equal to $\bar{x} + \frac{y_{i,o}}{\beta m}$ and on the right,

to $\bar{x} - \frac{y_{i,0}}{\beta m}$. Note that the summation terms in the equations for w are

singular for points on a line vortex, that is, when $Y_{i,0}=z_0=0$. In order to avoid this singularity and to obtain more realistic values for downwash, experience indicates that points in the z=0 plane should be chosen midway between the trailing vortices. Another singularity which exists in the equation for w as well as in that for v occurs when the square root in the denominator is zero. Points that give rise to this type of singularity lie on the aftercone from a corner of a horseshoe vortex and should not be used.

It is possible by the use of equations (1) and (2) to prepare tables or charts which would considerably expedite the calculation of downwash

and sidewash, at a large number of points (x, y, and z) in the flow field, due to a swept lifting line approximated by semi-infinite yawed horseshoe vortices. To do this, however, would result, for the range of y values considered necessary, in tables half again as large as the ones contemplated and would not give the simplicity desired for calculations in the plane of symmetry. Equations (5) and (6) may also be used for preparing tables of downwash and sidewash influence functions though the accuracy of the results obtained through their use would not be so good as that obtained using tables based on equations (1) and (2). There is, however, one advantage that equations (5) and (6) have over equations (1) and (2) and that is that they have one less parameter in the summation terms. In preparing downwash and sidewash tables for a given number of field points this advantage would mean a considerable decrease in the size of the tables required. Charts might also be used in lieu of tables in the case of equations (5) and (6) to obviate the need for interpolation between X_i values and thus effect an additional time saving.

The computational scheme to be used herein is as follows. puting downwash and sidewash in the plane of symmetry tables have been prepared that are based on equations (1) to (4) and charts based on equations (5) and (6) are presented for estimating the spanwise variation of these quantities. It is intended that the level of the spanwise variations be adjusted, if necessary, to the values at the plane of symmetry obtained using the tables. This procedure is an attempt to make use of the advantages of both sets of equations and thereby to obtain reasonable accuracy and greater speed from a smaller set of tables than would be required if equations (1) and (2) were used exclusively. The tables for the plane of symmetry are in a form such that no interpolation is required in obtaining downwash and sidewash at the field points and \(\beta\mathbb{m}\) values for which tabulations have been presented. In making preliminary estimates of vertical- or horizontal-tail loads, where it is often expedient to restrict the calculations to the plane of symmetry, this is especially convenient.

The necessary equations of the flow velocities for the plane of symmetry are, from equations (1) to (4), respectively,

$$-w = -\sum_{i=n_{1}}^{0} \frac{\left(\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}\right)}{b/2} \frac{\left[-y_{i,0}X_{1,0}^{2} - X_{1,0}^{2}\left(z_{0}^{2} - y_{1,0}^{2}\right) + \beta^{2}m^{2}y_{i,0}X_{1,0}\left(y_{1,0}^{2} + 2z_{0}^{2}\right) - \beta^{2}m^{2}y_{1,0}^{2}\left(z_{0}^{2} + y_{1,0}^{2}\right)\right]}{b/2} + \sum_{i=0}^{n_{2}} \frac{\left(\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}\right)\left[-y_{i,0}X_{1,0}^{2} + X_{1,0}^{2}\left(z_{0}^{2} - y_{1,0}^{2}\right) + \beta^{2}m^{2}y_{i,0}X_{1,0}\left(y_{1,0}^{2} + 2z_{0}^{2}\right) + \beta^{2}m^{2}y_{1,0}\left(z_{0}^{2} + y_{1,0}^{2}\right)\right]}{b/2} \left[\frac{-y_{i,0}X_{1,0}^{2} + X_{1,0}^{2}\left(z_{0}^{2} - y_{1,0}^{2}\right) + \beta^{2}m^{2}y_{1,0}X_{1,0}\left(y_{1,0}^{2} + 2z_{0}^{2}\right) + \beta^{2}m^{2}y_{1,0}\left(z_{0}^{2} + y_{1,0}^{2}\right)\right]}{b/2} + \frac{\Gamma_{0}}{b/2} \frac{X_{0}^{2}}{\pi\sqrt{X_{0}^{2} + \beta^{2}m^{2}z_{0}^{2}\left[X_{0}^{2} + z_{0}^{2}\left(1 - \beta^{2}m^{2}\right)\right]}}{\sqrt{(1 + \beta^{2}m^{2}z_{0}^{2}\left[X_{0}^{2} + z_{0}^{2}\left(1 - \beta^{2}m^{2}\right)\right]}}$$

$$(7)$$

$$v = \sum_{i=n_1}^{0} \frac{\left(\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}} \right)}{b/2} \frac{\left[z_{o}y_{i,o} \left(2X_{1,o}^{2} - \beta^{2}m^{2}y_{i,o}^{2} - \beta^{2}m^{2}z_{o}^{2} \right) - z_{o}X_{i,o} \left(X_{1,o}^{2} - \beta^{2}m^{2}z_{o}^{2} \right) \right]}{4\pi \sqrt{X_{1,o}^{2} - \beta^{2}m^{2}y_{i,o}^{2} - \beta^{2}m^{2}z_{o}^{2}} \left[\left(-y_{i,o} + X_{i,o} \right)^{2} + z^{2} \left(1 - \beta^{2}m^{2} \right) \right] \left(y_{i,o}^{2} + z_{o}^{2} \right)} - \frac{1}{2} \left[\left(-y_{i,o} + X_{i,o} \right)^{2} + z_{o}^{2} \left(1 - \beta^{2}m^{2} \right) \right] \left(-y_{i,o} + z_{o}^{2} \right)} - \frac{1}{2} \left[\left(-y_{i,o} + X_{i,o} \right)^{2} + z_{o}^{2} \left(1 - \beta^{2}m^{2} \right) \right] \left(-y_{i,o} + z_{o}^{2} \right)} - \frac{1}{2} \left[\left(-y_{i,o} + X_{i,o} \right)^{2} + z_{o}^{2} \left(1 - \beta^{2}m^{2} \right) \right] \left(-y_{i,o} + z_{o}^{2} \right)} - \frac{1}{2} \left[\left(-y_{i,o} + x_{i,o} \right)^{2} + z_{o}^{2} \left(1 - y_{i,o} + z_{o}^{2} \right) \right]} - \frac{1}{2} \left[\left(-y_{i,o} + x_{i,o} \right)^{2} + z_{o}^{2} \left(1 - y_{i,o} + z_{o}^{2} \right) \right]} - \frac{1}{2} \left[\left(-y_{i,o} + x_{i,o} \right)^{2} + z_{o}^{2} \left(1 - y_{i,o} + z_{o}^{2} \right) \right]} - \frac{1}{2} \left[\left(-y_{i,o} + z_{o} + z_{o} \right) + z_{o}^{2} \left(1 - y_{i,o} + z_{o} \right) \right]} - \frac{1}{2} \left[\left(-y_{i,o} + z_{o} + z_{o} \right) + z_{o}^{2} \left(1 - z_{o} + z_{o} \right) \right]} - \frac{1}{2} \left[\left(-y_{i,o} + z_{o} + z_{o} \right) + z_{o}^{2} \left(1 - z_{o} + z_{o} \right) \right]} - \frac{1}{2} \left[\left(-y_{i,o} + z_{o} + z_{o} \right) + z_{o}^{2} \left(1 - z_{o} + z_{o} \right) \right]} - \frac{1}{2} \left[\left(-y_{i,o} + z_{o} + z_{o} \right) + z_{o}^{2} \left(1 - z_{o} + z_{o} \right) \right]} - \frac{1}{2} \left[\left(-y_{i,o} + z_{o} + z_{o} \right) + z_{o}^{2} \left(1 - z_{o} + z_{o} \right) \right]} - \frac{1}{2} \left[\left(-y_{i,o} + z_{o} + z_{o} \right) + z_{o}^{2} \left(1 - z_{o} + z_{o} \right) \right]} - \frac{1}{2} \left[\left(-y_{i,o} + z_{o} + z_{o} \right) + z_{o}^{2} \left(1 - z_{o} + z_{o} \right) \right]} - \frac{1}{2} \left[\left(-y_{i,o} + z_{o} + z_{o} \right) + z_{o}^{2} \left(1 - z_{o} + z_{o} \right) \right]} - \frac{1}{2} \left[\left(-z_{o} + z_{o} + z_{o} + z_{o} \right) + z_{o}^{2} \left(1 - z_{o} + z_{o} \right) \right]} - \frac{1}{2} \left[\left(-z_{o} + z_{o} + z_{o} + z_{o} \right) + z_{o}^{2} \left(-z_{o} + z_{o} + z_{o} \right) \right]} - \frac{1}{2} \left[\left(-z_{o} + z_{o} + z_{o} + z_{o} \right) + z_{o}^{2} \left(-z_{o} + z_{o} + z_{o} \right) \right]} - \frac{1}{2} \left[\left(-z_{o} + z_{o} + z_{o} + z_{o} \right) \right] + \frac{1}{2} \left[$$

$$\sum_{i=0}^{n_2} \frac{\left(\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}\right)}{b/2} \frac{\left[-z_0 y_{i,0} \left(2 x_{i,0}^2 - \beta^2 m^2 y_{i,0}^2 \cdot \beta^2 m^2 z_0^2\right) - z_0 x_{i,0} \left(x_{i,0}^2 - \beta^2 m^2 z_0^2\right)\right]}{4\pi \sqrt{x_{i,0}^2 - \beta^2 m^2 y_{i,0}^2 - \beta^2 m^2 z_0^2} \left[\left(y_{i,0} + x_{i,0}\right)^2 + z^2 \left(1 - \beta^2 m^2\right)\right] \left(y_{i,0}^2 + z_0^2\right)}$$
(8)

$$-w = -\sum_{i=n_{1}}^{O} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} \frac{\left[-y_{i,o}\bar{x}^{3} - y_{i,o}\bar{x}\left(y_{i,o}^{2} + 2z_{o}^{2}\right) \right]}{4\pi\sqrt{\bar{x}^{2} - y_{i,o}^{2} - z_{o}^{2} \left[\left(\bar{x}^{2} - z_{o}^{2}\right)\left(y_{i,o}^{2} + z_{o}^{2}\right) \right]}} + \sum_{i=0}^{n_{2}} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} \frac{\left[-y_{i,o}\bar{x}^{3} + y_{i,o}\bar{x}\left(y_{i,o}^{2} + 2z_{o}^{2}\right) \right]}{4\pi\sqrt{\bar{x}^{2} - y_{i,o}^{2} - z_{o}^{2} \left[\left(\bar{x}^{2} - z_{o}^{2}\right)\left(y_{i,o}^{2} + z_{o}^{2}\right) \right]}}$$

$$(9)$$

and

$$v = -\sum_{i=n_{1}}^{O} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} \frac{z_{o}\bar{x}}{\mu_{\pi}\sqrt{\bar{x}^{2} - y_{i,o}^{2} - z_{o}^{2}(y_{i,o}^{2} + z_{o}^{2})}} + \sum_{i=0}^{n_{2}} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} \frac{z_{o}\bar{x}}{\mu_{\pi}\sqrt{\bar{x}^{2} - y_{i,o}^{2} - z_{o}^{2}(y_{i,o}^{2} + z_{o}^{2})}}$$
(10)

For purposes of identifying the functions tabulated or plotted and of facilitating some of the simplifications possible, it is convenient to write equations (7), (8), (9), (10), (5), and (6), respectively, in the following functional forms:

$$-w = \sum_{i=n_1}^{o} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} \left[F_{w}(y_{i,o}) \right]_{1} +$$

$$\sum_{i=0}^{n_2} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} \left[F_{\mathbf{w}}(y_{i,0}) \right]_2 + \frac{\Gamma_0}{b/2} F_{\mathbf{w},0}$$
 (11)

$$v = \sum_{i=n_1}^{O} \frac{\Gamma y_{i+1} - \Gamma y_{i-1}}{b/2} \left[F_v(y_{i,0}) \right]_1 +$$

$$\sum_{i=0}^{n_2} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} \left[F_v(y_{i,0}) \right]_2$$
 (12)

$$-w = \sum_{i=n_1}^{O} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} \left\{ \left[F_{w}(y_{i,0}) \right]_1 \right\}_{m=\infty} +$$

$$\sum_{i=0}^{n_2} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} \left\{ \left| F_w(y_{i,0}) \right|_2 \right\}_{m=\infty}$$
 (13)

$$v = \sum_{i=n_{1}}^{0} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} \left\{ \left[F_{v}(y_{i,0}) \right]_{1} \right\}_{m=\infty} +$$

$$\sum_{i=0}^{\underline{n_2}} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} \left\{ \left[F_{v}(y_{i,0}) \right]_{2} \right\}_{m=\infty}$$
 (14)

.

$$-w = -\sum_{i=n_1}^{0} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} F_w(Y_{i,o}) +$$

$$\sum_{i=0}^{n_2} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} F_{w}(Y_{i,o})$$
 (15)

$$v = -\sum_{i=n_1}^{O} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} F_v(Y_{i,o}) +$$

$$\sum_{i=0}^{n_2} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} F_v(Y_{i,o})$$
 (16)

It is evident from equations (5), (6), (15), and (16) that $F_{W}(Y_{i,0}) = -F_{W}(Y_{i,0}) \quad \text{and that} \quad F_{V}(Y_{i,0}) = F_{V}(Y_{i,0}); \text{ hence, it is only necessary to plot the functions} \quad F_{W}(Y_{i,0}) \quad \text{and} \quad F_{V}(Y_{i,0}) \quad \text{for positive values of} \quad Y_{i,0}. \quad \text{The equations for the plane of symmetry may be put in forms comparable to equations (15) and (16) through further simplifications. By noting that <math>y_{i,0}$ values in $\left[F_{W}(y_{i,0}) \right]_{1}, \quad \left[F_{V}(y_{i,0}) \right]_{1}, \quad$

$$\left[F_{\mathbf{W}}(\mathbf{y}_{i,0})\right]_{1} = \left[F_{\mathbf{W}}(\mathbf{y}_{i,0})\right]_{2} \equiv F_{\mathbf{W}}(|\mathbf{y}_{i,0}|) \tag{17}$$

$$\left\{ \left[F_{\mathbf{w}}(\mathbf{y}_{\mathbf{i},0}) \right]_{1} \right\}_{m=\infty} = \left\{ \left[F_{\mathbf{w}}(\mathbf{y}_{\mathbf{i},0}) \right]_{2} \right\}_{m=\infty} \equiv \left[F_{\mathbf{w}}(|\mathbf{y}_{\mathbf{i},0}|) \right]_{m=\infty}$$
 (18)

$$-\left[F_{\mathbf{v}}(\mathbf{y}_{\mathbf{i},0})\right]_{1} = \left[F_{\mathbf{v}}(\mathbf{y}_{\mathbf{i},0})\right]_{2} = F_{\mathbf{v}}(\left|\mathbf{y}_{\mathbf{i},0}\right|)$$
 (19)

$$-\left\{ \left[F_{\mathbf{v}}(y_{i,0}) \right]_{1} \right\}_{m=\infty} = \left\{ \left[F_{\mathbf{v}}(y_{i,0}) \right]_{2} \right\}_{m=\infty} \equiv \left[F_{\mathbf{v}}(|y_{i,0}|) \right]_{m=\infty}$$
(20)

The identities given in equations (17) to (20), together with equations (11) to (14), yield the final or computational form of the equations for the downwash and sidewash in the vertical plane of symmetry (y = 0). These equations are

$$-w = \sum_{i=n_1}^{O} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} F_{w}(|y_{i,o}|) +$$

$$\sum_{i=0}^{n_2} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} F_{w}(|y_{i,0}|) + \frac{\Gamma_{0}}{b/2} F_{w,0}$$
 (21)

$$v = -\sum_{i=n_1}^{O} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} F_v(|y_{i,o}|) +$$

$$\sum_{i=0}^{n_2} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} F_{v}(|y_{i,o}|)$$
 (22)

$$-w = \sum_{i=n_1}^{Q} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} \left[F_w(|y_{i,0}|) \right]_{m=\infty} +$$

$$\sum_{i=0}^{n_2} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} \left[F_{\mathbf{w}} \left(| y_{i,0} | \right) \right]_{m=\infty}$$
 (23)

$$\mathbf{v} - \sum_{\mathbf{i}=n_{1}}^{0} \frac{\Gamma_{\mathbf{y_{i+1}}} - \Gamma_{\mathbf{y_{i-1}}}}{b/2} \left[\Gamma_{\mathbf{v}} \left(|\mathbf{y_{i,0}}| \right) \right]_{m=\infty} + \sum_{\mathbf{i}=0}^{n_{2}} \frac{\Gamma_{\mathbf{y_{i+1}}} - \Gamma_{\mathbf{y_{i-1}}}}{b/2} \left[F_{\mathbf{v}} \left(|\mathbf{y_{i,0}}| \right) \right]_{m=\infty} + (24)$$

Obviously only the functions $F_{w}(|y_{i,o}|)$, $F_{v}(|y_{i,o}|)$, $\left[F_{w}(|y_{i,o}|)\right]_{m=\infty}$,

 $\left[F_{\mathbf{v}}(|\mathbf{y_{i,o}}|)\right]_{m=\infty}$, and $F_{\mathbf{w,0}}$ need to be tabulated to determine the downwash and sidewash.

Wings that are at an angle of attack or performing a pitching motion have symmetrical spanwise distributions of circulation and rolling wings have asymmetrical distributions of circulation. Formulas for the plane of symmetry when applied to these motions may be further reduced. For the angle of attack and pitching motions

$$(\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}})_{\text{Left panel}} = (\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}})_{\text{Right panel}}$$

so that

$$-w = 2 \sum_{i=0}^{n_2} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} F_w(|y_{i,0}|) + \frac{\Gamma_0}{b/2} F_{w,0}$$
 (25)

and

$$(-w)_{m=\infty} = 2 \sum_{i=0}^{n_2} \frac{\Gamma y_{i+1} - \Gamma y_{i-1}}{b/2} \left[F_w(|y_{i,0}|) \right]_{m=\infty}$$
 (26)

The relationship of the incremental circulation strengths on the lefthand panel and on the right-hand panel of a rolling wing is

$$-(\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}})_{\text{Left panel}} = (\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}})_{\text{Right panel}}$$

Hence,

$$v = 2 \sum_{i=0}^{n_2} \frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{b/2} F_v(|y_{i,0}|)$$
 (27)

and

$$(\mathbf{v})_{\mathbf{m}=\infty} = 2 \sum_{i=0}^{n_2} \frac{\Gamma_{\mathbf{y}_{i+1}} - \Gamma_{\mathbf{y}_{i-1}}}{b/2} \left[F_{\mathbf{v}}(|\mathbf{y}_{i,0}|) \right]_{\mathbf{m}=\infty}$$
 (28)

To obtain the downwash and sidewash in the plane of symmetry behind a sideslipping wing requires the use of equations (21) and (22) or equations (23) and (24).

Sidewash and Downwash at Trailing Edge and Vortex Sheet

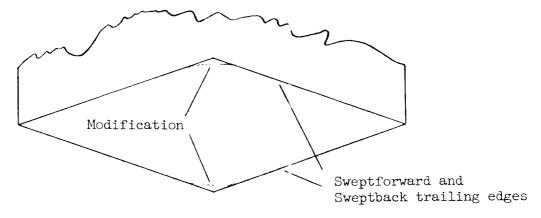
Lifting-line methods do not yield accurate approximations of lifting-surface downwash values in the vicinity of the wing trailing edge nor of lifting-surface sidewash values near the vortex sheet or wing trailing edge. These inadequacies may be minimized to some extent by the use of simple exact expressions, previously derived, for the downwash at the trailing edge and the sidewash at the vortex sheet. For a wing with trailing-edge slope m₁ references 1 and 8 give the downwash at the trailing edge as

$$-w_{\text{te}} = \sigma_{\text{te}} V_{\infty} - \frac{u_{\text{te}} \sqrt{\beta^2 m_1^2 - 1}}{m_1}$$
 (29)

where σ_{te} is the local angle of attack at the wing trailing edge. When the trailing edge is unswept, equation (29) becomes

$$-w_{te} = \sigma_{te} V_{\infty} - \beta u_{te}$$
 (30)

This equation may also be used to determine w at the trailing edge of the root chord of wings having swept trailing edges if the trailing-edge shape is modified as shown in the following sketch:



By considering the properties of vertex sheets, the sidewash at the vortex sheet has been determined in reference 14 to be

$$(\mathbf{v})_{z=0} = \frac{\mathrm{d}\phi_{te}(\mathbf{y}_{1})}{\mathrm{d}\mathbf{y}_{1}} = \frac{1}{2} \frac{\mathrm{d}\Gamma(\mathbf{y}_{1})}{\mathrm{d}\mathbf{y}_{1}}$$
(31)

Distortion, Rotation, and Displacement of Vortex Sheet

The effects of vortex-sheet distortion, rotation, and displacement have been discussed in most of the flow-field papers published to date so that no further discussion of these effects will be given other than pointing out several of these papers.

The method of accounting for the vertical displacement of the vortex sheet with longitudinal distance behind the trailing edge may be found in a number of papers. (See, e.g., ref. 9) Information regarding the distortion or rolling up of the vortex sheet may be obtained from references 9 and 15 to 18. The rotation of the vortex sheet which occurs in the rolling motion may be taken into account or neglected in accordance with the equations and discussion of references 4 or 19.

Comparisons of Lifting-Line and Lifting-Surface

Downwash and Sidewash

Comparisons of lifting-line and lifting-surface downwash at angle of attack have been made for triangular wings in references 7 and 8 and for rectangular wings in reference 9. Downwash variations computed by the two methods for a pitching rectangular wing are compared in reference 8. Lifting-line and lifting-surface sidewash have been determined and compared for a rolling triangular wing in reference 4. In addition, it is possible, by use of the lifting-surface results of reference 5 and the downwash tables presented herein, to make one other comparison, that of triangular-wing downwash due to pitching. This comparison has been made for βm_0 values of 0.5 and 1.0 and the results are given in figure 5. It can be seen in this figure that the agreement is very good.

Downwash and Sidewash Due to Flaps and Ailerons

The computation of downwash and sidewash due to flaps and ailerons is made with the same equations and tables as were used for calculating wing downwash and sidewash. It may well be that some shortening of the computing procedure may be effected in cases where a near-constant or constant value of the circulation exists across the span of the aileron or flap. Instead of using, say, 10 or 15 vortices across the span only one or two may be required.

PRESENTATION AND USE OF TABLES

A tabulation of the values of $y_{i,0}$, z_0 , x_0 , \bar{x} , and βm for which the plane-of-symmetry functions $F_V(|y_{i,0}|)$, $F_W(|y_{i,0}|)$, $[F_V(|y_{i,0}|)]_{m=\infty}$, and $[F_V(|y_{i,0}|)]_{m=\infty}$, and $[F_V(|y_{i,0}|)]_{m=\infty}$ are tabulated in table I. Values of $[F_V(|y_{i,0}|)]_{m=\infty}$ are tabulated in table II; $[F_V(|y_{i,0}|)]_{m=\infty}$ are tabulated in table III; and $[F_V(|y_{i,0}|)]_{m=\infty}$ are tabulated in table IV. Note in table I that no values of the $[F_V(|y_{i,0}|)]_{m=\infty}$ are tabulated out previously, which occurs for this condition. Plots of the variations of the $[F_V(|y_{i,0}|)]_{m=\infty}$ and $[F_V(|y_{i,0}|)]_{m=\infty}$ functions with longitudinal distance are given in figures 6 and 7,

respectively, for values of $Y_{1,0}$ from (1.05 to 1.45 and values of z_0 from 0 to 0.8 in the case of the downwash function and 0.2 to 0.8 for sidewash functions.

The usefulness of the tables can best be demonstrated by illustrative calculations for a particular wing. The wing chosen for this purpose is shown in figure 8 and has an aspect ratio of 3.57, a taper ratio of 0.565, and a leading-edge sweep of 38.80. The lifting line used to represent the wing connects the midpoints of the root and tip chords and has a sweep of 330. Calculations have been made for three Mach numbers, 1.35, 1.64, and 2.19. Values of βA , βm_O , and βm corresponding to each Mach number are listed in figure 8. It should be mentioned here that in order to avoid interpolation between &m values the Mach numbers were chosen to yield &m values identical to those given in tables II, III, and IV. The flow-field velocities computed are the angle-of-attack downwash and rolling and angle-of-attack sidewash. Angle-of-attack downwash has been determined in the plane of symmetry for a zo value of zero and a range of x_0 values extending from 1.0 to 5.0; rolling sidewash in the plane of symmetry has been calculated at an x_0 value of 2 and for z_0 values from 0 to 0.8. The spanwise variation of angle-of-attack downwash has been calculated using the charts of figure 6 at a x_0 value of 2.2 and a zo value of zero. The spanwise variation of rolling and angle-ofattack sidewash has been determined using the charts of figure 7 for an x_{O} value of 2.0 and a z_{O} value of 0.2. In order to give some indication of the ability of the charts based on equations (5) and (6) to approximate results based on equations (1) and (2), spanwise variations of the flow-field velocities using equations (1) and (2) have also been calculated for comparison.

The wing spanwise distribution of circulation for the angle-of-attack and rolling motions and for the Mach numbers previously listed were obtained by interpolation from the charts of reference 12 and are given in figures 9 and 10. These so-called circulation distributions are actually spanwise variations of a nondimensional circulation parameter. It is convenient in determining the angle-of-attack downwash and rolling sidewash to alter equations (13), (16), (25), and (27) so that the circulation strengths appear in the same nondimensional forms. Consider the downwash equations first. If both sides of equations (15) and (25) are divided by $V_{\infty}a$, the incremental circulation on the right-hand side can be grouped with $V_{\infty}ab/2$ to form the same nondimensional

parameter $\frac{\Gamma}{V_{\infty}ab/2}$ as is plotted in figure 9 and given in references 11

and 12. The left-hand side becomes equal to $\frac{-w}{V_{\infty}\alpha} = \frac{d\varepsilon}{d\alpha}$. For the rolling sidewash, both sides of equations (16) and (27) are nondimensionalized

by pb/2. When this is done, the circulation on the right-hand side of the equations may be grouped with $p(b/2)^2$ to form the same nondimensional

parameter $\frac{\Gamma}{p(b/2)^2}$ as is plotted in figure 10 and given in references 11

and 12. The left-hand side becomes equal to $\frac{v}{pb/2} = \frac{v/V_{\infty}}{pb/2V_{\infty}}$ and can be thought of as the induced lateral angularity per unit wing-tip helix angle $pb/2V_{\infty}$.

To illustrate the calculation procedure for each motion it is only necessary to show calculations for one Mach number and two points in the flow field, one in and one off the plane of symmetry. The points for which the downwash calculations are presented are both located at longitudinal and vertical coordinates of $x_0 = 2.2$ and $z_0 = 0$. Rolling sidewash calculations are presented for points located longitudinally and vertically at $x_0 = 2.0$ and $z_0 = 0.2$. Calculations for both motions are at spanwise locations of $y_0 = 0$ and $y_0 = 0.15$ and at a Mach number of 1.64. Tables V and VI show the downwash and sidewash computations, respectively, for the points in the plane of symmetry. Tables VII and VIII give the downwash and sidewash computations, respectively, for the points at $y_0 = 0.15$.

In table V the first column gives the spanwise location of the trailing vortices. The second column gives the strength of the circulation as determined from figure 4 at the spanwise location of column (1). Column (3) gives the incremental circulation strength. Column (4) gives the $F_W\left(\left|y_{i,o}\right|\right)$ function from table II corresponding to $\beta m=2.0$, $x_0=2.2$, $z_0=0$, and the $\left|y_{i,o}\right|$ values of column (1). Note that no $F_W\left(\left|y_{i,o}\right|\right)$ values are given for $\left|y_{i,o}\right|$ values beyond 0.7. This indicates that the forecone from the field point at which the downwash is being determined intersects the lifting line between $\left|y_{i,o}\right|=0.7$ and $\left|y_{i,o}\right|=0.75$. Those horseshoes outside the forecone obviously do not contribute to the downwash. Twice the summation of the products of columns (3) and (4) gives the first term of equation (25) (when nondimensionalized as previously indicated) and, for the example calculation, is equivalent to -0.238. The last term in equation (25), that is, the product of the nondimensional circulation parameter $\frac{\Gamma_0}{V_\infty \alpha b/2}$ and $F_W,0$, is determined from column (2) and the value of $F_W,0$ given in table III.

The second term for the example calculation is equal to 0.126. Summing up the contributions of the two terms in equation (25) gives

 $-\frac{w}{V_{\infty}\alpha} = \text{-0.112.} \quad \text{To determine the downwash for any other point in the plane of symmetry at this same Mach number requires that the } F_{w}\left(\left|y_{i,o}\right|\right)$

and $F_{w,0}$ functions appropriate to the point being considered be obtained from tables II and III and used in the same manner as the numbers in columns (4) and (5) for the calculation just outlined. The calculating procedure for determining the rolling sidewash in the plane of symmetry (see table VI) follows closely that just outlined for determining angle-of-attack downwash and need not be discussed.

Calculations for the point off the plane of symmetry are slightly more lengthy than those for the plane of symmetry since the value of $Y_{i,0}$ for each value of $y_{i,0}$ and the value of \overline{X}_i for either the positive or negative $y_{i,0}$ values (\overline{X}_i is the same for positive and negative $y_{i,0}$ values) must be calculated. In table VII, which illustrates the angle-of-attack downwash calculation, columns 1 and 7 give the $y_{i,0}$ values of the vortices located on the left and right panels, respectively; columns 2 and 8 give the corresponding $Y_{i,0}$ values and column 3 gives the values of \overline{X}_i . The $F_w(Y_{i,0})$ functions corresponding to the $Y_{i,0}$ values of columns 2 and 8 and the \overline{X}_i values of column 3 are given in columns 4 and 9. (Note that $F_w(Y_{i,0}) = -F_w(Y_{i,0})$). The sum of the products of the values of $F_w(Y_{i,0})$ and the incremental circulation strengths $(\Gamma_{Y_{i+1}} - \Gamma_{Y_{i-1}})$ of column 5 are given in columns 6 and 10 . Substitution of the values of columns 6 and 10 into equation (15), nondimensionalized by $V_{\infty}\alpha$, yields 0.003 for de/d α .

The calculation procedure for rolling sidewash (table VIII) is essentially the same as that just outlined for angle-of-attack downwash with one exception. For the rolling motion the spanwise distribution of circulation is asymmetric; hence, the incremental circulation strengths on the right wing panel are of opposite sign to those on the left wing panel given in column (5). This difference accounts for the negative sign in the heading of column (0) in table VIII.

The results of the calculations for the wing of figure 8 and for the Mach numbers and points mentioned previously are presented in figures 11 to 13. Figure 11 gives the longitudinal variation of angle-of-attack downwash behind the wing along the x-axis. The inaccuracies in

the lifting-line method near the trailing edge are not too apparent in this figure except for the M = 2.19 curve. As pointed out previously, these inaccuracies may be minimized by determining the exact value at the trailing edge. By use of equation (30), in conjunction with the pressure expression given in reference 20, exact values of the downwash at the trailing edge have been obtained and are shown in figure ll as the circled point. It is felt that the dashed-line curves connecting the exact trailing-edge values with the troughs of the lifting-line curves give a reasonable approximation of lifting-surface results.

Variations with vertical height of lifting-line sidewash (in non-dimensional form) in the vertical plane of symmetry for the rolling motion are shown in figure 12. Values of the sidewash at $z_0=0$ were obtained by use of equation (31) and the spanwise distributions of circulation given in figure 10.

The spanwise variations of downwash and sidewash due to angle of attack and of sidewash due to rolling as calculated by use of the charts (eqs. (15) and (16)) and equations (1), (2), (25), and (27) are presented in figure 13. Figure 13(a), giving the spanwise variation of angle-ofattack downwash at $x_0 = 2.2$ and $z_0 = 0$, shows that the magnitude of the downwash computed by use of the charts does not agree well with the more exact values computed using equations (1) and (25). It further indicates that if the curve determined by use of the charts is translated so that the value at $y_0 = 0$ is made to coincide with that computed by the tables and equation (25) (as suggested earlier in outlining the proposed computing procedure), reasonably good agreement is obtained between the translated curve and the values computed from equation (1). For x_{O} values greater than 2.2 and a Mach number of 1.64 it is expected that the agreement between a translated chart-computed downwash curve and a curve computed from equation (2) would be as good as, if not better than, that shown in figure 13(a). On the other hand for x_0 values less than 2.2 the agreement will probably deteriorate from that shown in figure 13(a), with the worst agreement being at the outboard stations. should be remarked here that an increase in βm will have a similar effect on the flow-velocity variations at a particular longitudinal station as a decrease in x_0 for a particular value of βm .

The spanwise variations of sidewash due to rolling and angle of attack as computed from the charts, tables, and equation (2) are given in figure 13(b). It is evident from this figure that the chart-computed curves are in good agreement with the values computed using the tables (in conjunction with eq. (27)) and equation (2). Whereas the chart-computed curve of angle-of-attack downwash (fig. 13(a)) required a translation to obtain good agreement with the points computed from the yawed vortex equations, the rolling sidewash computed from the charts is in good agreement at y=0 and requires no translation. This situation will not necessarily be true for all x_0 values. The sidewash due to

angle of attack whether computed from the charts or from the tables and equation (27) is zero at $y_0 = 0$ because of the symmetry of the circulation distribution. Obviously no translation is necessary for this case. Increases or decreases in longitudinal distance will have an effect on the spanwise variation of sidewash similar to that mentioned in connection with downwash.

Langley Research Center,
National Aeronautics and Space Administration,
Langley Field, Va., December 1, 1958.

APPENDIX A

Derivation of Downwash and Sidewash Equations

The equation for the potential in space of a yawed lifting line with a variable circulation strength $\Gamma(y_1)$ and constant slope m may be obtained from reference 7 or 8 and is given by

$$\phi = \frac{\Gamma(y_1)}{2\pi} \tan^{-1} \frac{z\sqrt{x^2 - \beta^2(y^2 + z^2)}}{yx - \frac{z^2}{m} - \frac{y^2}{m}} \bigg|_{h_1}^{h_2}$$

$$\frac{1}{2\pi} \int_{h_1}^{h_2} \frac{d\Gamma(y_1)}{dy_1} \tan^{-1} \frac{z\sqrt{x^2 - \beta^2(y^2 + z^2)}}{yx - \frac{z^2}{m} - \frac{y^2}{m}} dy_1$$
 (A1)

where the equation for the lifting line is

$$y_{1} = mx_{1} \tag{A2}$$

(See fig. 1(a) for pertinent symbols, lifting-line geometry, etc.) For the potential in space of a yawed lifting line of constant circulation

strength, $\frac{d\Gamma(y_1)}{dy_1}$ is zero and equation (A1) reduces to

$$\phi = \frac{\Gamma}{2\pi} \tan^{-1} \frac{z\sqrt{x^2 - \beta^2(y^2 + z^2)}}{yx - \frac{z^2}{m} - \frac{y^2}{m}} \bigg|_{h_1}^{h_2}$$
(A3)

By definition this is also the potential for a yawed horseshoe vortex of the type depicted in figure l(b). A distribution of a number of these constant-strength horseshoes along a line can be used to approximate the potential of a lifting line with any prescribed circulation distribution. This approach, of course, represents an approximate numerical solution to equation (Al).

Partial differentiation of equation (A3) with respect to z and y yields the downwash and sidewash, respectively, due to a yawed constant-strength horseshoe vortex as

$$-w = -\frac{\Gamma}{2\pi} \left\{ \frac{Y_{m}^{3}X^{3} + m^{2}X^{2}(z^{2} - Y^{2}) - \beta^{2}m^{2}Y_{m}X(Y^{2} + 2z^{2}) + \beta^{2}m^{2}Y^{2}(z^{2} + Y^{2})}{m\sqrt{X^{2} - \beta^{2}(Y^{2} + z^{2})} \left[(Y - mX)^{2} + z^{2}(1 - \beta^{2}m^{2}) \right] (Y^{2} + z^{2})} \right\}_{h_{1}}^{h_{2}}$$
(A4)

and

$$v = \frac{\Gamma}{2\pi} \left\{ \frac{zY \left[2m^2 X^2 - \beta^2 m^2 (Y^2 + z^2) \right] - zmX (m^2 X^2 - \beta^2 m^2 z^2)}{m\sqrt{X^2 - \beta^2 (Y^2 + z^2)} \left[(Y - mX)^2 + z^2 (1 - \beta^2 m^2) \right] (Y^2 + z^2)} \right\}_{h_1}^{h_2}$$
(A5)

When m is set equal to infinity in equations (A^{\downarrow}) and (A5), respectively, the following expressions result:

$$-w = -\frac{\Gamma}{2\pi} \left[\frac{Yx^3 - \beta^2 Yx(Y^2 + 2z^2)}{\sqrt{x^2 - \beta^2 (Y^2 + z^2)}(x^2 - \beta^2 z^2)(Y^2 + z^2)} \right]_{h_1}^{h_2}$$
(A6)

$$v = \frac{\Gamma}{2\pi} \left[\frac{-zx}{\sqrt{x^2 - \beta^2 (Y^2 + z^2)}} \right]_{h_1}^{h_2}$$
 (A7)

Equation (A6) gives the downwash and equation (A7) the sidewash due to a rectangular horseshoe vortex; these equations agree with the expressions given for these quantities in references 6, 9, and 21.

It should be noted that equations (f4) to (A7) give the total contributions of the bound and trailing vortices. The separate contributions of the two components for the rectangular horseshoe vortex may be easily obtained. (See ref. 7.) Equatior (A6) written in the following form

$$-w = -\frac{\Gamma}{2\pi} \left[\frac{-\beta^2 xY}{\sqrt{x^2 - \beta^2 y^2 - \beta^2 z^2} (x^2 - \beta^2 z^2)} + \frac{Yx}{\sqrt{x^2 - \beta^2 y^2 - \beta^2 z^2} (Y^2 + z^2)} \right]_{h_1}^{h_2}$$
(A8)

gives the contributions at the bound and trailing vortices as the first and second terms, respectively. The sidewash due to a rectangular horseshoe vortex equation (A7), results solely from the trailing vortices. Since the contributions of the trailing vortices are the same for both yawed and rectangular horseshoe vortices, the trailing-vortex contributions for the latter (with x replaced by X to account for the displacement of the origin of the trailing vortices from x = 0) may be subtracted from equations (A4) and (A5) to obtain the bound-vortex contributions of a yawed horseshoe vortex.

With m, the slope of the bound vortex, defined as an absolute magnitude, expressions for the downwash and sidewash due to a yawed horseshoe vortex of negative slope are obtained by replacing m with -m in equations (A4) and (A5).

A swept horseshoe vortex of the form given in figure 4 may be obtained by combining yawed horseshoe vortices of opposite slope in such a way that two of these trailing vortices coincide along the x-axis. The effects of the two coinciding trailing vortices cancel leaving the effects of the two outboard trailing vortices and the two bound vortices, that is, a swept horseshoe vortex. Expressions for the downwash and sidewash due to a swept horseshoe vortex are, respectively,

$$-\mathbf{x} = \frac{\Gamma}{2\pi} \left\{ \frac{-(\mathbf{y} - \mathbf{h}_{2})(\mathbf{n}\mathbf{x} - \mathbf{h}_{2})^{2} - (\mathbf{n}\mathbf{x} - \mathbf{h}_{2})^{2} \left[\mathbf{z}^{2} - (\mathbf{y} - \mathbf{h}_{2})^{2}\right] + \beta^{2}\mathbf{m}^{2}(\mathbf{y} - \mathbf{h}_{2})(\mathbf{n}\mathbf{x} - \mathbf{h}_{2}) \left[(\mathbf{y} - \mathbf{h}_{2})^{2} + \mathbf{z}^{2}\right] - \beta^{2}\mathbf{m}^{2}(\mathbf{y} - \mathbf{h}_{2})^{2} \left[\mathbf{z}^{2} + (\mathbf{y} - \mathbf{h}_{2})^{2}\right] + \sqrt{(\mathbf{n}\mathbf{x} - \mathbf{h}_{2})^{2} - \beta^{2}\mathbf{m}^{2}\left[(\mathbf{y} - \mathbf{h}_{2})^{2} + \mathbf{z}^{2}\right] \left[(\mathbf{y} - \mathbf{n}\mathbf{x})^{2} + \mathbf{z}^{2}(\mathbf{1} - \beta^{2}\mathbf{m}^{2})\right] \left[(\mathbf{y} - \mathbf{h}_{2})^{2} + \mathbf{z}^{2}\right] + \sqrt{(\mathbf{n}\mathbf{x} + \mathbf{h}_{1})^{2} - \beta^{2}\mathbf{m}^{2}\left[(\mathbf{y} - \mathbf{h}_{1})^{2}\right] - \beta^{2}\mathbf{m}^{2}(\mathbf{y} - \mathbf{h}_{1})^{2} \left[(\mathbf{y} - \mathbf{h}_{1})^{2} + 2\mathbf{z}^{2}\right] - \beta^{2}\mathbf{m}^{2}(\mathbf{y} - \mathbf{h}_{1})^{2} \left[\mathbf{z}^{2} + (\mathbf{y} - \mathbf{h}_{1})^{2}\right] + \sqrt{(\mathbf{n}\mathbf{x} + \mathbf{h}_{1})^{2} - \beta^{2}\mathbf{m}^{2}\left[(\mathbf{y} - \mathbf{h}_{1})^{2} + \mathbf{z}^{2}\right] \left[(\mathbf{y} - \mathbf{n}_{1})^{2} + 2\mathbf{z}^{2}\right] - \beta^{2}\mathbf{m}^{2}(\mathbf{y} - \mathbf{h}_{1})^{2} \left[\mathbf{z}^{2} + (\mathbf{y} - \mathbf{h}_{1})^{2}\right] + \sqrt{(\mathbf{n}\mathbf{x} + \mathbf{h}_{1})^{2} - \beta^{2}\mathbf{m}^{2}\left[(\mathbf{y} - \mathbf{h}_{1})^{2} + \mathbf{z}^{2}\right] \left[(\mathbf{y} - \mathbf{n}_{1})^{2} + 2\mathbf{z}^{2}\right] - \beta^{2}\mathbf{m}^{2}(\mathbf{y} - \mathbf{h}_{1})^{2} + \mathbf{z}^{2}\right]} + \frac{-(1 - \beta^{2}\mathbf{n})\mathbf{y}(\mathbf{y} + \mathbf{m}\mathbf{x}) + (\mathbf{y} - \mathbf{m}\mathbf{x})^{2}}{\sqrt{\mathbf{m}^{2}\mathbf{x}^{2} - \beta^{2}\mathbf{m}^{2}(\mathbf{y}^{2} + \mathbf{z}^{2})} \left[(\mathbf{y} - \mathbf{n}\mathbf{x})^{2} + \mathbf{z}^{2}(\mathbf{1} - \beta^{2}\mathbf{m}^{2})\right]} + \sqrt{\mathbf{m}^{2}\mathbf{x}^{2} - \beta^{2}\mathbf{m}^{2}(\mathbf{y}^{2} + \mathbf{z}^{2})} \left[(\mathbf{y} + \mathbf{n}\mathbf{x})^{2} + \mathbf{z}^{2}(\mathbf{1} - \beta^{2}\mathbf{m}^{2})\right]}$$

$$(A9)$$

and

$$v = \frac{\Gamma}{2\pi} \left(\frac{z(y - h_2) \left\{ 2(mx - h_2)^2 - \beta^2 m^2 \left[(y - h_2)^2 + z^2 \right] \right\} - z(mx - h_2) \left[(mx - h_2)^2 - \beta^2 m^2 z^2 \right]}{\sqrt{(mx - h_2)^2 - \beta^2 m^2} \left[(y - h_2)^2 + z^2 \right] \left[(y - mx)^2 + z^2 (1 - \beta^2 m^2) \right] \left[(y - h_2)^2 + z^2 \right]} + \frac{z(y - h_1) \left\{ 2(mx + h_1)^2 - \beta^2 m^2 \left[(y - h_1)^2 + z^2 \right] \right\} + z(mx + h_1) \left[(mx + h_1)^2 - \beta^2 m^2 z^2 \right]}{\sqrt{(mx + h_1)^2 - \beta^2 m^2} \left[(y - h_1)^2 + z^2 \right] \left[(y + mx)^2 + z^2 (1 - \beta^2 m^2) \right] \left[(y - h_1)^2 + z^2 \right]} - \frac{z_0 \left[-(y + mx) + y(1 - \beta^2 m^2) \right]}{\sqrt{m^2 x^2 - \beta^2 m^2} (y^2 + z^2) \left[(y - mx)^2 + z^2 (1 - \beta^2 m^2) \right]} - \frac{z_0 \left[-(y + mx) + y(1 - \beta^2 m^2) \right]}{\sqrt{m^2 x^2 - \beta^2 m^2} (y^2 + z^2) \left[(y + mx) + z^2 (1 - \beta^2 m^2) \right]} \right)}$$
(A10)

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TABLE I.- VALUES OF $\beta m,~x_{0},~\bar{x},~z_{0},$ AND $y_{\mbox{i},0}$ FOR WHICH PLANE-OF-SYMMETRY FUNCTIONS ARE TABULATED

| βm | x_0 or \bar{x} | z _O | y _{i,0} |
|---|--|----------------|--|
| 0.4 .68 1.24 1.80 1.50 5.05 4.50 5.05 8 | 0.6 .8 1.2 1.4 1.6 1.8 2.0 2.2 2.6 3.0 3.5 4.0 5.0 | a 02.468 | 0 .05 .10 .15 .20 .25 .30 .35 .40 .55 .60 .70 .75 .80 .90 .95 |

aValues of $F_v(|y_{i,0}|)$ and $\left[F_v(|y_{i,0}|)\right]_{\beta m=\infty}$ for $z_0=0$ are zero; hence, no tabulation of these functions for $z_0=0$ is necessary. F_w functions are singular at $y_{i,0}=z_0=0$ and have been dropped from the computation procedure.

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_w(|y_{i,0}|)$

 β m = 0.2

| Хo | Vi,ol | z o = 0 | z ₀ = 0.2 | z _o : 0.4 | z _o = 0.6 | z _o = 0.8 |
|--|--|---|---|---|---|--|
| 66666666666666666666666666666666666666 | 00505050505050505050505050505050505050 | -1.46600000000000000000000000000000000000 | .120113 .028736 0385076 00677480 0067720737 00677207373 007322 0073222 0093957 00949104 1099643159 0099643159 00996431075 007531596 0075316596 0076310757 0076311065 007684004 109964314 109828888996 00849192 00849192 008494685 008494685 008494685 008494685 008494685 008494685 008494685 008486888 00849488 008486888 008489488 008816888 008816888 008816888 008816888 008816888 008816888 008816888 008816888 008816888 008816888 008816888 008816888 008816888 008816888 008816888 008816888 008816888 008816888 00881688 00881688 00881688 00881688 00881688 008816888 008816888 008816888 00881688 | 0938002 0695549 00495440 001564462 001564462 001564463 001564463 00164265 00164265 00164265 00164265 00164265 0016435 0016435 0016435 0016435 0016435 0016436 0016436 0016436 0016436 0016436 0016436 0016436 0016436 0016436 0016436 0016436 0016436 0016436 0016436 0016436 0016436 001636 | 06343154 043883149 03343160 03343160 03343160 03343160 03343160 03343160 03343160 03343160 03343160 03343160 03343160 03343160 03343160 03343160 03343160 03343160 03343160 03343160 033462224 03362224 03362224 033622233220 034323623321 0343236223322233222332223322233222332223 | 0.04428 0.044247 0.044247 0.0291544 0.02921544 0.02921544 0.02921544 0.0293154 0.0293154 0.0293154 0.0293154 0.0293154 0.0293154 0.0293154 0.0293154 0.0293154 0.0293154 0.0293154 0.03441421 0.014378 0.014478 0.01447 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(|\mathbf{y}_{i,o}|\right)$ - Continued

βm = 0.2

| ×о lyi,ol | Z ₀ =0 | z ₀ = 0.2 | z _o = 0.4 | z _o = 0.6 | z _o = 0.8 |
|-----------|---|--|--|---|--|
| 1.4 | -1.534846 4738539 27388539 2381074 1738522 20811447 119458 101945933 074459333 07445933 0047931 005563 0047931 00244607 00244607 00244607 00244607 00244607 012468293 012468293 012468293 12683293 13683293 13683293 03735343 0373535 0373535 038535 038535 038535 038535 038535 038535 038535 038535 038535 038535 038535 038535 038535 | - 057727727-109655079607727-11352242779796077-11342807979797-110293797979-110293797979-110293797979-1004499979-1004495979-100449597999-100449597999-100449597999-100449597999-100449999-1004499999-1004499999-10049999-10049999-10049999-10049999-10049999-10049999-1004999-1004999-1004999-1004999-1004999-100499-10099-10099-100999-10099-10099-10099-10099-10099-10099-10099-10099-10099-10099-1 | 0527374 002837472 00283774 00283774 00124720 00124720 001245977 00462433 00454438 00454438 00454438 00454438 00454438 00454438 00454438 00454438 00454438 00454438 00454438 00454438 00454438 00454438 00128520024 001286034 001286034 001286034 001286034 001286034 001286034 001286034 001287478 001286034 001287338 001287338 001287338 001287338 001287338 001287338 001287338 001287338 001287338 001287338 001287338 001287338 001287338 001287338 001287338 001287338 001287338 001287 | 0484999 .0375661 .0375661 .03775661 .03775661 .03770831 .00184084 .00182409 .001828409 .00168740 .00168770 .00188770 .001887661 .001887661 .001887661 .001887661 .001887661 .001887661 .001887661 .001887661 .001887661 .001887661 .001887661 .001887661 .001887766 .002848619 .001887661 .001887661 .001887661 .001887661 .001887661 .001887661 .001887661 .001887661 .001887661 .001887661 .001887661 .001887661 .001887661 .001887661 .001887661 .001887661 .001887661 | . 0 4 3 5 6 1 . 0 3 7 4 10 9 . 0 2 5 3 6 1 2 . 0 3 1 4 10 9 . 0 2 5 3 5 8 8 . 0 1 1 1 4 2 9 . 0 0 1 5 4 9 8 8 . 0 1 1 6 2 8 8 . 0 1 1 4 2 9 . 0 0 1 4 2 4 8 . 0 0 1 6 4 8 0 . 0 0 1 4 6 8 0 . 0 0 0 2 4 2 7 7 . 0 0 4 4 6 8 0 . 0 0 0 4 4 6 8 8 . 0 0 1 4 6 8 8 1 . 0 0 0 4 4 9 9 7 . 0 0 4 4 9 9 7 . 0 0 4 4 9 1 7 . 0 0 4 4 9 1 7 . 0 0 4 4 9 1 7 . 0 0 4 1 3 1 5 2 . 0 0 2 2 2 4 4 9 1 . 0 0 2 2 2 4 4 9 1 . 0 0 2 2 2 4 4 9 1 . 0 0 2 2 2 4 4 9 1 . 0 0 2 2 2 4 4 9 1 . 0 0 2 2 2 4 4 9 1 . 0 0 2 2 2 4 4 1 . 0 0 2 2 2 4 4 1 . 0 0 2 2 2 4 4 1 . 0 0 0 8 3 5 6 2 . 0 0 1 2 8 9 5 . 0 0 0 4 8 9 4 7 . 0 0 0 8 1 9 2 9 6 . 0 0 0 7 8 8 1 2 9 . 0 0 1 2 8 9 4 7 . 0 0 1 2 8 9 4 7 . 0 0 1 1 4 6 6 5 7 . 0 0 1 1 6 5 5 1 . 0 0 1 1 6 5 5 1 . 0 1 1 1 6 5 5 1 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}\right)$ - Continued

 β m = 0.2

| | | | βm = | 1 | | |
|-----|--|--|--|--|--|--|
| | Vi,ol | z _o = 0 | z _o =0.2 | Z ₀ = 0.4 | z _o =0.6 | Zo=0.8 |
| 1 1 | 667788999000112233444556667788990001122333445566778899 | -1.5559456 19443 2257465 155843297 155843297 155889191 1045959 11545959 11545959 1098234635 008234635 008234635 008234635 008234635 008234635 004338985 004338985 00438985 00438985 00438985 00438985 00438985 00438985 00438985 00438985 00438985 00438985 00438985 00438985 00438985 11664464 112822916611 1282916611 1096595776 005517041 | - 039418 - 039418 - 015945037 - 115945037 - 11594508 - 11594508 - 11594508 - 11594508 - 11594508 - 11987506006 - 10987920254 - 10987920254 - 10987920254 - 1095336498 - 1095336498 - 109533669 - 109533669 - 109533669 - 109533669 - 109533668 - 109687728 - 116873109 - 116873109 - 116873109 - 1168731664 - 1168731664 - 1168731664 - 11687316664 - 116873166664 - 1168731666664 - 1168731666664 - 1168731666 | . C3834830 C4814931 C4814941 C5700744 C5700744 C55700744 C55700744 C5534481 C66022431 C66022431 C5530912661 C5530912661 C5530912661 C537480722 C64377923684 C6337480722 C6337480722 C6337480722 C6337480722 C6337480722 C6337480722 C6337480722 C6337480722 C6337480722 C6337480722 C6337480722 C6337480722 C6437723 C6337480722 C6337480722 C6337480722 C6437407056411 C65374661736642 C65374676 C6537466 C6 | .036690 .0156249 .016219 .0105302899 .010550092 .01062164288 .010247388 .012247388 .012247388 .012247388 .012247388 .012247388 .012247388 .012247388 .012247388 .012247388 .012247388 .012247388 .012247388 .012247388 .012247388 .012247388 .012247388 .012251288 .012251288 .012251288 .0123128128 .0123128128 .0123128128 .0123128128 .0123128128 .0123128128 .0123128128 .0123128128 .0123128128 .0123128128 .0123128128 .01313817 .0123128128 .01313817 .0123128128 .01313817 .0123128128 .01313817 .0123128128 .01313817 .0123128128 .01313817 | .034602 .0284402 .0284402 .016898 .00163982 .00163982 .0017984 00179837 001478674 011426684 011426884 01145398 01145398 01145398 01145398 01145398 01145398 01145398 01145398 01145398 01145689 0114568997 .001468997 .00167698 .002692406 00167698 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{\mathbf{i},o}\mathbf{I}\right)$ - Continued

| xo y _{i,o} zo=0 zo=0.2 zo=0.4 zo=0.6 zo=0.8 3.0 .00 .026415 .026090 .025565 .024866 |
|--|
| 3.0 |

TABLE II. - TABULATION OF THE DOWNWAS I FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y_{i,o}}\mathbf{I}\right)$ - Continued

<u>βm=02</u> **z**o = 0 $z_0 = 0.2$ $\mathbf{x}_{\mathbf{0}}$ $z_0 = 0.4$ zo=0.8 Di,ol Zo= 0.6 Zo=Ub

.015703
.004730
-005798
-0015494
-024072
-031367
-037328
-0419489
-047927
-050322
-050368
-047927
-04947927
-049489
-050352
-049779
-0484938
-0447898
-0447898
-044671
-0446730 20-02
- 015892
- 077726
- .1432257
- .175084
- .1831838
- .167728
- .131246
- .1312746
- .111858
- .103481
- .095899
- .083111
- .077668
- .077668
- .068244 -1.575631 -.779853 -.514591 -.381959 -.302378 -.211425 -.183001 -.160892 -.143204 -.116670 -.106464 -.097715 -.090132 -.083496 -.072434 -.067776 -.063582 .00 .015820 . 015542 . 009352 . 009356 - 002466 - 007850 - 017141 - 020962 - 024219 - 026931 - 029129 - 030857 - 033093 - 033702 - 034034 - 034038 - 033781 - 033781 - 033781 - 033781 .015542 .00 .05 .10 .15 .20 .25 -.0086683 -.0309883 -.043744 -.073576 -.073576 -.0886527 -.0882934 -.0881190 -.073973 -.0637395 -.06373961 -.0637961 -.0532701 .008662 . 40 . 4 5 . 5 0 . 5 5 .60 .65 .70 .75 .85 .90 .95 -.064344 -.060546 -.033394

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}\right)$ - Continued

 β m = 0.4

| Хo | Yi,o | z ₀ =0 | z ₀ = 0.2 | z ₀ = 0.4 | z ₀ = 0.6 | z _o = 0.8 |
|--|--|---|--|---|---|--|
| 66666668888880000000000000000000000000 | 05050505050505050505050505050505050505 | -1.4579556694339917795417078448770784789 -1.12155877039789 -1.4952751016952751012151654672957510112154670961365104444850215944112156934411215693441121569344109613366032814449871423669328144498714236693281444987142369328155894940727898949407289844026937468073787468084843026937468073787468084843026937468073787468084843026937468073787468147888441534888426937468073787468084888826937468094944770199888882693746807378746808488884207937468084888884208991050144422 | . 122400 .0297888 0344523 0344523 0670824 063311 068311 0693190017 094190017 094190017 095361189 0953611 0953611 0953611 0953611 0953611 006551728 006551728 016551728 016551728 016551728 016551728 016551728 016189494 01761894 01818193 0197944855 0197944855 019794486 019794486 019794486 019794486 019794486 019794486 019794486 019794486 019794486 019794486 019794486 019794486 019794486 019794486 019794486 019794486 019794486 019794486 01979486 0 | 100203 .076872 .055988 .0372641 .021607 .0212682 .037284 .0021607 .0237284 .0037284 .0037284 .0003903 .0383561 .0073349 -0013884 -00649860 .013606 .0071065 .00469864 -002356864 -00235888 -013702 -00213888 -001488270 | .078647 .069133 .0691334 .0491344 .049640 .06003000 .0700815 .060501 .0507541 .034592 .0248871 .02447534 .02347534 .002447534 .002447534 .002447534 .002447534 .002447534 .002447534 .002447534 .002447534 .002447534 .00247534 .00247534 .00247534 .00247534 .002557 .002557 .00262349 .0132557 .00132557 .00132557 .00132557 .00132557 .001444 .0132557 .0017859 .044948 .017836 .04444 .017836 .045936 .045936 .0499888 .049988 .049888 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .049888 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .049888 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .049888 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .049888 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .049888 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .049888 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .049888 .049888 .049888 .049888 .049888 .04988 .04988 .04988 .04988 .04988 .04988 .04988 .0 | 062884 058799 055814 05587666 060182 1077000 0000000 00550666 060182 10070000 0000000 0058988 00485950 0040150 0040150 00374370 0036479 005158450 0040000 00588450 00400000 00588425 00000000 005488647 00488647 00488647 00488647 00488647 00488647 00488647 00488647 00488647 00488647 00488647 00488647 00488647 00488647 00488647 00488647 00488647 00235652 0020000 005441886 00235552 0030000 00544188647 001131999 001386340 00139994 00139994 00139994 001399994 001399999999999999999999999999999999999 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(| \mathbf{y}_{i,o} | \right)$ - Continued

| | | Pil | 1=0.4 | | |
|----------|--|---|----------------------|---|--|
| ×о Уі,о | z ₀ =0 | z _o = 0.2 | 2 ₀ = 0.4 | z _o = 0.6 | z _o =0.8 |
| 1.66 | -1.5416853-3447583-321765183-321765183-321765183-321765163-3-1107284704-10080977404-10080977404-10080977404-10080977404-10080977404-10080977404-10080977404-10080979-1158535359-12823744570835-10080618099-115853589-10080618099-115861237809-1 | - 0443355 - 10473355 - 11497355 - 11497355 - 11497355 - 114921961 - 114921961 - 11431155 - 112869310 - 00865768382 - 00865768382 - 007677836 - 005927355 - 00497146 - 005927146 - 003944990 - 001497146 - 001497146 - 114911386926 - 00497146 - 11491136436 - 11491136436 - 11491136436 - 114911364 - 11491136 - 11591146 - 11591146 - 11591146 - 11591146 - 11591166 - 0032798 - 0055667695 - 0057695 - 0057695 - 0057695 - 00576996 - 0057696 - 005766 - 005766 | | .044991 .0347639 .0145809 .0145809 .001715809 .001715809 .001715809 .001715809 .001715809 .001715809 .001715809 .001715809 .001715809 .001715809 .001715918 .0018001 .0018001 .0018001 .0018009 .0018009 .00199474 .002094779 .0020947898 .0019947898 .001994779 .0020995109 .0011603410 .00203360309 .0019947898 .0019995109 .0011603410 .00203360309 .0019999109 .00116034100 .00203360309 .0018039970 .00203360309 .0018039970 .00203360309 .001999910 .00199910 .0018039907 .00203360309 .0018039907 .00203360309 .00199910 .00203360309 .00199910 .00203360309 .00199910 .00203360309 .00199910 .00203360309 .00199910 .002033707 .002033707 .002033707 .002033707 .002033707 .002033707 .002033707 .002033707 .002033707 .002033707 .002033707 .002033707 .002033707 .002033707 .0020339907 .002033707 | .0419908 .0359001 .03191755 .030431755 .00102491755 .00102491755 .00102667383 .00102344982 .00003344982 .00003344982 .0000334982 .0000334982 .0000334982 .0000334982 .0000334982 .0000334982 .0000334982 .0000334982 .0000334982 .0000334982 .00000354982 .000000000000000000000000000000000000 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}\right)$ - Continued

 $\beta m = 0.4$ |Yi,o| zo=0 Zo= 0.4 Χo $z_0 = 0.2$ $z_0 = 0.6$ Zo=0.8 .035946 .035288 .010870 $032905 \\ 026783$ 5.5 1.555311 -.759465 -.494133 . 05 .123071 .154827 .162707 .157773 .10 .15 .20 .011383 .012883 020808 2.22.22.22.23 -.029904 -.043996 -.053749 .003260 .015111 .361426 .005242 .009806 -.04537441
-.0597441
-.063530
-.0662741
-.05583622
-.05522627
-.045276
-.0552263627
-.045276
-.035644666444
-.0353565 . 25 .30 .228629 .147235 .018331 .000686 . 2 .003041 -.190644 -.162128 -.139921 -.122129 -.107546 -.095366 -.085033 .122562 . 40 .026298 .006199 .45 . 2 .028641 .008805 -.030095 -.030810 -.030931 -.030581 .010891 .100399 .090870 .082324 .074665 .067788 .0615990 .0559901 .046258 2.2 .012497 .60 - .030 931 - .030 581 - .029 865 - .028 867 - .027658 - .026292 - .024812 - .023251 - .021630 .029422 .018495 .008014 .65 .70 2.2 .014464 . 2 -.068419 -.061625 -.055597 -.050205 2.2 . 2 .015090 .80 .015010 2.2 .85 .014718 .014245 2.2 -.045342 .041998 -.013618 -.012857 .028569 .028426 .016428 .010707 .005376 .000521 -.003802 -.007561 -.013407 -.013507 1.00 -.040923 .038072 -1.560895
-.765070
-.499760
-.367077
-.28744332
-.196376
-.167891
-.145719
-.113421
-.101285
-.0910000 2.6 .00 030470 .05 . 128 587 .008014 -.001632 -.010159 -.017399 -.023303 -.027913 -.031335 2.6 .160366 . 15 · ž o .25 2.6 .163360 2.6 .140546 -.068139 -.068954 .116685 .106147 .096658 .088157 - .033715 - .035207 - .035207 - .035839 - .035180 - .035180 - .034247 - .033110 - .031826 - .028981 - .027481 .025746 .01480 .004513 - .005547 - .013889 . 6 . 4 5 -.0668200
-.066388
-.06610097
-.057902
-.0551527
-.045363
-.045363
-.045363
-.0396384
-.036973
-.026173
-.020564
-.0391222 068200 2.6 .015527 5.5 60 .018405 .019254 .019774 .020012 2.6 .65 .080547 2.6 .082168 -.073723 -.067587 -.062050 -.057035 -.052473 -.048307 ಕ 0 ಕ 5 .020011 2.6 .061813 .056502 2.6 9 0 9 5 .019436 .048307 -.044486 .026437 -.067148 -.132645 -.16447 018925 3.6 .00 .018299 .025174 .019018 .013007 1.564988 -.769176 -.503879 -.371210 -.291591 -.238497 0 5 1 0 1 5 .0 -.132645 -.164437 -.172355 -.167462 -.156967 -.144680 -.039121 -.053252 -.063046 -.069083 -.072136 -.072970 -.072935 -.070444 -.067979 -.065111 -.0652032 -.055717 -.052622 -.0496227 -.0496227 -.043977 -.043977 .007272 .001925 -.002947 -.007286 -.0110648 -.014278 -.016943 -.019094 -.020771 -.022023 -.013889 3.0 .20 .25 -.013889 -.021145 -.027066 -.031693 . 0 .200558 .172091 .149938 -.031693 -.035135 -.037534 -.039049 -.039832 -.040027 -.039757 -.039127 - 0 40 .132391 .132204 - .110340 - .100874 - .092397 - .084812 3.0 5.0 60 .105571 65 70 75 .022900 .086508 -.078016 -.071910 -.039127 -.038226 -.037124 -.035877 -.034531 -.023722 -.023757 . 0 -.066406 -.061427 -.056903 80 .072170 8.5 .066250 -.023594 -.023266 3.0 .90 1.00 -.056248 -.051980 -.052780 -.049006 -.033119 -.031670 3.0 -.022804 -.022231

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}$ (Iy $_{\mathbf{i},\mathbf{o}}$ I) - Continued

| xo y _{i,o} | z ₀ = 0 | z ₀ = 0.2 | z ₀ = 0.4 | z ₀ = 0.6 | z _o = 0.8 |
|-----------------------|---|---|--|---|--|
| 3.5 | -1.5629899999999999999999999999999999999999 | - 0 2 0 4 1 4 2 1 4 1 4 | 2513 -032513 -032513 -0342813 -0342813 -0342813 -03567598 -03725759 -03725759 -03725723 -03725723 -03725723 -03725723 -03725723 -0352723 -0352723 -0352723 -0352723 -0352723 -0352723 -0352723 -0352723 -0352723 -0352723 -0352723 -0352723 -0352723 -0352723 -0352723 -0352723 -0352723 -035273 -035273 -035273 -035273 -035273 -035273 -035273 -035273 -035273 -035273 -035273 -035273 -035273 -035273 -035273 -03727 | . 022241 . 011291 . 0008883 - 00174836 - 00247058 - 00352735 - 00411479 - 00424799 - 00434640 - 00428312 - 00436500 - 00386528 - 00415884 - 003865528 - 00415884 - 00207426 - 00383017 - 00385528 - 0018908 - 00115844 - 00227426 - 00438472 - 00438478 - 0044862470 - 004464232 - 00456565 - 00115844 - 002333012285 - 00157828 - 004862470 - 00486232 - 00486232 - 00486232 - 00486232 - 00486232 - 00486232 - 00486232 - 00486232 - 00486232 - 00486232 - 00486232 - 00486232 - 00486232 - 00486232 - 00486232 | . 0 2 1 8 7 2 . 0 1 5 7 0 6 . 0 0 9 9 3 8 . 0 0 0 1 4 2 0 . 0 0 1 5 7 0 6 . 0 0 9 9 3 8 . 0 0 1 4 2 0 . 0 1 6 3 0 5 7 . 0 1 4 4 4 4 9 . 0 1 7 3 5 8 4 . 0 2 2 5 2 8 4 . 0 2 2 6 9 5 7 0 . 0 2 7 1 7 1 1 8 8 . 0 2 7 1 7 1 1 8 8 1 0 . 0 2 7 1 7 1 1 8 8 1 0 . 0 2 7 1 7 1 1 8 8 1 0 . 0 2 7 1 7 1 1 8 8 1 0 . 0 2 7 1 7 1 1 8 8 1 0 . 0 1 3 1 3 0 8 1 0 . 0 1 3 1 3 0 8 1 0 . 0 1 3 1 6 0 9 9 1 1 3 . 0 0 1 3 2 1 6 7 6 9 9 9 1 1 3 . 0 0 2 2 9 1 6 7 6 1 3 8 8 1 0 . 0 1 2 2 9 6 6 1 5 1 8 1 8 1 8 1 8 1 8 1 8 1 8 1 8 1 8 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{y}_{\mathbf{i},o}\right)$ - Continued

| x _o y _{i,o} | z _o = 0 | z ₀ = 0.2 | z ₀ = 0.4 | Z _O = 0.6 | z ₀ = 0.8 |
|---|---|--|--|---|--|
| .66.66.66.66.66.66.66.66.66.66.66.66.66 | -1.45637448354883771061321061402106140210614021061402106140210614021061402106140210614021061402106140210614021061402116336730226344112207925730114604421210444273004442121044427300444212104442731044427310444273104442731044427310444273104442731044427310444273104442731044427310444273104442731044427310444273104442731044427310444473112665511411266551441126655114 | .123544553440700384555700054554562244558570005455570006455857000645585700064558570006455857000645585700064558670006455867000645586700064558670006455867000645586700064558670006455867000645586700666700667006670066700667006670066 | .112664 .091471 .0735128 .0561993 .0680600 .005089898 .04663492 .021840976 .0158498 .012840976 .0158411 .007473920 .0158411 .007473920 .011992470 .011992470 .011992470 .011992470 .011992470 .0011992470 .0011992470 .0011992470 .0011992470 .0011992470 .0011992470 .0011992470 .0011992470 .0011992470 .0011992470 .0011992470 .0011992470 .0011992470 .00119920 | .1010893 .0964948 .0900000 .0000000000000000000000000000 | 103401 1113299 10140000 100000000 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}\right)$ - Continued

βm=0.6

| Хo | y _{i, o} | z ₀ =0 | z _o = 0.2 | Z _C = 0.4 | z _o = 0.6 | Z _O = 0.8 |
|--|--|---|--|---|--|--|
| 2.0 0.000000000000000000000000000000000 | 00505050505050505050505050505050505050 | -1.544944 -1.1746155299-1.174613189-1.174813189-1.1746 | - 04939457 - 1144826204484 - 114483144444444444444444444444444444444 | . 0 4 4 1 9 9 0 1 6 9 8 4 7 9 0 1 6 9 8 4 7 9 9 1 0 1 6 9 8 4 7 9 9 1 0 1 4 1 1 1 1 2 9 2 9 1 1 1 1 1 1 1 1 1 1 1 1 | .046830 .02679 .026677 .00816556 .0016677 .0016819 .00124409 .001243682 .00123133882 .00123133882 .001231738 .001231739 .001231739 .001231739 .001231739 .00117139 .001184092 .00117139 .001185227 .001845227 .001845227 .00184648 .001773 .0002458 .001773 .0018492 .00185227 .00185227 .00185227 .00176677 .00176677 .00176677 .00177668 .0017668 | . 0449447 . 0334497 . 0283176.5 . 01849447 . 0283176.5 . 0184945 . 00184946.6 . 00184946.6 . 0018496.6 . 001848.6 . 000548.6 . 000548.6 . 000699.7 . 00188.7 . 00188.7 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $~{\rm F_{w}}~({\rm Iy_{i,o}I})$ - Continued

βm=0.6

| x _o y _{i,o} | z _o = 0 | βm= z _o = 0.2 | z _o = 0.4 | z _o = 0.6 | z _o = 0.8 |
|---------------------------------------|---|---|--|---|---|
| 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 | -1.55593886642 -1.75593886642 -1.75593886642 -1.861305579 -1.189133833 -1.10933444793 -1.10933444793 -1.0933444793 -1.0933441927 -1.0934447355 -1.0934447355 -1.093441927 -1.04475359 -1.04475359 -1.04475359 -1.04475359 -1.04475359 -1.04475359 -1.04475359 -1.04475359 -1.04475359 -1.04475359 -1.04475359 -1.04475359 -1.04475359 -1.04475359 -1.04475359 -1.14496731 -1.110949681 -1.110949681 -1.110949681 -1.110949681 -1.110949681 -1.1109496999 -1.110949699 -1.110949699 -1.110949699 -1.110949699 -1.1109496999 -1.11094969 -1.11094969 -1.110969 -1.110969 -1.110969 -1. | . 0 3 5 5 4 8 4 7 2 8 8 0 3 0 3 3 4 2 3 6 3 8 0 3 0 3 3 4 2 3 6 3 8 3 2 3 6 3 8 8 6 7 2 4 8 8 0 3 0 3 3 2 3 3 3 3 3 3 3 3 3 3 3 3 3 3 | 3556116504470223388982425974683772468377288395277938764384716506665555544415881473956239463142956234233889488441588147395644811495662344335577938862394363476529639666464311864355779388639766666555555443356777666665555443356777766666555544335677776666655554443586777766666656666666666666666666666666 | .034333 -00443922 -0111926 -012146446 -012146446 -012146446 -012146446 -012146446 -012146446 -012146446 -012146446 -012146446 -012146446 -01214646 -01214646 -01214646 -01214646 -01214646 -01214646 -01214646 -01214646 -01214646 -01214646 -01214646 -01214646 -01214646 -01214646 -01214646 -01214646 -01214646 -0121466 -0 | .034149 .022461599 .0224615990 .000393513 .000393513 .000393513 .000393513 .000393513 .000393513 .0003936736 .0011148919 .0011188919 .0011188919 .0011188919 .0011188919 .0011188919 .0011188919 .0011188919 .001177622 .001177515 .001177515 .001177515 .001177515 .001177515 .001179553 .001177515 .001179553 .00117955 .0011795 .0011795 .0011795 .0011795 .0011795 .00117955 .00117955 .0011795 .0011795 |

TABLE II. - TABULATION OF THE DOWNWAS+FUNCTION $F_{\mathbf{w}}$ (I $\mathbf{y}_{i,o}$ I) - Continued

| xo Vi,ol | z ₀ = 0 | z ₀ = 0.2 | z ₀ = 0.4 | z _o = 0.6 | z ₀ = 0.8 |
|----------|---|---|--|--|---|
| 3.5 | -1.56875477299737490329421382041673123573841756497135738410997517082243098924307555590694285107571689069424830757168905518906942481055180 -1.57168905518906942481055189069424810551890694248307574870551890778651158748448112483350930379078675706277467058468111683220977289164284160114284216116832209772891642841601142842161168322097728907871160771160771160771160771160771720627942 | .020592 0706592 16679973 116879973 116879973 116879976 1171052392 11687996 1171052392 1188996 1188996 1188996 1188996 1188996 1188996 1188996 11896 11896 118996 118996 11896 11896 11896 11896 11896 | 0124040404050507050507050705050705050705050705050705050705050705050705000000 | .02420 .0115523 .001058399 .001870999 .001870999 .001870999 .001870999 .001870999 .001870999 .001870999 .0018709999 .0018709999999999999999999999999999999999 | .02459491 .0103333316 .022689222 .011308393 .001038393 .001038393 .001038393 .001038393 .001038393 .001038393 .001038393 .001038393 .001038393 .0021038393 .0021038393 .0021038393 .0021038393 .0021038393 .00210389393 .00210389393 .0010389393 .0010389393 .0010389393 .0010389393 .0010389393 .0010389393 .0010389393 .0010389393 .0010389393 .0010389393 .0010389393 .0010389393 .001038939393 .001038939393 .001038939393 .001038939393 .001038939393 .001038939393 .0010389393939393939393939393939393939393939 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{i,o}\mathbf{e}\right)$ - Continued

| Хo | Ni, ol | z _o = 0 | z ₀ = 0.2 | z ₀ = 0.4 | z _o = 0.6 | z _o = 0.8 |
|---|--|---|---|---|--|---|
| .66 .66 .68 .88 .88 .88 .88 .88 .88 .88 | 05050505050505050505050505050505050505 | -1.4546479384311390795414283777 -1.489236615714923661571492366157149236615714924616183159261936183 -1.7713039534602203484262144648271096183 -1.771303973260747365033744642621192661936611226617304801192661891192661899 | .13433889 .0046044167 .004041667 .0098477998 .008774489 .0087734187 .009794766673 .0077266673 .0077883887 .10588887 .0077888887 .0077888887 .0077888887 .0077888887 .0077888887 .0077888887 .0077888887 .0077888887 .0077888887 .0077888887 .0077888887 .0077888887 .0077888887 .0077888887 .0077888887 .0077888887 .0077888887 .0077888887 .00778888887 .00778888887 .00778888887 .00778888887 .00778888887 .00778888887 .008888887 .008888887 .008888888888 | 6304473000 723582988800075054884000690946469902908468857293745400069094642855000753396885729374540006620622169824316614522006690824316982431661452200662069082431698243161452200662062169824431698000621100006211000062110000621100006211000062110000621100000000 | 162536 191033 .0000000 .0000000 .0000000 .0000000 .0000000 .0000000 .0098270 .11832060 .00000000 .00803753 .006471344 .00000000 .087173444 .00531285 .000000000000000000000000000000000000 | .0000000 .0000000 .0000000 .0000000 .000000 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}\right)$ - Continued $\beta \mathbf{m} = 0.8$

| Хo | Yi, 0 | z ₀ =0 | z _o = 0.2 | z _o = 0.4 | z _o = 0.6 | z ₀ = 0.8 |
|--|---|--|--|---|---|--|
| 1.6 1.6 1.6 1.6 1.6 1.6 1.6 1.6 1.6 1.6 | .00505050505050505050505050505050505050 | -1.5413007449131345810265818173181511731815117318151173181511731815117318151173181510162120072783405092705099270218813039984130218801715180992718201715068269094036460597793115786826910177115553304402365711155330440246686605047666817612824815115533044029951111553304402995130766686605043476402034576440203457644 | .04970704835601493660133689591336856013368595913370873890110370873890010491890005998907500599890750049171183002928890004911718500292889000491171850029288901145275446568883126670059876751630291155724665694500598767591630291155724666888315668 | .049645 .0257037 -013937 -0139399 -0139399 -0416900 -0436707 -034707 -034707 -034707 -034707 -034707 -03446157 -01048435 -0010471 -0104841 -0010471 -0010435 -001045 -00104 -00104 -00104 -00104 -00104 -00104 - | .049685 .029497 .012740 .0020497 .012740 .0014035 00214035 0050336 0050336 0050336 0050336 0050336 0050336 0050336 0050336 0050336 0050336 0050336 0050336 0050335 0050337 00503334 01133771 012372 007692 007692 00104429 007692 001044379 01176993 01176993 01176993 01176993 01176993 01176993 01176993 01176993 01176993 01176993 01176993 01176993 01176993 01176993 01176993 01176993 01176993 01176993 0118652 0116652 01166593 011665993 01166993 01166993 01166993 01166993 01166993 01166993 01166993 01166993 01166993 01166993 0166993 01166993 01166993 01166993 01166993 01166993 01 | .044352 .034284 .024287 .034284 .022427 .023119 .0204401 .0118909 .0125674 .025674 .034092 .0581884 .0000000 .00441605 .0380557 .02772259 .0155654 .0105108 .01158654 .010907925 .0158654 .010907925 .0158654 .010907925 .0158654 .010907925 .0158654 .010907925 .0158654 .010907925 .0158654 .010907933 .0158654 .010907933 .0158654 .01090793 .0158654 .01090793 .0158654 .01090793 .0158654 .01090793 .0158654 .01090793 .0158654 .01090793 .0158654 .01090793 .0158654 .01090793 .0158654 .01090793 .0158654 .01090793 .0158654 .01090793 .0158654 .01090793 .0158654 .01090793 .0158654 .00090793 .00 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}$ ($\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}$) - Continued $\beta \mathbf{m} = 0.8$

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{Iy}_{i,o}\mathbf{I}\right)$ - Continued

βm = 0.8

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}$ (Iy,oI) - Continued

βm=1.0

| x _o y _{i,o} | z _o = 0 | z _o = 0.2 | z _o = 0.4 | z _o ≈ 0.6 | z _o = 0.8 |
|---|--|---|--|---|---|
| .6 .0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | -1.44973300 -1.489747320 -1.22979499 -1.489747320 -1.229794997531300 -1.4897492499 -1.4819249992955050505050505050505050505050505050 | .140674 .055082 .0000000 -017014 .00823446 .102983 -0172983 -0175194 -0075194 -0075194 -0075194 -0075194 -006031871 -1067399 -0112983 -010731871 -1067298 -0072488669 -00747888669 -008886699 -008886699 -008886699 -008886699 -008886699 -108886699 -110739888669 -010739888669 -112888669 -112888669 -112888669 -112888669 -1139888669 -1139888669 -114888669 -117398888669 -117398888669 -117398888669 -117398888669 -117398888669 -117398888669 -117398888669 -117398888669 | .177941 .176688 .1985999 .354577 .00000000 .0196787 .0827506 .07956577 .107482 .00000000 .086826 .04756577 .107482 .00000000 .086826 .0442634 .02144990 .004472 .0000000 .086826 .0045940 .00214997 .007741 .0000000 .0085931490 .002141173 .00000227365 .001429411 .0015854421 .0015854421 .001687 .0026414285 .0026414285 .0026414285 .0026414285 .0026414285 .0026414285 .0026414285 .0026441173 .000000000000000000000000000000000000 | .0000000 .0000000 .0000000 .0000000 .000000 | . U 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}\right)$ - Continued

βm = 1,()

| | r | T**** | r | | , | |
|--|---|--|--|--|---|---|
| Хo | ly _{i,ol} | z _o = 0 | z _o = 0.2 | z _o = 0.4 | z _o = 0.6 | z _o = 0.8 |
| 1.888888888888888888888888888888888888 | .00505050505050505050505050505050505050 | -1.54670844842933502611216582177051121658217850441256123125612306452505351670535167053516705351670535167154140115415410111541640111541640111541640111541640111541640111541640111541640111541640111541640111541640111541640111541640111541640111541640111541640111541640111541640107824662064468550627641158764115876411587641158764115876411587703226740158770322674006446855064468506446855 | .0444485 14133295 11444997 15159397 14445997 134459938 10757487 10757487 10953457 00824695 0082465 0082465 0082465 0082465 0082465 00826 | .045343 .0200000 017784 031988 045916 0446605 0446605 0446511 0446605 044611 031910 036203 0116614 .000080 016604 016604 016604 016604 016604 0236513 03553170 05531899 0553189 0553189 0553189 0553189 0553189 0553189 0555569 055569 055569 055569 05569 05569 05569 05569 05569 05569 05569 05569 05569 05569 05569 0569 05569 05569 05569 05569 05569 0569 | .046891 .036739 .0270971 .016829 .0016850 .00003391 .0055071 .0005106 .0005106 .0005106 .0004449 .0000000 .041710 .031567 .0128529 .0014739 .00155558 .00207504 .001795578 .0017795578 .0017795578 .0017795558 .00006031 .00333100 | .049352 .049188 .039261 .0397267 .0247267 .0247267 .0227367 .0227367 .0227369 .02273499 .02239992 .02373491 .046263 .00000000 .043413 .037773 .02784040 .01637977 .01199634 .01199634 .01199634 .01199634 .01199634 .01179833 .0227780 .02297226 .0000000 .038815 .0227780 .0227780 .0227780 .0227780 .0227780 .0227780 .0227780 .02295399 .00000000 .038815 .0227780 .00000000 .0038815 .0027780 .000000000 .0038815 .0027780 .000000000 .0038815 .0027780 .0000000000000000000000000000000000 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}\right)$ - Continued

βm = 1.0

| xo Ni,ol | z _o = 0 | z ₀ = 0.2 | z ₀ = 0.4 | z _o = 0.6 | z _O = 0.8 |
|--|---|---|--|---|---|
| 2.6 .00 2.6 .10 2.6 .10 2.6 .20 2.6 .20 2.7 .20 2.7 .20 2.8 .20 2.9 .20 2.9 .20 2.0 | -1.56496004648 99123-6.00559724 46984-6.23992413649914364991-1.1098399294567903929232399371663698032992469803913939139391393913939139391393913939 | .030698989950750791159899499943999439994399499339750947994661967999439943994399439943994399439943994399 | .03081838885599077-001334248484-665318855912888-665314995526655344995-000558299155615499155651544995-000667459855151188559982316840845959828459598284595982845959828459598284595982845959828459566318885998284595982845959828459598284595982845959828459598284595982845959828459598284595982845959828459598284595982845959828455546549899598284595982845959828459598284595982845959828459598284595982845959828459598284595982845959828459598284595982845959828566598485598285988885599888889998888899988888888 | .031456 .0206316 .01013874 .00137292505 .0137292505 .02365435 .022962832 .02292382 .02292382 .02292382 .02292382 .02292382 .0229231670 .02166737 .02166737 .02166737 .02166737 .02166737 .0216679 .0216679 .0216679 .0216679 .0216679 .0216679 .0216679 .0216679 .0216679 .0216679 .0216679 .03354447 .03354447 .03354447 .0335788 .00175988 .00175988 .001759788 .001759788 .001759788 .001759788 .001759788 .001759788 .001759788 .001759788 .001759788 .001759788 .001759788 .001759788 .001759788 .001759788 .003554461 .00366768 .0035526988 .0035526988 .0035526988 .003552698 .003552698 .003552698 .003552698 .003552698 .003552 | . 0323584 . 00103384 . 00103205834 . 00103205834 . 0003607655 00092765997 0009891206 0009891206 0009891206 0009891206 0009891206 0009891206 0009891206 0009891206 0009891206 0009891206 0009891206 0009891206 0009891206 0009891206 0009891206 0010821599 0010821599 0010821599 0010821599 0010821599 0010821599 0010821599 0011448175 0011448175 0011472158 0011472161038 00114 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}\right)$ - Continued

βm = 1.0

| | · · | | 1 | = I.O T | | |
|--|--|--|--|--|---|---|
| Xo | Di, ol | z _o = 0 | z _o = 0.2 | z _o = 0.4 | z _o = 0.6 | z _o = 0.8 |
| 4.00 4.00 4.00 4.00 4.00 4.00 6.00 6.00 | 05050505050505050505050505050505050505 | -1.572448 -1.7517465946 -1.751777551418 -1.1309839654 -1.13771578196883 -1.130983974 -1.130983974 -1.130983974 -1.130983979 -1.130983979 -1.10016867 -1.10016867 -1.10016867 -1.10016867 -1.11427763167 -1.1142763167 -1.1142763167 -1.1142763167 -1.1142763167 -1.1142763167 -1.1142763167 -1.1142763167 -1.1142763167 -1.1142763167 -1.1142763167 -1.1142763167 -1.1142763167 -1.1142763167 -1.1142763167 -1.1142763167 -1.1142763167 -1.1142763167 -1.114276 -1. | 019397797797797797797797797797797797797797 | .019995 004362 025555 045015 059046 063730 07783492 0775585 0775585 0775585 0775585 07559836 066801 0632217 05538984 0632217 05538984 0478781 05538984 0478781 05538984 0478781 0632217 0632010 0632217 0730110 082011 | .020122 .0011676 -0011676 -0011676 -0019114 -00262076 -003699198 -004435947 -004435947 -0044394942 -0044394942 -0044394942 -0044394942 -004651388 -00464942 -00364942 -00364942 -0046494 -0046847 -00468494 -00468494 -00468494 -00468494 -00468494 -00468494 -00468494 -00468494 -00468494 -00468494 -00468494 -00468494 -004764 -004 | . 0 2 4 3 4 3 6 8 9 9 4 4 5 4 5 4 5 1 6 6 6 7 5 7 4 4 4 7 1 6 6 6 6 7 5 7 4 4 4 7 1 6 6 6 6 7 7 5 7 6 7 6 7 6 7 6 7 6 7 6 7 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}$ ($\mathbf{ly_{i,o}l}$) - Continued $\beta_{\mathbf{m}=\mathbf{l}.2}$

| 152149 |
|--|
| 1.6 .40 136751 095073 028839 .024899 .095968 1.6 .45 112219 080863 024198 .030887 .156071 1.6 .55 073848 067152 0073810 .073409 .000000 1.6 .65 057526 024255 007002 .000000 .000000 1.6 .65 041496 024255 .047924 .000000 .000000 1.6 .70 022957 0244255 .0000000 .000000 .000000 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{Iy}_{i,o}\mathbf{I}\right)$ - Continued

βm=1.2

| | Iv. | 7 - 0 | | | - 00 | - ^^ |
|---|--|--|----------------------|---|--|---------------------|
| X ₀ | lУi,оl | z _o = 0 | z ₀ = 0.2 | z _o = 0.4 | z _o = 0.6 | z _o =0.8 |
| 1.8 8.8 11.8 8.8 8.8 8.0 9.0 9.0 9.0 9.0 9.0 9.0 9.0 9.0 9.0 9 | 05050505050505050505050505050505050505 | -1.57484961-12045-1458-3-1458-3-1-1458-3-1-1458-3-1-1-15548-3-1-1-15548-3-1-1-15548-3-1-1-15548-3-1-1-15548-3-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1- | 044824 | .0448990 -004873204667 -00127528223743099001275888670201275888670201210123002217 -0004133374389019 -0004133374389019 -0004133379488772002111033072217 -0002111033072418877200211103307217 -000204133374887720003374818772000337748877200000000000000000000000000000000 | .051633 .0239167 .011793 .00239167 .011793 .00065588 .0015814 .025763 .0005588 .0105814 .0247343 .00000000 .04444379 .0164200 .000312218 .000312218 .00055270 .00044789 .015864 .000552714 .000552714 .00055270 .00055270 .00055270 .00055270 .00055270 .00055270 .00055270 .00055270 .00055270 .00055270 .00055270 .00055270 .00072360 .00072360 .00072360 .00072360 .00072360 .00072360 .00072360 .00072360 .00072360 .00072360 .00072360 .00072360 .00072360 .00072360 .00072360 .00072360 .00072360 .00072360 .00072360 .000237454 .000837474 .000837474 | . 05 48 98 83 1 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}\right)$ - Continued

βm=1.2

| | , | <u>, </u> | , , , | 1=1.2 | · · · · · · · · · · · · · · · · · · · | |
|--|--|--|----------------------|--|---|--|
| Хo | ly _{i,ol} | z _o = 0 | z _o = 0.2 | z _o = 0.4 | z _o = 0.6 | Z _Q = 0.8 |
| 66666666666666666666666666666666666666 | 00505050505050505050505050505050505050 | -1.57644499-1.1284899-1.1296633-1.12964311-1.128533-1.12964311-1.12853-1.12964311-1.12853-1.1296633-1.12964311-1.1296633-1.1296633-1.12963 | .0362346277 | 0314349 0017438499 0017438469 0013246105 004613762 005083362 0060833649 0050864189 0050864189 0050864189 0050864189 0050864189 0050864189 0050864189 0050864189 00127292539 001272539 001272539 001272539 001272539 001272539 001272539 00127353 00127353 00127353 00127353 0012735 001 | .032617 .012169 .00321640 .00349403 .00349403 .00349403 .00349403 .0023518892 .0023518892 .002257223 .0022435007 .0022435007 .0022435007 .002243507 .002243262 .002243262 .002243262 .002243263 .0017702269934 .0017702269937 .00177702002269937 .00177702002269937 .00177702002269937 .00177702002269937 .00177702002269937 .001770200200200200000000000000000000000 | .034365 .028771 .0233348 .013248 .0133248 .0133248 .00138272 .0013846 .0028887 .001096 .0021628 .001096 .001096 .0013550 .0013550 .0013550 .0013550 .0013550 .0013550 .0013550 .0013550 .0013550 .00132121763 .00288122 .001755088 .001219122 .01219122 .01219126 .000288445 .001288415 .001288415 .001288415 .001288415 .00128228415 .001288812 .0012853 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}$ ($\mathbf{y}_{i,o}$) - Continued β m = 1.2

z_o= 0 z_o = 0.2 \mathbf{x}_{o} ly_{i,ol} $z_0 = 0.4$ $Z_0 = 0.6$ $z_0 = 0.8$.019952 -.073486 -.138832 -.170471 -.178230 -.173174 -.162514 -.150055 -.137589 -.125874 -.115169 -.105509 -.096832 -.099089 -.096874 -.0699089 -.0684741 .02 0128
-.0141703
-.0144701
-.0180699
-.0141599
-.01741556
-.0176863
-.0176770
-.01690333
-.01690333
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-.0169337 .005 .020427 .020860 1.571474 -.775513 -.510064 -.377238 -.297459 .009646 .014875 .009038 .009483 .001677 .006357 .010499 .014073 .10 4.0 .000684 . 0 .018546 4.0 . ŏ -.297459 -.244200 -.206092 -.177451 -.155118 -.1371497 -.112487 -.110178 -.099715 -.099698 -.082837 -.075912 -.064232 -.059242 -.059242 ----. 0313663 -. 035803 -. 0390503 -. 041249 -. 042555 -. 043123 -. 0443123 -. 0443123 -. 0443123 -. 0443123 -. 0443123 -. 0439167 -. 03360309 -. 03360309 -. 0346331 -. 005076 -. 014649 -. 02312067 -. 0360308 -. 0360309 -. 046630 -. 047696 -. 0446676 -. 0446376 4.0 . 30 .40 .45 .50 . 0 . 0 .019520 .0 -.0228827 -.0238837 -.024505 -.024774 -.024510 -.024553 -.02255370 -.02255370 -.02255370 -.022553 -.021601 .016402 .010325 .004414 -.011258 -.011258 -.019179 -.0226899 -.024654 -.0296161 -.029617 . 0 .65 .0 4.0 -.064741 -.059965 -.055575 -.051523 .0 .85 .90 4 . 0 4 . 0 5 . 0 1.00 -.051523 -.077959 -.142975 -.1746884 -.177539 -.164583 -.154583 -.142205 -.119971 -.110411 -.10941162 -.0942666 -1.575518
-.779625
-.514246
-.301494
-.301866
-.210534
-.152029
-.159786
-.141960
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-.115140
-.104785
-.095883
-.0861344 .05 5.0 5.0 .25 5.0 . 0 .45 .50 -.046278 -.047694 -.048376 -.048468 -.0487357 -.046347 -.045133 -.045773 -.042310 -.040779 -.039208 . 0 .50 .50 .60 .70 .70 555555 -.031056 -.075449 -.070365 .80 .85 .90 5.0 .081344 -.030882 -.030596 -.065736 -.061504 -.057619 -.069943 -.065107 -.060730 . 0 -.030142 . 0 - .039208 1.00 0 < 9 5 5 3

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}\right)$ - Continued

βm=1.4

| | | | | | | 7 00 |
|--|--|--|--|---|--|--|
| Χo |) (y _i ,o | z _o = 0 | z _o = 0.2 | z _o = 0.4 | Z _O = 0.6 | Z _O = 0.8 |
| 66666688888888888888888888888888888888 | 05050505050505050505050505050505050505 | -1.436933 -1.636903 -1.89432 -1.48522299 -1.688993 -1.68879299 -1.688993 -1.68879299 -1.1689817435 -1.29181745 -1.29181745 -1.094781034 -1.5723481002 -1.17314716 -1.05233466637 -1.17349164 -1.734694308 -1.17349164 -1.17349164 -1.18939642 -1.18939642 -1.163196433 | . 167592922 . 167592922 . 167592922 . 167592922 . 167592922 . 109459292 . 109459292 . 109459292 . 109459292 . 109459292 . 109459292 . 10926493600 . 10926493600 . 1092623550 . 109262350 . 109262350 | .644353 .00000000 .00000000 .00000000 .00000000 | .00000000 .0000000 .0000000 .0000000 .000000 | .0000000000000000000000000000000000000 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(|\mathbf{y}_{i,o}|\right)$ - Continued $oldsymbol{eta}$ m=1.4

| Хo | y _{i,} o | z ₀ = 0 | z _o = 0.2 | z _p = 0.4 | z _o = 0.6 | z _o =0.8 |
|--|--|--|--|---|---|---|
| 00000000000000000000000000000000000000 | 00505050505050505050505050505050505050 | -1.550761763956376314877563753940278480172848011490219105888720064859200485981004859810048598103584510358451035845103584510952688210952688210962882109628821096288210962882109628821012861112074086988210962882109628821096288210962882109628821096288210962882109628821096288210062882100628821006288210062882100628821 | .040574052000114708314759901475990121871107489708187910948970818791094897085860030036600300366003003660031251524531140964112749411390094730087773645115845311158453111584566811584566811584566811584566811584601158460115846011584601158460115846011584600046965115846681158466800469659700546983760054698376004696597004696597004696597004696597004696597004696597004696597 | . (43102 . C19820 - 0018243 - 0018423 - 001843359 - 00435714 - 00435714 - 0029640 - 00137714 - 00406745 - 00406711 - 0040611 - 004 | .047989 .038552 .029686 .021801 .015216 .0101377 .006675 .0044701 .009901 .015954 .0261896 .201235 .0042146 .023363 .0012351 .0093351 .0093351 .0093351 .0003351 .0012351 .0050387 .0063346 .0012351 .0050387 .006346 .0012351 .0050387 .006346 .0012351 .005087 .006346 .0012351 .00502587 .006346 .0012351 .00502587 .006346 .0012351 .00502587 .006346 .0012351 .00502587 .006346 .0012351 .00502587 .006346 .0012351 .00136735 .0000000 .00000000 .034086 .0014122 .0052436 .00173337 .01173337 .01173337 .01173337 .01173337 .01173337 .01173337 .0019917 .00099930 .020989 .020966 .0116536 .0019917 .00099930 .029077 .0000000 | . 0 5 6 7 4 1 . 0 5 2 7 9 8 . 0 4 9 2 4 8 . 0 4 9 2 4 8 . 0 4 4 2 9 3 4 . 0 4 4 3 0 9 . 0 4 4 7 0 8 . 0 4 4 7 0 8 . 0 4 8 6 0 3 . 0 5 5 8 9 5 . 0 6 9 6 4 8 . 1 0 1 0 9 0 0 . 0 0 0 0 0 0 0 . 0 0 0 0 0 0 0 . 0 0 0 0 |

TABLE II.- TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{i}\mathbf{y}_{\mathbf{i},o}\mathbf{i}\right)$ - Continued etam=1.4

| xo y | i,ol | z ₀ = 0 | z ₀ = 0.2 | Z _O = 0.4 | z _o = 0.6 | z ₀ = 0.8 |
|--|---|---|--|--|--|--|
| 3.00 4.00 | 0 0 1 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 9 0 0 0 1 1 2 2 3 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 9 0 0 0 1 1 2 2 3 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 | -1.557938865586 -223964477752898865586 -356895586 -11298883881586 -11298883785588 -11298883785588 -1129888378958 -1129888378958 -1129888378958 -1129888378958 -1129888378958 -1129888378958 -1129888378958 -1129888378958 -1129888378958 -128282375027187978 -12828275027187978 -1282827502718798 -12828275027718798 -1282828275027718798 -12828275027718798 -12828275027718798 -12828275027718798 -12828275027718798 -12828275027718798 -128282750277187988 -12828275027718798 -12828275027718798 -12828275027718798 -12828275027718798 -12828275027718798 -12828275027718798 -12828275027718798 -12828275027718798 -12828275027718798 -12828275027718798 -12828275027718798 -12828275027718798 -12828275027718798 -1282828275027718798 -12828275027718798 -12828275027718798 -12828275027718798 -12828275027718798 -12828275027718798 -12828275027718798 -12828275027718798 -1282827798 -128282798 -128282798 -128282798 -128282798 -128282798 -128282798 -128282798 -128282798 -128282798 -128282798 -128282798 -128282798 -128282798 -128282798 -1282828 -128282798 -128282798 -128282798 -128282798 -128282798 -1282828 -1282828 -1282828 -1282828 -1282828 -12828 -1282828 -12828 -12828 -12828 -12828 -12828 -12828 -12828 -12828 -12828 -12828 -12 | 0264433 75148810 026644831622913880 716709997136709971363367799997136336779999713697799881179971369877998811799713698797988112810916684979988112810916684979988112810916684979988112810916684979888291846899888271166886976869768116499988827116688697681164997681164997681164989768116499768116499768116499768116499768117777270008769788111109176811111111111111111111111111111111111 | 0274461 027461 027461 | 028734 01888 00087458 00087458 00087458 00087458 00087458 00087458 00087458 00087458 00087458 00087469 000874769 000874769 000874769 000874769 000874769 000874769 000874769 000874100 000874100 001016788 001016788 001016788 001017888 001017888 001017888 001017888 001017888 001017888 001017888 00101788888 00101788888 0010178888 0010 | .03519705 .014607 .0014607 .0014607 .0014607 .0005775 .00021976 .0003121 .0004849 .000555406 .0005555406 .0001336065556 .0001338609 .000552864 .00134662 .001346635 .01138629 .00048641 .001662849 .001346635 .001346694 .001346635 .001346694 .001355406 .001355406 .001365406 .001365406 .001365406 .001365406 .001365406 .00155406 .001662841 .001 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}$ ($\mathbf{i}\mathbf{y}_{i,o}\mathbf{l}$) - Continued $\boldsymbol{\beta}\mathbf{m}=\mathbf{l.4}$

| Хo | Vi,ol | z _o = 0 | z _o = 0.2 | z _o = 0 4 | z _o = 0.6 | Z _O = 0.8 |
|--|--|--|--|--|---|--|
| •••••••••••••••••••••••••••••••••••••• | 00 00 01 00 01 01 01 01 01 01 | -1.579541 3714118 3714118 3813572 2483345 1159373 1146827 1146828 1145675 087331 087331 008034342 008035 | .015997 0742869 174535 182323 166670 154288 154288 154288 1199866 1199866 101237 0935497 0946032 064753 064753 066487 | . 016115 - 0030367 - 043794 - 06:794 - 073349 - 081071 - 076511 - 079511 - 079 | .016371 -005563 -004796 -014320 -022722 -02283612 -045627 -045627 -047631 -047 | . 010726 . 000732 . 0004857 0007332 0010650 0014833 021503 0224002 0028553 00296076 0029507 0029132 0028584 0027088 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}$ ($\mathbf{Iy}_{i,0}\mathbf{I}$) - Continued $\beta \mathbf{m} = \mathbf{I.6}$

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(|\mathbf{y}_{i,o}|\right)$ - Continued $\beta m = 1.6$

| Хo | Yi, o | z ₀ = 0 | z _o = 0.2 | z _o =(:4 | z _o = 0.6 | z _o = 0.8 |
|--|--|--|--|--|---|--|
| 2.000000000000000000000000000000000000 | 00505050505050505050505050505050505050 | -1.553394 7553394 27533948 276295 17629690 037556 1458468 12139672 037556 037556 037556 03756515 037576139 2276556 1528236 1528236 1528236 1288515 0977166 156375995 2289486 1564448 16977936 16977936 16977936 16977936 17697595 188554 19637505 1964448 19637505 19677133 1164418 06777607 0574608 196389681 0977166 11677697 117789 1188534 19637505 19637671 05774608 196389681 097710657 05774608 196389681 09772459 1167133 | 164035 152861 139861 126821 114494 103134 092770 083329 074705 066777 059428 052541 046001 033680 033423 | .044792 .0214339 .0015339 .0015339 .0027321 .00384603 .0027321 .00386229 .0036668 .0015184 .1228332 .00398622 .0016392 | .052763 .044108 .0361240 .029778 .02923778 .02923778 .02923778 .02923778 .02923778 .02923778 .029237168 .00000000 .0045478 .0237168 .000000000 .0045478 .0237168 .0013456 .0013456 .0013456 .00137689 .00137689 .00137689 .00137689 .00137689 .00137689 .00137689 .00137689 .00166000 | .06907 .0667742 .0667742 .0665713 .0684631 .0785123 .00684631 .0785123 .0000000 .00000000 .00000000 .00562473 .0045626 .0049673207 .004504742 .004504742 .00476473 .00476473 .004504742 .004504742 .004504742 .004504742 .004504742 .004504742 .004504742 .004504742 .004504742 .004504742 .004504742 .004504742 .004504742 .00504742 .0016473 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{i}\mathbf{y}_{i,0}\mathbf{i}\right)$ - Continued $\mathbf{\beta}\mathbf{m}$ = 1.6

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}\right)$ - Continued

βm = 1.8

| xo lyi,ol | z ₀ = 0 | Z _O = 0.2 | z ₀ = 0.4 | z ₀ = 0.6 | z _o = 0.8 |
|--|--|--|--|---|---|
| .6 .00 .00 .00 .00 .00 .00 .00 .00 .00 . | -1.439255618683318310115623 -1.4812889832898732125823 -1.5057727427528428426061188520363378 -1.505784285342119808812036294221918151088114057812 -1.531224062948324062948325364491533644943253644943253644943253644943253644943253644943253644943253644943253644943253644943253644943253644943253644943253644943253644432536444 | .220722 .182827 .0000000 .1294116 .0122467 .00124677 .0012467 .00124677 .0093691 .0093691 .0093691 .0093691 .0093691 .0093691 .0093691 .0093691 .0093691 .0093691 .0093691 .0093691 .0093691 .0093691 .0093691 .00627982 .00627982 .007268903 | .00f000 .000000 .000000 .000000 .000000 .000000 | .0000000 .0000000 .0000000 .0000000 .000000 | . 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}\right)$ - Continued $oldsymbol{eta}\mathbf{m}\mathbf{=}\mathbf{I.8}$

| Хo | ly _{i,ol} | z _o = 0 | z _o = 0.2 | Z _O = 0.4 | z _o = 0.6 | Z _O = 0.8 |
|--|--|--|---|--|--|---|
| 00000000000000000000000000000000000000 | 05050505050505050505050505050505050505 | -1.555873 -3.569373640 -2.26937922 -1.73213630 -2.173213630 -1.17421364933 -0.0541218 -0.0541218 -0.0541218 -0.0541218 -1.14443545600 -1.57560888030 -1.27997682 -1.1494693 -1.27997682 -1.1494693 -1.12997682 -1.1494693 -1.12997682 -1.1494693 -1.12964653 -2.21997682 -1.1494693 -1.156316760 -1.1688867 -1.1688867 -1.1688867 -1.1688867 -1.1688867 -1.1688867 -1.176618279 -1.1888667 -1.1888667 -1.1888667 -1.1888667 -1.1888667 -1.1888667 -1.1888667 -1.1888667 -1.1888667 -1.1888667 -1.1888667 -1.1888667 -1.1888667 -1.1888667 -1.188867 -1.1888667 -1.1888667 -1.188867 -1. | .04137605046141143916114391611439161143916114391611439161143916114391611439161143916114391611437880983726098372609837260983956309839563098395630983956309839563112070701097941209664702112070701097940811207070109836411805261180661180661180661180661180661180661180661180661180661180661180661180661180661806618066180661806618066 | .046846 .02467227 -00412376 -0012376 -00231590 -00231590 -00231590 -00231590 -003305000 -0019594 -00335500 -0019594 -00335500 -0019594 -0018426 -0018426 -0018426 -0018426 -0018426 -00334135747 -004135747 -004135747 -004135747 -004135747 -004135747 -004135747 -004135747 -004135747 -004135747 -004135747 -004135747 -004135747 -004135747 -004135747 -004135747 -004135747 -005542780 -005542780 -005542780 -005542780 -005542780 -005611656 -005614316 -005614316 -005614316 -005614316 -005614316 -005614316 -0056143175 -005614316 -005611656 -005614316 -005 | .059211 .051723 .045061 .0367132 .039714 .036732 .0347911 .0404040 .049567 .110207 .0000000 .0000000 .00000000 .0049819 .0413307 .026778 .0215031 .016266 .019399 .0244991 .0346443 .100108 .00162664 .019398 .0217938 .100108 .00000000 .00000000 .00000000 .00000000 | .089362 .0993495 .09934738 .1097719 .1231993 .2238600 .0000000 .0000000 .0000000 .0000000 .000000 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(|\mathbf{y}_{i,0}|\right)$ - Continued $\boldsymbol{\beta}\mathbf{m}=1.8$

| xo yi,o | ,ol z ₀ = 0 | z ₀ = 0.2 | z _o = 0.4 | z _o = 0.6 | z _o = 0.8 |
|--|------------------------|--|--|--|--|
| 3.5 3.5 3.5 3.5 3.5 3.5 3.5 3.5 | 0.5 | 02703048 -01703018 -01703018 -1167361444 -1167361444 -1167361444 -115774788 -11441775 -1143187042 -10774788 -0077881732 -00778821732 -00778821732 -00778821732 -00778821732 -117188722 -1188722 -1198722 -1198722 -1198722 -1199722 -1199722 -118872758 -1188722 -1188722 -1188722 -1199722 -1188722 -1188722 -1199722 -1199722 -1188722 -1188722 -1199722 -1188722 -1188722 -1199722 -1199722 -1188722 -1188722 -1188722 -1188723 -1188722 -118872 -1188722 -1188722 -118 | 02334 .CC00679 .CC00679 .CC0393163 .CC053188 .CC067689 .CC067689 .CC0670151 .CC067 | .025529 .01538828 .011788281 .0011788281 .00211788281 .002298478 .002298478 .003118871 .002298478 .003114085 .003144457 .002444167 .001844520 .001128382 .00128382 .001128382 .001128382 .0011283 | .0227649 .0176757 .00176752 .00176752 .00040990 00178318 0006017192 000516828 0006017192 000516828 0001617192 000516828 0001617192 0001617192 0017131688 0017131688 0017131688 0017131698 001711702 001711702 00171702 0027 |

.

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}\right)$ - Continued

 β m = 2.0

| Хo | ј Уі, о ј | z ₀ =0 | z ₀ = 0.2 | z _o = 0.4 | z _o =0.6 | z _o = 0.8 |
|---|--|--|--|--|---|---|
| .6666888888000000002222222224444444444444 | 05050505050505050505050505050505050505 | -1.434603607783296568 -1.4787556382388222426709116738224267091266401.50982694219191.77566401.519456230913674219191.44482691.4482691.4482691.44828591.452186840913689133036391323546800913689369 -1.5389378323546800913689369 -1.5389378323546800913841734842691.27166334842691.27166334842691.27166334842691.2802398307378924944471.4716431.2109884471.2109884471.2109884471.210988360737891.37889 | . 268448 . 4444852 . 00403668 . 0444852 . 00403668 . 00435567 . 00986689 . 0069157 . 00986689 . 003254776 . 003254776 . 0073254776 . 0073355 . 00817825 . 008178382 . 008373449 . 00851725 . 00851725 . 00851725 . 0085173868 . 00853131759 . 011173835 . 004786868 . 00538680 . 0053860 . 0053860 . 0053860 . 0053860 . 0053860 . 00 | .00000000 .00000000 .00000000 .00000000 | .0000000 .0000000 .0000000 .0000000 .000000 | .0000000 .0000000 .0000000 .0000000 .000000 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}\right)$ - Continued

| | | 7- | 70.11 | 1 = 2.0 | | |
|--|--|--|--|---|---|--|
| Хo | ly _{i, ol} | z _o = 0 | z _o = 0.2 | z _o =0.4 | z _o = 0.6 | z _o = 0.8 |
| 22222222222222222222222222222222222222 | 00505050505050505050505050505050505050 | -1.5536950 7561023 7561023 354408 2277364 1769782 145839 0998803 0998803 0646927 05627148 22869813 04962148 22869813 1562803 0562803 0562803 0562803 0562803 0562803 0562803 0562803 0562803 0562803 0562803 0562803 0562803 0562803 0562803 0562803 0562803 0562803 066280 | .037783 0176993 117747475 11474775 11474775 11474775 11474775 11474775 11474775 11474775 11474775 11474775 11826621 0187285120 0187285120 0187285120 0187285 01873449 01873449 118775 118775 118775 118775 1187757 118775 118775 118775 118775 118775 118775 118777776 11877777777777777777777777777777777777 | .043105 .02)931 -014851 -014851 -025120 -033257 -033274 -0033274 -0034676 -0019778 .107703 .034676 -0019778 .107703 .034626 -0019778 .107703 .034626 -0019778 .107703 .034626 -0019778 .107703 .034626 -0019778 .107703 .034626 -0019778 .107703 .034626 -0019779 -0051267 -0051267 -0051267 -0061268 -00612 | .055553 .04H182 .0416343 .032787 .0312364 .0356453 .059715 .26000000 .00000000 .00400611 .023749 .0163331 .0163331 .0163331 .000277357 .00027757 .00027757 .00027757757 .00027757 .00027757 .00027757757 .00027757757757 .000277577577577577757757775777777777777 | . UB 7354 . 08 2352 . 09 27 87 70 08 . 12 21 05 22 . 09 27 87 70 08 . 12 21 05 22 . 09 27 87 70 00 . 10 20 00 00 . 00 00 00 . 00 00 00 . |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}$ ($\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}$) - Continued $\beta\mathbf{m}$ = 2.0

| xo þ | ,ન | z _o = 0 | z _o = 0.2 | z _o = 0.4 | Z _O = 0.6 | z _o = 0.8 |
|--|--|--|--|--|--|---|
| 3.5 3.5 3.5 3.5 3.5 3.5 3.5 3.5 | 105 105 105 105 105 105 105 105 105 105 | 577400 577400 577400 577400 577400 57752052119 14761531677405 57952052119 14761531677405 5795206119 11100076816176761 1110007681617676 11100076816176 11100076816176 11100076816176 11100076816 111000076816 111000076816 111000076816 11100000076816 111000000000000000000000000000000000 | .023113 0634669 16669 116569 11656994 11656994 116605416 116605416 00867328469 11060618472 00867328469 0076918472 00867328469 00867328469 00867328469 00867328469 00867328469 00867328469 008684878 0086884878 0086884878 0086884878 00868848 0086888 00879284 1160949 1160949 11761868 1186382 0086884877 11761868 1186382 1186382 1186382 1186382 1186382 1186382 1186382 11998883 1199883 11998883 11998883 11998883 11998883 11998883 1199883 1199883 11998883 11998883 11998883 11998883 11998883 11998883 11998883 11998883 11998883 11998883 11998883 119 | .024307 .0003889 -03871288 -00610975 -00684226 -0068370987 -0068370987 -0068370987 -0068370987 -0068370987 -0068370987 -0068370987 -0068370987 -0068370987 -0068370987 -005559567 -005559567 -005559567 -0055597 -00203097 -00203097 -00203097 -00203097 -00203097 -00203097 -00565594 -00566597 -005666424 -005666424 -005998664 -0068887 -0068887 -007033097 -007033097 -007033097 -007033097 -007033097 -007033097 -007033097 -007033097 -007033097 -007033098 -005066424 -005066424 -0050664 -0070306 -0070306 -0070306 -0070306 -0070306 -0 | .026544 .016438 .00664384 .000619348 .000619538 .00157991 .00246187 .00277724 .00275724 .00275582 .002756578 .002854966 .0027566578 .001389161 .00148899 .012260577 .00246849 .012260577 .00335465 .0012114 .01418090 .0012118185 .00138444 .0024681941 .00346849 .003354666 .00347666 .00347666 .00347666 .00347666 .00347666 .00347666 .00347666 .00347666 .00347666 .00347666 .00347666 .00347666 .00347666 .00347666 .00347666 .00347666 .00347666 | .030315 .022322 .011653 .002057660 .0011653 .0008169 .0002934 .0000841673 .0000841673 .0000841673 .001681744 .0000841673 .001259518 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}$ ($\mathbf{i}\mathbf{y}_{i,o}\mathbf{i}$) - Continued $\beta \mathbf{m} = 2.5$

| Хo | Yi,0 | z ₀ =0 | z _o = 0.2 | z ₀ = 0.4 | z _o = 0.6 | z _o = 0.8 |
|---|--|--|--|--|--|---|
| .66.66.88.88.00000000000000000000000000 | 00505050505050505050505050505050505050 | -1.4207421 -1.47123826082-1.12488481 -1.4712388068122-1.1635826081-1.1035880-1.1035880-1.1035880-1.1035880-1.103880-1.10 | .575844 1.161551 .0000000 .1859181 .60000000 .185918100 .01479100 .0147757 .1265001 .00304039 .0147757 .020854031 .005544796 .005544796 .005544796 .005544796 .005544796 .006168460 .006168868 .008570236 .008570236 .008570236 .00854796 .00808608 .00815886 .00815886 .00815886 .00815886 .00815866 .00815866 .00815866 .00815866 .00815866 .00815866 .00815866 .00815866 .0081586 .00815 | .0000000000000000000000000000000000000 | .000000 .000000 .000000 .000000 .000000 .000000 | . 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathsf{I}\mathbf{y}_{i,o}\mathsf{I}\right)$ - Continued

 β m = 2.5

| | T | <u> </u> | | T | |
|---|--|---|--|--|---|
| ×о ly _i ,o | Z n= 0 | z _o = 0.2 | Z _O = 0.4 | Z ₀ = 0.6 | Z ₀ =0.8 |
| 2.22.22.22.22.22.22.22.22.22.22.22.22.2 | -1.55223044552-1.1357352449-1.137352415-1.137352415-1.137352415-1.137352415-1.137352415-1.137352415-1.137352415-1.137352415-1.137352415-1.137352415-1.137352415-1.137352415-1.137352415-1.137352415-1.137352415-1.137352415-1.137352415-1.137352415-1.1349615-1.1349615-1.1344869-1.134489-1.1344869-1.1 | .038828 01426742 14267925 114269926 114269928 114269928 114269928 114269928 114269928 114269928 114269928 114269928 114269928 114269928 114279 114279 115704499 11570498 115704 | .049137 .029319 .00119978 .00119978 .00119978 .00113133318 .000000000000000000000000000000000000 | .081220 .0804188 .0994230 .0804188 .0925006 .1037923 .2080200 .0000000 .0000000 .0000000 .0000000 .0052548 .03329933 .0340351996 .03329975 .03226733 .0340351996 .07099795 .0000000 .0000000 .0000000 .0000000 .000000 | 283945 3568281 1.262099 .00000000 .00000000 .00000000 .00000000 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(|\mathbf{y}_{i,0}|\right)$ - Continued $\beta m = 2.5$

| Хo | Ni,ol | z _o = 0 | z _o = 0.2 | z ₀ = 0.4 | z _o = 0.6 | z _o = 0.8 |
|--|---|--|--|--|--|---|
| 5.00 5.00 5.00 5.00 5.00 5.00 5.00 5.00 | .00505050505050505050505050505050505050 | -1.570848477084947708494374207224024202012420114805511300761141700896620079041500624223004713800470074057889662047007405788966204707415778866712247021122470211224702112247021098933040089933750089933750089933750049699 | .020318072488213781449137814491168214715821471188910711444789117300700809479008780792006241668004711540034724860047125811891883118918831189188311891888311981883 | .021685 001876 02376 02376 0439967 061856 061856 061856 061836 061836 061836 051812 046569 0318269 0318269 0118608 0018608 - | .024335 .014430 .014447 .00534447 .0016786 .00216786 .00271480 .0026555 .00271480 .0026556 .0027149 .0026151 .00261549 .00169378 .0046930 .0046930 .0046930 .0018049 .0018049 .0018049 .0018049 .0019769 .0019769 .00399991 .003999917 .003999917 .003999917 .003999917 .003999917 .003999917 .003999917 .003999917 .003999917 .003999917 .003999917 .003999917 .00399917 .00399917 .00399917 .0039918 .0039988 .003888 .003888 .003888 .003888 .00388 .00388 .00388 .00388 .00388 .00388 .00388 .00388 .003 | .0293446 .0194846 .011977 .002870 .0046776 .0036476 .0036476 .0036476 .0036476 .0036476 .004007 .004007 .0051633 .007101633 .007101633 .00470010 .001000000 .0020061 .0014505 .0047827 .001478287 .001478787 .0014787 .0014787 .0014787 .0014787 .0014787 .0014787 .00147878787 .0014787 .0014787 .0014787 .0014787 .0014787 .0014787 .001 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}$ ($\mathbf{Iy}_{i,o}\mathbf{I}$) - Continued β m=3.0

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}\right)$ - Continued $\beta \mathbf{m} = 3.0$

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{W}}\left(\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}\right)$ - Continued β m = 3.0

| Хo | y _{i,} o | z ₀ =0 | z _o = 0.2 | z _o = 0.4 | z _o = 0.6 | z _o = 0.8 |
|--|--------------------|---|--|--|--|--|
| 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 | y _i , o | Zo=0 -1.574910778394651238137886012447292059871766677113504711959921065500008531500685710613055006456370642108 | Zo=0.2 .01623907663414140317245117392616262214943944123911112456102009092582807583760617700055273049251037443 | Z ₀ = 0.4 . 017279 006379 027357 045583 0588859 067770 073091 074050 070216 070216 066613 062540 0536388 0489847 0536388 048988 048988 048988 048988 | Zo=0.6 .019280 .0092870092833008888016391022569037082903412830342639034263903426790246790212070172580007069007069 | Zo= 0.8 . 0 2 28 15 . 0 17895 . 0 13163 . 0 08759 . 0 0 13866 - 0 0 13876 - 0 0 0 5051 - 0 0 0 5051 - 0 0 0 5050 - 0 0 0 2491 . 0 0 0 0 63 . 0 0 0 7791 . 0 1 3 5 86 . 0 2 1 5 87 . 0 3 5 8 2 1 . 0 5 9 3 5 6 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $\ \ F_{w} \ (Iy_{i,o}I)$ - Continued

 β m = 3.5

| Χo | Ŋi,ol | z ₀ =0 | z ₀ = 0.2 | z _o = 0.4 | z _o = 0.6 | z ₀ = 0.8 |
|---|--|---|---|--|--|---|
| .6668888000000222222444444446666666666666 | 05005050505050505050505050505050505050 | -1.383100473581 -1.473581 -1.473581 -1.450301662544149265946143154101 -1.6594643154101 -1.507155112367937 -1.521667937 -1.521667937 -1.521667937 -1.521667937 -1.521667937 -1.521667937 -1.521667937 -1.521667937 -1.521687937 -1.521687937 -1.531667937 -1.531668333322686965 -1.574586965 -1.574586965 -1.574736867 -1.774785331226877937478537252979477853112477362217757663127478537252979351301617757663217757663217757663217757663211693272 | .0000000 .0000000 .0000000 .0000000 .000000 | .000000 .000000 .000000 .000000 .000000 .000000 | .0000000 .000000 .000000 .000000 .000000 | . 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{w}(Iy_{i,o}I)$ - Continued

 β m = 3.5

| xo ly _{i,o} | z _o = 0 | z _o = 0.2 | z _o = 0.4 | z _o = 0.6 | z _o = 0.8 |
|---|--|---|--|--|---|
| 33.00 .005 33.00 .105 33.00 .105 33.00 .255 33.00 .255 35.00 | - 1.5626690 - 1.7626690 - 1.7828140 - 1.17828140 - 1.17828140 - 1.17828140 - 1.19437163 - 0.075130 - 1.19437163 - 0.0244084163 - 0.0761666604 - 1.288852156666631 - 1.288852156666631 - 1.153198088232 - 1.153198088232 - 1.153198088232 - 1.2035666331 - 0.024488353 - 1.17927885248660 - 1.17927885248660 - 1.17927885248660 - 1.17927885248660 - 1.17927885248660 - 1.179278852886666331 - 0.0244886266631 - 0.0388232 - 1.17936666331 - 1.17936666331 - 1.17936666331 - 1.17936666331 - 1.179378248 - 1.179378248 - 1.179378248 - 1.179378248 - 1.1793778248 - 1.179378248 - 1.1793778248 - 1.179378248 - 1.1793778248 - 1.179378248 - 1.17937 | 028715 -061778 -10240423 -11240423 -11240423 -11240423 -11240423 -11240711 -11371280 -08828139 -0042833 -0042833817 -01386707 -113984673 -11579943667 -11493707 -11493707 -11493707 -11493707 -008407322334 -002711701 -11614419496 -1177129 -116449496 -1177129 -116449496 -1177129 -116449496 -1177129 -11782980 -007677221 -00836889 -00760707 -00836889 -00760707 -11782980478 | 037490 .017714 .0127770 .0127770 .0207974 .022593 .0165503 .0165503 .0165503 .0165503 .016579 .0297560 .0297560 .0297560 .0297560 .0297560 .0297560 .0297560 .0297560 .0297560 .037641 .0446191 .037645 .037641 .0446191 .039143 .03000000 .0297560 .016669 .037641 .0446191 .039143 .0016657 .00166669 .00166669 .0016677 .0016677 .0016677 .001677 .001677 .001677 .001677 .001677 .001677 .001677 .001677 .001677 .001677 .001677 .001677 .001677 .001677 .001677 .001 | .067534 .067542 .0693571 .082695 .09736374 .1722387 .0000000 .00000000 .00000000 .00000000 | 369429 498012 7678668 0000000 00000000 00000000 00000000 0000 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}\right)$ - Continued β m=4.0

| ×o ly _{i,0} | z _o = 0 | z _o = 0.2 | z _o = 0.4 | z ₀ = 0.6 | z _o = 0.8 |
|---------------------------------------|---|---|--|--|---|
| .6 .0 .0 .0 .0 .0 .0 .0 | -1.359044397887 -1.438048571422165786 -1.4780866641574319413 -1.5679522380948198944 -1.51777370308541554201129118 -1.5289253190244376891297118 -1.52892514902428571118042828571118042820942513262942094251326294209425132629420942513262942094251326294209425132629420942513262942094251326294209425132629420942513262942094251326294 | .0000000 .0000000 .0000000 .0000000 .000000 | .0000000000000000000000000000000000000 | .000000 .000000 .000000 .000000 .000000 .000000 | . U O O O O O O O O O O O O O O O O O O |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}$ (Iy, oI) - Continued

 β m = 4.0

| ×o y _i | i,ol | z ₀ = 0 | z _o = 0.2 | Z ₀ = 0.4 | z ₀ = 0.6 | z ₀ = 0.8 |
|---|---|---|---|---|--|---|
| 33.00 4.00 4.00 4.00 4.00 4.00 4.00 4.00 4.00 5.00 | 00011222333445550001112233344455566600011223334455505050505050505050505050505050505 | 1.561896 49268951 2761896 35588891 27718089 1705203 1355904 1079577 0520101 1.56676769 36612344 18399604 1282483207 1282483207 1282483207 1282483207 1282483207 1282483207 1282483207 12828321002 282183207 11839322 11839321602 2821602 2821602 2821602 28321602 28321602 28321602 28321602 28321602 28321602 11462847 11462847 11462847 11462847 11462847 11462847 11462847 11462847 1146307 283216002 283216002 283216002 1147795 12819332 0985396 2941999 2941999 00544556 00346699 | .0294880 02998951 02998951 124809045 1140948487 1140948487 1140434447 00315114988 00315114988 0024605214 0031511655164 1161631764 1161631764 1161631764 1161631764 1161631764 1161631764 1161631764 1161631764 1161631764 1161631764 1161631764 1161631764 1161631766 116166 116166 116166 116166 116166 1 | .042769 .0113328 .0015387 .0015387 .000863 .0015387 .00084183 .052254 .1200000 .00317995 .011705 .00187976 .00187976 .00187705 .00187705 .00187705 .0018740 | . 126987 .126987 .126987 .18387329 1.149387329 1.000000000 .000000000 .000000000 .000000 | .0000000 .0000000 .0000000 .0000000 .000000 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}$ ($\mathbf{i}\mathbf{y}_{i,o}\mathbf{i}$) - Continued $\beta \mathbf{m} = 4.5$

| Хo | lyi, ol | z ₀ =0 | z ₀ = 0.2 | Z _O = 0.4 | z _o = 0.6 | z ₀ = 0.8 |
|---|--|--|---|--|--|---|
| 666888000002 222244444446666688888880000000000002222224666666668888880000000000 | 05005050505050505050505050505050505050 | -1.331255 -289058 -1.4233518 -1.42333518 -1.4689245 -2.74065 -1.4957529 -1.66555782 -1.44529 -1.51322516 -2.25483 -1.569386781 -2.25483 -1.525579 -1.51322583 -1.71255079 -1.148460 -1.5247562 -1.4255079 -1.148460 -1.53447562 -1.2924720 -1.188553 -1.7734897 -247568123 -1.57346897 -2475681 -272427562 -1.4566897 -1.4566897 -1.4566897 -1.4566897 -1.4566897 -1.4566897 -1.4566897 -1.4566897 -1.4566702 -1.57469788 -1.213703420 -1.5546897 -1.213703420 -1.5546897 -1.4566702 -1.46769 -1.546762 -1.4967788 -1.218999 -1.55468789 -1.218999 -1.55468789 -1.218999 -1.5546702 -1.405788 -1.218999 -1.5546702 -1.405788 -1.218999 -1.5546702 -1.405788 -1.218999 -1.55404784 -1.2189998 -1.405788 -1.21895137 -1.2 | .000000 .000000 .0000000 .0000000 .000000 | .000000 .000000 .000000 .000000 .000000 .000000 | .000000 .000000 .000000 .000000 .000000 .000000 | . 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}\right)$ - Continued

 β m = 4.5

| | βm = 4.5 | | | | | | | |
|--|--|---|--|---|---|--|--|--|
| Хo | ly _i ,οl | z _o = 0 | z ₀ = 0.2 | zo=0.4 | z ₀ = 0.6 | z _o = 0.8 | | |
| 3.000000000000000000000000000000000000 | 05050505050505050505050505050505050505 | -1.74896551 4896551 2061517 12978 12061517 12978 12061517 12978 12061517 12978 12061517 12978 1216273738 121627373738 1216273737373737373737373737373737373737373 | .0307571 114236110024 114236110024 114236110024 114236110024 114236110024 003377806 0033777806 0033777806 00666666666666666666666666666666666 | 0 4 0 8 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 | 264584 363853 .527870 .00000000 .000000000 .000000000 .000000 | . 00 00 00 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | | |

TABLE II. - TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{i,o}\mathbf{I}\right)$ - Continued

βm= 5.3

| Хo | lyi, ol | z _o = 0 | z _o = 0.2 | Z _O =0.4 | z _o = 0.6 | Z _O = 0.8 |
|--|--|--|---|--|---|---|
| 1.00 1.00 1.00 1.22 1.44 1.44 1.44 1.66 1.66 1.66 1.66 1.66 | 05050050050505050505050505050505050505 | -1.299495 -1.406744487311 -1.458679595503212207 -1.4887586497487 -1.5081646497487 -1.50816468209337894018852015314655101487511014821531469018832343316552763656172934924106103154977522194924106103154979521949241062008 -1.549795219496103538800216547140610815798282177882821654714061092598999198862263146826177882123670070736 | .0000000 .0000000 .0000000 .0000000 .000000 | .(00000 .(0000000 .(000000 .(000000 .(000000 .(000000 .(000000 .(000000 .(0000000 .(000000 .(000000 .(000000 .(000000 .(000000 .(000000 .(0000000 .(000000 .(000000 .(000000 .(000000 .(000000 .(000000 .(0000000 .(000000 .(000000 .(000000 .(000000 .(000000 .(000000 .(0000000 .(000000 .(000000 .(000000 .(000000 .(000000 .(000000 .(00000000 | . 000000 | . U 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 |

TABLE II.- TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{w}}\left(\mathbf{I}\mathbf{y}_{i_{\mathbf{q}}\mathbf{O}}\mathbf{I}\right)$ - Continued

 β m = 5.0

| | | <u></u> | = 5,0 | T | |
|--|---|--|---|---|---|
| Xo Ni,o | z _o = 0 | z _o = 0.2 | Zo=0.4 | Zo = 0.6 | Zo= 0.8 |
| 3.5 3.5 3.5 3.5 3.5 3.5 3.5 3.5 | -1.56434127-142441-13575337444-13774443388-15-16-16-16-16-16-16-16-16-16-16-16-16-16- | 4897844189313288993067899024499319886 5281945102479230688975284600144098298296144086 1.12457923088517551224960144098298296144086 1.124542199423518997122493108977288486050645728821 1.12111086425165321086425165327227277768829 1.1211086410811675329963329 1.121108641165327227277768829 1.121108641167758677288999339 | 6 1 4 4 4 1 5 7 6 6 2 8 4 4 1 5 7 6 6 1 8 4 1 4 1 5 6 2 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 | 83749000000000000000000000000000000000000 | . 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 |

TABLE II.- TABULATION OF THE DOWNWASH FUNCTION $F_{\mathbf{v}}(|\mathbf{y_{1,o}}|)$ - Continued

1 = 00

| | | r | m = 0 | · · · · · · · · · · · · · · · · · · · | | · |
|--|---|---|---|---|---|---|
| X | y ₁ ,0 | z _O = 0 | z _o = 0.2 | z _o = 0.4 | z _o = 0.6 | z _o = 0.8 |
| 0.6 | 0 .05 .10 .15 .20 .25 .30 .35 .40 .45 .50 | -1.586014 784636 513673 375132 289363 229721 184673 148284 116968 087976 057824 | 0 086449 144711 169058 169186 155985 156414 113895 089525 062600 029170 .040753 | 0 006198 009655 008150 0 .016276 .043159 .087652 .179049 | 0 | 0 |
| .88888888888888888888888888888888888888 | 0 .05 .10 .15 .20 .25 .30 .35 .40 .45 .50 .55 .60 .65 | -1.588488789536521108385253502568245901204450172290146210105069087726077370055036036922 | 0090030151948180112184322175610161146144689127965111645095838080439064975048667026623 .001705 | 001875)03527304794705598505988105861505427704689103672402360 300655 L .01767 L .06326 5 0 | 0 .004904 .010643 .018010 .027846 .041107 .059116 .084155 .121171 .184578 .355072 0 0 | 0 |
| 1.0 1.0 1.0 1.0 1.0 1.0 1.0 1.0 1.0 1.0 | 0 .05 .10 .15 .20 .25 .30 .35 .40 .45 .55 .60 .55 .70 .75 .80 .85 | -1.589540 -791785 -524515 -389849 -310335 -253040 -212980 -182335 -157922 -137832 -120837 -106103 -095036 -081204 -070181 -059683 -049318 -038541 -026156 | 0091440154785184408190129185000170221155587140870126809113641101370089892079054068669058510048271037448024928006098 | 002158)04098 :05662 ;06778 /07454 ;07724)07724 ;07330646705800 ;05048 ;04212 ;032760847013106597 ; 0 | 0005961011431015985019263021057021237019747016566011655004896 .003998 .015665 .031559 .055522 .102582 0 | 0 .008128 .016670 .026060 .036778 .049397 .064685 .083801 .108742 .143545 .198448 .313352 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 |
| 1.2 1.2 1.2 1.2 1.2 1.2 1.2 1.2 1.2 1.2 | 0 .05 .10 .20 .25 .35 .40 .45 .50 .55 .66 .70 .75 .85 .99 .10 | -1.590155793005526356392322311326256835521747818756616393411486112859411486102911092336082827074142066085058484051177043988 | 0092149156207186573193014186647174658160851147009133884121728110567100527009899082161073992066275058891051713044594037332 | 00226904322060010723510845208569084590779907335068200569405097104476:03825103130025613014585 | 000843001640302551902547903410303732303916403971003907703738903475603126102694702180401573908531 .000290 .012492 .028821 | 0001638003099004214004833004823004075002496 0 .003505 .008138 .014073 .021594 .03139 .04188 .089525 .150465 0 |

TABLE II.- TABULATION OF THE DOWNWASH FUNCTION $F_{w}(|y_{i,o}|)$ - Continued

n = ∞

| x | Y _{i,0} | z _o = 0 | z _o = 0.2 | z ₀ = 0.4 | z _o = 0.6 | z _o = 0.8 |
|-----|------------------|--------------------|-------------------------|----------------------|----------------------|----------------------|
| 1.4 | 0 | | 0 | 0 | 0 | 0 |
| 1.4 | .05 | -1.590540 | 092557 | 023260 | 009403 | 003877 |
| | | | 157026 | 044357 | 018357 | 007601 |
| 1.4 | .10 | 793741 | | 061718 | 026469 | 011030 |
| 1.4 | .15 | 527462 | 187787 | | 033449 | 014042 |
| 1.4 | .20 | 393807 | 194669 | 074646 | | 016534 |
| 1.4 | .25 | - 313194 | 188731 | 083227 | 039126 | |
| 1.4 | .30 | 259097 | 177183 | 088036 | 043443 | 018452 |
| 1.4 | •35 | 220144 | 163830 | 089845 | 046436 | 019737 |
| 1.4 | .40 | 190651 | 150459 | 089412 | 048206 | 020375 |
| 1.4 | .45 | 167455 | 137827 | 087385 | 048888 | 020363 |
| 1.4 | •50 | 148659 | 126188 | 084272 | 048630 | 019711 |
| 1.4 | •55 | -,133053 | 115576 | 080446 | 047577 | 018432 |
| 1.4 | .60 | 119831 | 105923 | 076177 | 045855 | 016539 |
| 1.4 | •65 | 108432 | 097128 | 071645 | 043575 | 014034 |
| 1.4 | .70 | 098452 | 089081 | 066972 | 040820 | 010904 |
| 1.4 | •75 | -,089594 | 081677 | 062232 | 037654 | 007107 |
| 1.4 | .80 | 081632 | 074819 | 057467 | 034112 | 002559 |
| 1.4 | .85 | 074390 | 068419 | 052692 | 030205 | .002895 |
| 1.4 | .90 | 067760 | 062397 | 047905 | 025913 | .009536 |
| 1.4 | •95 | 061529 | 056677 | 043081 | 021173 | .017900 |
| | | 055693 | 051188 | 038179 | 015863 | .029112 |
| 1.4 | 1.00 | 077097 | 071100 | 0,0017 | 01/00/ | |
| 1 4 | 0 | | 0 | 0 | 0 | 0 |
| 1.6 | | -1.590769 | 092815 | 023588 | 009895 | 004761 |
| 1.6 | .05 | | | 045015 | 019343 | 009375 |
| 1.6 | .10 | 794219 | 157543 | | 027954 | 013707 |
| 1.6 | .15 | 528180 | 188565 | 062709 | 035441 | 017639 |
| 1.6 | .20 | 394767 | 195710 | 075974 | | 021082 |
| 1.6 | .25 | 314400 | 190040 | 084897 | 041635 | |
| 1.6 | .30 | 260554 | 178765 | 090056 | 046483 | 023973 |
| 1.6 | • 35 | 221858 | 165690 | 092224 | 050025 | 026280 |
| 1.6 | .40 | 192626 | 152606 | 092161 | 052365 | 027992 |
| 1.6 | •45 | 169701 | 140268 | 090518 | 053643 | 029122 |
| 1.6 | •50 | 151184 | 128936 | 087805 | 054014 | 029694 |
| 1.6 | •55 | 135869 | 118642 | 084400 | 053628 | 029743 |
| 1.6 | .60 | 122950 | 109323 | 080573 | 052621 | 029308 |
| 1.6 | .65 | 111869 | 100879 | 076513 | 051113 | 028428 |
| 1.6 | .70 | 102225 | 093204 | 072344 | 049204 | 027139 |
| 1.6 | •75 | 093724 | 086198 | 068151 | 046973 | 025470 |
| 1.6 | .80 | 086145 | 079843 | 063983 | 044483 | 023461 |
| 1.6 | .85 | 079317 | 073833 | 059869 | 041779 | 021077 |
| 1.6 | .90 | 073105 | 068321 | 055822 | 038860 | 0183 62 |
| 1.6 | •95 | 067402 | 063168 | 051845 | 035842 | 015285 |
| 1.6 | 1.00 | 062120 | 058320 | 047929 | 032632 | 011804 |
| | | | | • • | | |
| 1.8 | 0 | | 0 | 0 | 0 | 0 |
| 1.8 | .05 | -1. 590926 | 092989 | 023798 | 010181 | 005207 |
| 1.8 | .10 | 794547 | 15 7 891 | 045435 | 019916 | 010270 |
| 1.8 | .15 | 528671 | 189088 | 063340 | 028817 | 015053 |
| 1.8 | .20 | 395424 | 196410 | 076819 | 036596 | 019444 |
| 1.8 | .25 | 315225 | 190919 | 085958 | 043087 | 023354 |
| 1.8 | .30 | 261548 | 179824 | 091336 | 048237 | 026723 |
| 1.8 | •35 | 223025 | 166934 | 093728 | 052088 | 029822 |
| 1.8 | .40 | 193969 | 143784 | 093894 | 054746 | 031742 |
| 1.8 | .40 .45 | 171223 | 141892 | 092486 | 056353 | 033400 |
| 1.8 | .50 | 152891 | 130758 | 090015 | 057063 | 034525 |
| 1.8 | •55 | 137767 | 120667 | 086861 | 057031 | 035156 |
| | .60 | 125044 | 111559 | 083294 | 056395 | 035338 |
| 1.8 | | 114166 | 103334 | 079506 | 055278 | 035116 |
| 1.8 | .65 | 104734 | 095887 | 075623 | 053783 | 034537 |
| 1.8 | .70 | | | 071730 | 051994 | 033641 |
| 1.8 | •75 | 096454 | 089120 | 067882 | 049980 | 032465 |
| 1.8 | .80 | 089108 | 082942 | | 047792 | 031040 |
| 1.8 | .85 | 082525 | 077273 | 064109 | 047192 045471 | 029392 |
| 1.8 | •90 | 076573 | 072045 | 060430 | 043048 | 027540 |
| 1.8 | •95 | 071149 | 067198 | 056851 | | 025495 |
| 1.8 | 1.00 | 066167 | 062679 | 053365 | 040541 | 02,497 |
| | | | | L | | |

TABLE II.- TABULATION OF THE DOWNWASH FUNCTION $F_{w}(|y_{1,o}|)$ - Continued

m = ∞

| ſ | Τ | T | 1 | | i | I |
|--|---|---|--|---|---|---|
| x | ly _{i,o} l | z _o = 0 | z _o = 0.2 | z _o = 0.1 | $z_0 = 0.6$ | z _o = 0.8 |
| 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 | 0 .05 .10 .15 .20 .25 .30 .35 .40 .45 .50 .66 .70 .75 .80 .95 1.00 | -1.591051794779529023395893315813262257223856194924172504154101139108126520115781106492098360091167084745073805068916 | 00931121581371894581969041915381805701678081550431430301320311220801131141050350977410911310851160795618074568069909065593 | 0023941045726063765077396086677092204094745095816093816091500088505085111081496077793074088070435066867 | 0010364020282029367037332044011049352058051058980059161058747057860056604055066053315051407049383049277049383 | 000546701079001583602049102466902831103138803589403727203821603824038625038109037337036346035166035823032338 |
| | 0 .05 .10 .15 .20 .25 .30 .35 .40 .45 .50 .55 .66 .70 .75 .88 .90 .95 .90 | -1.591759794953529282396240316248262780224468195628173100154990140092127601116961107774092662086351080682075553070882 | 0093202158328189728197265191991181116168447155776143859132958123106114242106267099079092579086677081295076367071833 | 0024042045924064075077801087190092821095468095895094751082895072212068779072212068779065457062254059174 | 001048802053202974203783304463905010905428405727206027206059406032405958605848405710405551905378205193805021048057 | 0005633011122016335021158025506029320035271035257103738803900104013604084004115604086004031803956803968039683038643036373 |
| 2.6 2.6 2.6 2.6 2.6 2.6 2.6 2.6 2.6 2.6 | 0 .05 .10 .15 .20 .25 .30 .35 .40 .45 .50 .65 .70 .75 .80 .95 .90 | -1.591253 795186 529240 596708 316835 265487 225295 196575 174170 156184 141412 129049 118539 109484 101593 094646 088476 082953 077974 | 0093388158558190090197749192597181845169300156754144965134192124470115737107898100847094487094487094788074398074398070309 | 0024175046189064474078354087857093623096407095969093909091175088040084693081264077841074477071209068055065026062125 | 0010644020842030209038459045421051050055386060645061868062263061702060780059586059586059586058191056650055009053490051556 | 0005827011510016917021937026482030496033948036836039175040999042349043822044043043984043686043189042526041726040814 |

TABLE II.- TABULATION OF THE DOWNWASH FUNCTION $F_w(|y_{i,o}|)$ - Continued

m = ∞

| | | | | | | · · |
|--|--|---|---|--|---|---|
| x | [y _{i,0}] | z _o = 0 | z _o = 0.2 | z _o = 0.4 | z _o = 0.6 | z _o = 0.8 |
| 3.0 3.0 3.0 3.0 3.0 3.0 3.0 3.0 | 0 .05 .10 .15 .20 .25 .30 .35 .40 .45 .50 .55 .60 .65 .70 .75 .80 .85 .90 .95 | -1.590768795333529853529853397002317203263923225812197167174838156929142234129949119519110544102734095870089784084347079455075026 | 0093988158708198050198050192973169829157361145649134954125311116659108901101932095655089933084833080144075855071918 | 0024255046350064715078656088260094109096975097622094728092079089029085770082430075824072649069590066658063856 | 0010734021023030480038819045874051595056023059267061469063776063776062913062092061000059708058274055144053511 | 000593301172201723602236302701503113703469803769604014604208204354604585045653045653045674043907043131 |
| 3.5 3.5 3.5 3.5 3.5 3.5 3.5 3.5 3.5 3.5 | 0 .10 .15 .20 .25 .30 .35 .40 .45 .50 .55 .60 .75 .80 .85 .90 .95 .10 | -1,591387 -,795450 -,530029 -,397237 -,317497 -,264282 -,226225 -,197640 -,175371 -,157523 -,146025 -,130666 -,120297 -,111385 -,103639 -,096839 -,096839 -,096818 -,085446 -,080621 -,076260 | 0093474158828190495198452193272182657170250157842146191135558125978117388109693102788096576090967085885081263077042073174 | 002431704652106490407890808857509448709741809812909727409536409278108660508333208067076864073759070771067911065182 | 0010800021160030686039113046218052008056506059820062092063482064215063829063077062061060844059486058031056513054961 | 0006010011877017468022673027403031603035243038319040850042866044411045532046280046704046851046763046034045457044773 |

TABLE II.- TABULATION OF THE DOWNWASH FUNCTION $F_w\left(|y_{i,o}|\right)$ - Concluded

m = ∞

| | | | ш = | | | |
|--|---|---|--|--|---|---|
| x | y _{i,0} | z _o = 0 | z _o = 0.2 | z _o = 0.4 | z _o = 0.6 | z _o = 0.8 |
| 4.0 4.0 4.0 4.0 4.0 4.0 4.0 4.0 4.0 4.0 | 0 .05 .10 .15 .20 .25 .30 .35 .40 .45 .50 .65 .70 .75 .80 .85 .90 | -1.591424795526530143397390317688264511226492197946175716157907143312131129120800111928104222097462091482086152081369 | 0093496158905190611198443193466182889170521158152146541135947126407117857110202103338097167091599086559081978078849 | 00 ≥43580 165560 1550240 1790680 1847290 177000 184520 176370 175370 175210 175210 1752560 175150 18699 | 0 010845 021246 030630 039265 046432 052265 056807 060164 062480 063914 064735 064735 064390 065688 062716 061546 060234 058826 057356 | 0006057011970011970017609022859027638031885035572038696041274043339046102046899047373047569047532046906046381 |
| 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 | 0 .05 .10 .15 .20 .25 .30 .35 .40 .45 .50 .555 .60 .65 .70 .75 .80 .85 .90 .95 1.00 | 077051 -1.591470795615530278397569317912264780226806198306176121158357143808131671121391112563104903098190092258086975082240077970 | 073975 0093541158995190746198624193692183161170838158515146949136402126907118404110796103979097854092334082809078679074903 | 04.6016 001.440501.657401.516401.925401.500801.802601.802601.802601.802601.802601.802601.802601.802601.802601.802601.802601.802601.802601.802601.802601.802601.802701.802601.802701.802601.8027 | 055851 0010939021343030960046676052558057148060555062894065157065324065029064378065029064378062338061078059721058303056851 | 047884 D006108012074012074017764023068027897035197035936039116041744043861045507046731048109048377048200047862047392046818 |

TABLE III.- TABULATION OF THE DOWNWASH FUNCTION Fw,O

| | I 1 | | - I | | | | η | | | | |
|--|--|--|---|--|--|---|--|--|---|--|---|
| × _o | z ₀ = 0 | z _o = 0.2 | z ₀ = 0.4 | z _o = 0.6 | z _o = 0.8 | ×υ | z _o = 0 | z _o = 0.2 | z _o = 0.4 | z _o = 0.6 | z _o = 0.8 |
| | | | βm = 0 | | | βm = 1.0 | | | | | |
| 0.6 .8 1.0 1.2 1.4 1.6 1.8 2.0 2.2 2.6 3.0 5.0 | 0.550517 397887 318310 26528 227364 198944 176859 159159 144686 122427 106103 .090,46 .079577 .0636620 | 0.477465 .374482 .30609 .2288.7 .19583 .174682 .157579 .145500 .121707 .105634 .090650 | 0.567281 .518510 .274405 .258732 .210205 .187241 .153034 .140056 .115996 .104250 .067773 .078790 | 0.265258 .234048 .234051 .212207 .192083 .174416 .159155 .146014 .134670 .116237 .102022 .088349 .077826 | 0.190986 .198944 .194091 .183640 .171598 .159155 .147670 .137202 .127789 .099059 .086430 .076517 .062073 | 0.6 .8 1.0 1.2 1.4 1.6 1.8 2.0 2.6 3.5 4.0 5.0 | 0.530517 .397887 .518310 .265258 .227364 .198944 .176839 .159159 .14458 .12427 .106103 .090946 .075577 | 0.562698 .410936 .524874 .269021 .209720 .200516 .177941 .159927 .145288 .122791 .106340 .091095 .075677 | 0.711763 .459441 .347505 .281349 .237245 .205468 .181374 .162437 .147139 .125902 .107059 .091546 | 0 .601550 .397887 .306294 .251646 .214605 .187566 .166840 .150387 .125823 .108291 .092312 .080488 .064125 | 0 .530516 .555881 .277053 .289720 .197407 .173652 .155319 .128669 .110076 .093419 .081218 |
| | | L | m = 0.2 | | | | | β | m = 1.2 | | |
| 0.6 .8 1.0 1.2 1.4 1.6 2.0 2.2 2.6 3.0 3.0 4.0 5.0 | 0.55051.7 .597887 .518510 .265:28 .227364 .198344 .176859 .159155 .144686 .1224-27 .104105 .090446 .077577 .0630620 | 0.480451 .375836 .306784 .258512 .229086 .196065 .174811 .157673 .143571 .121750 .105662 .07657 | 0.375208 .322493 .276815 .240226 .211186 .187918 .169007 .153592 .140329 .119764 .104360 .089845 .076857 .065281 | 0.276253 .261325 .258278 .214996 .1193997 .175776 .160150 .146762 .135245 .116597 .102261 .088502 .077930 | 0.205568 .207190 .197742 .187604 .174244 .161247 .149241 .128729 .099464 .086692 .077066 | 0.6 1.0 1.2 1.4 1.6 1.8 2.0 2.6 3.5 4.0 5.0 | 0.536517 .397887 .518510 .265228 .227364 .198944 .176839 .159155 .144686 .122427 .106103 .090546 .079577 .0636620 | 0.608595 .428894 .533768 .274078 .232872 .202613 .174407 .161022 .146086 .123275 .106653 .091291 .079809 | 1.099136 .558830 .590321 .5904297 .251052 .214447 .187558 .166884 .1294879 .108335 .092344 .080511 | 0 1.213045 545006 372554 288420 237467 202865 177627 158299 130467 111256 094151 081708 | 0 0 1.584540 549568 .564778 .279415 .228952 .195160 .170737 .157462 .115625 .096798 .083447 |
| | <u></u> | í | 3m = 0.4 | | | | | f | m = 1.4 | | |
| 0.6 .8 1.0 1.2 1.4 1.6 2.0 2.2 2.6 3.0 4.0 5.0 | 0.936917 .397887 .318310 .805258 .207304 .198944 .176859 .159155 .144656 .12447 .106103 .070946 .070977 .0650620 | 0.489600 .379949 .308955 .399788 .223698 .196012 .179197 .107996 .143784 .121879 .109746 .000721 .079427 .063585 | 0.400812 .555613 .284280 .244800 .214177 .185977 .170470 .141151 .120268 .104691 .090073 .078978 | 0.314587 .283299 .29374:2 .199934 .179962 .163200 .149046 .136936 .117687 .102984 .088906 .078242 .062974 | 0.251534 .235941 .218507 .200406 .185277 .167807 .154128 .14-2150 .131622 .114-277 .100697 .087489 .077258 | 0.6 .8 1.0 1.2 1.4 1.6 1.8 2.0 2.2 2.6 3.0 5.5 4.0 5.0 | 0.530517 .397887 .518310 .265258 .227364 .198944 .176839 .159155 .144686 .122427 .106103 .090346 .071577 | 0.671460 451865 344814 280262 235690 205139 181165 162296 147059 125847 107025 031525 063860 | 2.577412 .733097 .453927 .355730 .269169 .225932 .195333 .172407 .154518 .128284 .109877 .093303 .061148 | 0 0 .896475 .488731 .345046 .270229 .223820 .191958 .166584 .114958 .006404 .063189 .006485 | 0 0 1,288706 ,551964 ,366548 ,278734 ,226977 ,19255 ,151357 ,101062 ,086203 ,066968 |
| | <u> </u> | | 3m = 0.6 | | L | βm = 1.6 | | | | | |
| 0.6 1.0 1.2 1.4 1.6 1.8 2.0 2.2 2.6 5.0 5.0 | 0.550)17 .597887 .518310 .265258 .227364 .198594 .176859 .159155 .144686 .122427 .106103 .000946 .077977 .0656620 | 0.505509 .386962 .312624 .261938 .225262 .197530 .173844 .158478 .144140 .12203 .105887 .0;0803 .073486 | 0.450655 .59968 .297456 .292754 .219542 .195481 .172965 .156312 .142539 .121117 .105447 .00405 .079214 .063475 | 0.404357 .527609 .277296 .259712 .210528 .187520 .158905 .159999 .119943 .104208 .089243 .076767 | 0.413604 .303268 .257408 .225327 .200197 .179784 .162890 .148718 .136497 .117492 .102809 .088843 .078156 | 0.6 .8 1.0 1.2 1.4 1.6 2.0 2.2 2.6 3.0 3.5 4.0 5,0 | 0.550917 .597887 .518510 .265258 .227364 .198944 .176859 .159159 .114468 .122427 .106105 .090946 .079577 .0636620 | 0.758659 .481031 .558357 .287691 .241227 .208119 .183230 .163787 .148152 .124514 .107457 .091796 .080146 | 0 1.087125 552257 379330 292945 240516 204994 179168 159450 131156 111701 094429 081894 064837 | 0 0 3.526118 .751306 .445609 .322123 .254873 .212298 .182753 .144116 .119713 .095275 .085057 | 0 0 0 1.144073 545562 365547 .276029 .224130 .165025 .131956 .06359 .089984 |
| | | 1 | βm = 0.8 | | | | | | βm = 1.8 | | |
| 0.6 8 1.0 1.2 1.4 1.6 1.8 2.0 2.2 2.6 3.5 4.0 5.0 | 0.550517 .397887 .318310 .265258 .227564 .198344 .176359 .159125 .144686 .122427 .106105 .000346 .075277 .0636620 | 0.529278 .597105 .517887 .264.998 .227159 .198828 .176756 .155094 .144640 .122399 .106085 .050934 .079570 .063658 | 0.540655 .598285 .517678 .204639 .226879 .176562 .176562 .18943 .144522 .122325 .106055 .079547 .063646 | 0.690142 413604 321213 .265523 227023 198501 .176426 .158801 .144392 .12222 .105962 .09852 .09852 .079513 | 0 .487607 .536690 .270527 .288750 .199145 .176641 .158839 .144555 .122150 .105896 .090798 .070472 .065604 | 0.6 .8 1.0 1.2 1.4 1.6 2.0 2.2 2.6 3.0 5.0 5.0 | 0.550517 .57887 .518510 .265258 .227564 .1789944 .176859 .159155 .144686 .122427 .106105 .090946 .079577 .0636620 | 0.882896 5160799 374764 296516 246595 211589 185519 165509 149430 125278 107950 092104 080552 064057 | 0 2.074581 .714895 .441443 .524457 .259040 .216945 .167364 .163364 .13534 .113543 .113543 .095734 .062753 .065268 | 0 0 1.383055 .607086 .393632 .293949 .236843 .19277 .152817 .12491 .102349 .087055 .067374 | 0 0 0 1.037291 ->28637 ->57448 -271921 -186614 -143665 -113007 -033689 -070522 |

TABLE III.- TABULATION OF THE DOWNWASH FUICTION $F_{w,0}$ - Concluded

| | T | Т. | Т | | т | | г ——— | | | , | T |
|---|---|--|---|---|---|---|---|---|--|--|---|
| × _o | z _o = 0 | z ₀ = 0.2 | z _o = 0.4 | z _o = 0.6 | z ₀ = 0.8 | × _o | z _o = 0 | z ₀ = 0.2 | z ₀ = 0.4 | z _o = 0.6 | z _o = 0.8 |
| | βm = 2.0 | | | | | βm = 4.0 | | | | | |
| 0.6 8 1.0 1.2 1.4 1.6 1.8 2.0 2.6 5.0 3.5 4.0 5.0 | 0.530517 .397887 .318310 .265258 .227364 .198944 .176859 .159155 .144686 .122427 .106103 .090346 .079577 .063662 | 1.067644 .565466 .394664 .306926 .252727 .215573 .188550 .107461 .150880 .126141 .108506 .092451 .080683 | 0 0 1.020224 .533822 .366908 .281759 .197552 .172419 .116292 .097229 .083730 .065755 | 0 0 0 0 9,83154 1,920259 3,55861 272526 222212 1,164245 1,31555 1,106174 0,69458 0,68540 | 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | 0.6 .8 1.0 1.2 1.4 1.6 1.8 2.0 2.2 2.6 3.0 5.0 | 0.530517 .397887 .318310 .265258 .227364 .176839 .159255 .144686 .122427 .106103 .090346 .079577 .063662 | 0 0 1,326291 .610062 .399283 .300043 .242273 .204297 .177298 .141202 .117953 .098230 .083863 .066079 | 0 0 0 0 0 1.488866 .658430 .418156 .240316 .171043 .127171 .102148 | 0 0 0 0 0 0 0 0 0 0 0 1.582187 .442089 .224101 .150146 | 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 |
| | | f | 3m = 2.5 | | | | | β | m = 4.5 | | |
| 0.66 .8 1.0 1.2 1.4 1.6 1.8 2.0 2.6 3.0 3.5 4.0 7.0 | 0.950917 .597887 .518510 .269258 .227,564 .176359 .159155 .144686 .122427 .106105 .070946 .079977 .063662 | 2.903378 .758629 .465256 .341613 .272628 .228148 .126842 .173482 .128755 .110179 .093491 .081273 | 0 0 1.151689 .568529 .579345 .287118 .252628 1.196549 .151448 .124124 .101888 .086741 .007254 | 0 0 0 0 2.188412 .767792 .456151 .324507 .208056 .155085 .119022 .097340 | 0 0 0 0 0 0 0 0 1.135780 -380946 -227158 -152706 -116514 -080246 | 0.6 .8 1.0 1.2 1.4 1.6 1.8 2.0 2.6 3.0 5.0 | 0.530517 .397887 .318310 .265258 .227364 .196944 .176839 .159155 .144686 .122427 .106103 .090946 .079577 .063662 | 0 3.175013 .861921 .488889 .544126 .267852 .220705 .188560 .147269 .121633 .00623 .085801 | 0 0 0 0 0 0 0 0 1.587507 .692027 .311658 .201632 .1110353 .077825 | 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 |
| | | β | m = 3.0 | | | βm = 5.0 | | | | | |
| 0.6 .8 1.0 1.2 1.4 1.6 1.8 2.0 2.2 2.6 3.0 5.0 | 0.550517 .597687 .518510 .505258 .227504 .176859 .159455 .144686 .122427 .106103 .050946 .079577 .005662 | 0 1.203098 585128 595806 500748 249262 208121 181348 161034 132075 112284 082131 | 0 0 1.272318 .601549 .592196 .2934696 .170240 .134962 .108110 .090674 .069118 | 0 0 0 0 0 0 0 1.304023 .621412 .295593 .195043 .136659 .108670 .077122 | 0 0 0 0 0 0 0 0 0 1.312058 .410193 .214671 .146282 | 0.6 .8 1.0 1.2 1.4 1.6 1.8 2.0 2.2 2.6 3.0 3.5 4.0 5.0 | 0.530517 .397887 .318310 .265258 .227364 .198944 .176839 .159155 .144686 .122427 .106103 .090946 .079577 .063662 | 0 0 1,43911 .636752 .407763 .502229 .241811 .202627 .154582 .125977 .087453 .067569 | 0 0 0 0 0 0 0 0 1.680954 .445567 .248289 .161422 .120906 | 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 2 0 | 0 0 0 0 0 0 0 0 0 0 0 0 0 0 |
| | | βι | m = 3.5 | | | | | | | | <u> </u> |
| 0.6 .8 1.0 1.2 1.4 1.6 1.8 2.0 2.5 5.0 5.0 | 0.530517 .597887 .318310 .205258 .227364 .138944 .176839 .159155 .144686 .122427 .106103 .090946 .079577 | 0 2.768413 .810405 .475024 .340777 .268425 .222907 .191438 .168862 .136186 .114858 .096301 .083164 | 0 0 0 0 1.384207 .635035 .405203 .296625 .198013 .149959 .116322 .099719 | 0 0 0 0 0 0 0 0 0 0 2.973954 .517957 .270135 .169830 .125187 | 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | | | | | | |

TABLE IV. - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(ly_{i,o}l)$

βm=0.2

| Хo | y _{i,0} | z _o = 0.2 | z ₀ =0.4 | z ₀ =0.6 | z _o = 0.8 |
|---|--|--|--|--|---|
| 666666666888888888888888888888888888888 | 00505050505050505050505050505050505050 | 3321 321 321 3321 3321 3331 33 | .138201 .135341012 .135568362 .035668362 .035668362 .035668145514 .11982366215514 .11982366215514 .1198266215514 .1198266215514 .1198266215514 .1198266215514 .1198266215514 .1198266215514 .1198266215514 .1198266215514 .119826621514 .1198266 | .0663367 .066372118387 .0663751683 .0653751683 .0053679440 .00536790001444 .00536790001444 .00537700014345 .00337700014345 .00337700014345 .00771554427 .00658447515151 .0077155700353 .0077155700353 .0077155700353 .0077155700353 .0077155700353 .0077155700353 .0077155700353 .0077155700353 .0077155700353 .0077155700353 .0077155700353 .00771558 .0077158 .007715 | . 0 3 5 4 3 4 5 6 6 3 4 3 4 5 6 6 5 7 2 5 6 6 5 7 2 2 3 1 6 6 6 5 7 2 2 3 1 6 6 5 7 2 2 3 1 6 6 5 7 2 2 3 1 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_v(ly_{i,o}l)$ - Continued

βm = 0.2

| Хo | Yi,o | z ₀ =0.2 | Z _O = 0.4 | Z _O = 0.6 | Z _O = 0.8 |
|---------------------------------------|--|--|---|--|---|
| 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 | 05050505050505050505050505050505050505 | ************************************** | 1841424264854427642854406 1874242764284408534406 18742427648854406 187424276488592453806887489999999999999999999999999999999999 | 11184921159384442130651159844221715988244423755000337065517971604477604798511009985180206634488094442427774706798811209988117460998811747067988117470699851791211111110998811747069981174706998811747069988117470699881174706998811747069988117470699881174706998811747069988117470699881174706998811747069988117470699881174709988117470698811747069988811747069988811747069988811747069988811747069988811747069988811747069988888888888888888888888888888888888 | .075234 .0774849 .077188887 .077188887 .077188887 .076633874 .0755333244038 .00555333244038 .00555333244038 .00555333244038 .00555333244038 .00555333244038 .00555333244038 .00555333244038 .00777399428 .00177994289533 .007773995538 .007777395518 .0077777777777777777777777777777777777 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(|y_{i,o}|)$ - Continued

βm=0.2

| Хo | Yi,o | z ₀ = 0.2 | z ₀ =0,4 | z _o = 0.6 | z _o =.0.8 |
|--|--|--|--|---|---|
| 1 1 1 1 000000000000000000000000000000 | . 00 505050505050505050505050505050505050 | 5 088 6115 99 77 08 82 10 77 08 82 115 127 08 115 127 08 1 | 191433 1191433 1191433 1191433 1191433 1191431 1191433 1191431 | -12184 -12284269924269924269924260942600 -00461552504983690 -00461552504983690 -00461552504983690 -0055449836920 -00554549836920 -00554549836920 -0055454980 -0055454980 -0055454980 -00554549992 -0055454980 -00650 -00660 -00650 -00650 -00650 -00650 -00650 -00650 -00650 -00650 -00660 -00650 | -0854270018 -0854270018 -0854270018 -0854270018 -09554270018 -09554270108 -09554270108 -09554013 -09554013 -09554013 -09554013 -0955442912 -0955442912 -0955442912 -0955244400 -0955244421 -095524421 -095524421 -095524421 -095524421 -0955244421 -09552442 -09552442 -095624 -095624 -095624 -095624 -095624 -095624 -095624 -095624 -095624 -095624 -095624 -095 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_v(|y_{i,o}|)$ - Continued $\beta m = 0.2$

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $\mbox{ F}_{\nu}(\mbox{Iy}_{i,o}\mbox{I})$ - Continued

 β m = 0.2

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{v}(ly_{i,o}l)$ - Continued

 β m = 0.4

| | βm=0.4 | | | | |
|----|--|---|--|--|--|
| Хo | Yi,o | z _o =0.2 | z _o = 0.4 | z _o = 0.6 | z _o = 0.8 |
| | .00 .00 .10 .10 .10 .30 .30 .30 .30 .30 .30 .30 .30 .30 .3 | .3672 .3672 .3672 .3672 .3672 .3672 .3672 .3672 .3672 .3672 .3672 .3672 .3672 .3662 .3662 .3662 .3662 .3762 .3762 .3762 .3762 .3762 .3763 | .136040 .1367951 .1367951 .10046279 .110046279 .0100462999 .1100462999 .010094 .124599 .010094 .124599 .125368 .00094 .124599 .10094 .12410999 .10094 .10094 .10094 .10094 .10094 .10094 .1009999 .10099991 .000929110 .110994 .10099991 .000929110 .1109974 .000929110 .11014 .11019999 .00093114 .11016 .11019999 .1101999 .11019999 .11019999 .11019999 .1101999 .1101999 .1101999 .11019999 .1101999 .110199 .110199 .110199 .110199 .110199 .110199 .110199 .110199 .110199 .110199 .110199 .110199 .1101999 .110199 .110199 .110199 .110199 .110199 .110199 .1101999 .110199 .11 | .066063 .00525642 .00525642 .00525642 .00525642 .00525600 .0043832 .0050000 .085922 .0050375 .007827860 .0059376 .005937 | .03747 .0353883 .0352983 .0352983 .0352983 .036970 .0400000 .0400000 .04491648 .055248 .04491648 .055248 .04491648 .055248 .04491648 .055248 .0 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(ly_{i,o}l)$ - Continued

βm=0.4

| Хo | y _{i,o} | z _o =0.2 | z _o =0.4 | z ₀ = 0.6 | z _o =0.8 |
|---|--|---|--|--|--|
| 1.6.6.6.6.6.6.6.6.6.6.6.6.6.6.6.6.6.6.6 | 00505050505050505050505050505050505050 | 246439903510704070351056555555555555555555555555555555555 | 32117744744078300855044178504831359700644183329733248694869484121 1110876680383295249702850441183009655486911110876651109766511097665110976554483329521111087655448332952111108765544833295211110876554483329521111087655448332952111108765544833295211110876554483329521111111111111111111111111111111111 | 1173 1113 1113 1113 1113 1113 1113 1113 | .080547 .0801182 .0801182 .07717070 .077477070 .0764066980 .07741730 .0766406980 .07741730 .0766406980 .005588989 .005588989 .005588989 .005588989 .005588989 .005588989 .005588989 .005588989 .005588989 .005588989 .005588989 .005588989 .005588989 .0055883 .005883 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(ly_{i,o}l)$ - Continued

 β m = 0.4

| | | | | |
|--------------------|----------------------|--|--|---|
| xo y _{i,} | z ₀ = 0.2 | Z _O = 0.4 | z _O = 0.6 | z _o = 0.8 |
| 3 | 560 | .193056 .1193056 .11930704 .11930704 .11930707 .119307 .1193 | .124085 .173107 .1106554 .11106737 .1044552 .1044552 .1044552 .0047531 .0043131 .004 | .088575 .077476 .08776 .0774778 .077477 .077476 .077477 .077476 .077477 .07747 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(ly_{i,o}l)$ - Continued

βm=0.4

| Хo | yi,o | z ₀ = 0.2 | z ₀ =0.4 | z _o =0.6 | z ₀ = 0.8 |
|--|---|--|---|--|--|
| 1 3.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5 | 995005050505050505050505050505050505050 | 39 5 0 8 6 2 1 1 6 2 2 9 1 8 6 2 2 2 2 2 1 8 6 2 2 2 2 2 1 8 6 2 2 2 2 2 1 8 6 2 2 2 2 2 1 8 6 2 2 2 2 2 2 1 8 6 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 | 19 9 1862 0 169 2 2 8 4 7 8 4 8 1 9 8 6 1 0 6 9 2 2 9 9 1 7 7 5 6 2 9 8 2 1 1 1 1 2 1 2 8 6 7 2 7 2 8 6 5 7 1 1 1 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1 2 | 912991558991558610471705111356640003225926899611221738708700000000000000000000000000000000 | •••••••••••••••••••••••••••••••••••••• |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_v(|y_{i,o}|)$ - Continued $\beta m = 0.6$

| ×ο | y _{i,} o | z _o =0.2 | z _o =0.4 | z ₀ =0.6 | z _o = 0.8 |
|---|---|---|---|---|---|
| .66666688888800000000000000000000000000 | .005 0.105 0 | .36 0 5 9 5 9 5 9 9 9 1 1 2 7 8 9 5 9 9 9 9 1 1 3 3 5 5 7 4 8 5 1 1 2 9 8 7 9 9 9 9 9 1 1 3 3 5 5 7 5 5 7 5 1 9 9 1 5 6 7 7 5 7 9 1 1 4 3 5 1 5 7 5 9 9 1 1 1 1 5 1 8 9 8 7 9 5 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | .141956 .138944 .11384075 .00000000 .1161850771 .00000000 .16619664 .11519662 .11519662 .11519664 .11519664 .11519664 .11519664 .11519664 .11618780 .11719780 .1181980 .1181980 .1 | .064697 .0639549 .0605498 .00605698 .00700000 .00870800 .00876200 .0087684 .0074784 .0066411 .0066411 .007697408 .0076874 .0076874 .0076874 .0076874 .0076874 .0076874 .0076874 .0076874 .0076874 .0076874 .0076874 .0076874 .0076874 .0076874 .0076874 .0076874 .0076874 .0076874 .007688 .007688 .007688 .007688 .007688 .007688 .007688 .007688 .007688 .007688 .007688 .007688 .007688 .007688 .007688 .008888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .008888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .008888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .008888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .008888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .008888 .008888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 .00888 | .027918 .028149 .0386422 .0000000 .00000000 .00000000 .00000000 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{v}(ly_{i,o}l)$ - Continued

 β m = 0.6

| Хo | β ί,ο | z _o =0.2 | z _o = 0.4 | z ₀ =0.6 | z ₀ = 0.8 |
|--|---|---|--|---|---|
| 1.6 6.6 6.6 6.6 6.6 6.6 6.6 6.6 6.6 6.6 | . 0 1 1 2 2 3 3 4 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 0 1 1 2 2 3 3 4 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 0 1 1 2 2 3 3 4 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 0 1 1 2 2 3 3 4 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 0 1 1 1 2 2 3 3 4 4 5 5 6 6 6 7 7 8 8 9 9 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | .398332026 .39944622960367222967222969693863363263383114426022667229672229672229672296669366693666994662629966635642629966635666633663563636363636363636363636 | .189128 .186068 .1764608 .166808 .1 | .118558 .1176448 .11769768 .110768 .1053976 .09829984 .09849895 .097180098 .097180098 .0077180098 .00547848 .00547848 .00547848 .00547847 .00408 .00547847 .00408 .00547847 .00408 .00547847 .110180725 .110180725 .110180725 .110180725 .110180725 .110180725 .110180725 .110180725 .110180725 .110180725 .110180725 .110180725 .110180725 .110180725 .110180725 .11180725 .11180725 .11180725 .11180725 .11180725 .11180725 .11180725 .11180725 .11180725 .00609990 .005501424 .00318479 .0045785 .0045785 .0059785 .0059785 .0059785 .0059785 .006082996 .005082996 .005082996 .0050829976 .0060829976 | .081416 .081440 .080478 .0773010 .0628440 .0773010 .06581215 .00543552 .0054665 .00546679 .0044699936 .0044699936 .0044699936 .00443998830 .00446916 .0053369 .00446916 .0053369 .00462356 .0053369 .00462356 .0053369 .00462356 .005336 .00462356 .005336 .00462356 .005336 .00533776 .00462356 .00533776 .00462356 .0053376 .0055978417 .00663978787878787878787878787878787878787878 |

TABLE IV - TABULATION OF THE SIDEWAS+FUNCTION $F_v(|y_{i,o}|)$ - Continued $\beta m = 0.6$

| Хo | Yi,0 | z ₀ =0.2 | z _o =0.4 | z _o = 0.6 | z _o = 0.8 |
|---|--|--|--|--|--|
| 2.6 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 | 00 01 01 01 01 01 01 01 01 01 | .395205 .371800 .315628 .371800 .315628 .351966 .1962593 .1197465 .0076901 .00528036 .00377797 .004371768 .00377397 .001882975 .001882975 .001882975 .001882975 .001882975 .001882975 .001882976 .001882975 .001882975 .001882976 .001882976 .001882976 .001882976 .001882976 .0018845518 .0018845518 .0018845518 .0018849 .0018849 .0018849 .0018849 .0018849 .0018849 .0018849 .0018849 .0018849 .0018849 .0018849 .0018849 .0018849 .0018849 .0018849 .0018889 .0018849 .0018849 .0018849 .0018849 .0018849 .0018849 .0018889 .0018849 .0018849 .0018849 .0018849 .0018849 .0018849 .0018889 .0018849 .0018889 .0018849 .0018889 | .193659 .193659 .193659 .1959534 .1537488 .1937488 .1937488 .1937888 .194056 .09425387 .0055990 .0049783 .0055990 .00497888 .00510009 .005100009 .005100009 .005100009 .005100009 .00510000009 .00510000000000 | .124896 .1231313 .12131397 .121397 .1115284 .10912884 .0091244 .0091244 .0091244 .0077594 .0064409 .00586408 .0048271 .0058671 .003086728 .003086728 .00308674822 .1126138 .11274808 .11284869 .0040874828 .1137407 .100933844 .00726498 .005674829 .005674829 .0128838 .11137407 .10093384 .00726498 .005674829 .0056748315 | .089501 .0899727 .088915549 .0899727 .088615579 .087356489 .087356489 .08576528637 .055652637 .0556528633229 .09988333229 .099883353839 .09927620333229 .09988335366 .04325560 .04325560 .043335366 .099276 .099883356 .099276 .099883356 .099276 .099883356 .099276 .09883356 .099276 .09883356 .099276 .0988356 .09928 .0988366 .09928 .0988366 .09928 .0988366 .09928 .0988366 .09928 .0988366 .09928 .098836 .09928 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $\mbox{ Fv}(\mbox{Iy}_{i,o}\mbox{I})$ - Continued

βm=0.6

| ×o | y _{i,0} | z _o =0.2 | z _o = 0.4 | z _o = 0.6 | z _o = 0.8 |
|--|--|--|--|--|---|
| 5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5. | 00505050505050505050505050505050505050 | 249768810495089318978864999358788110493588819955384783259784855438478565760744455104955538868939583857332597848597886678678165760744475026688909553478325978848554781657607644750266886909553885778844669696617844750266886909553788416177884669620000000000000000000000000000000000 | -196830 -19730 -1986283 -198730 -198730 -118730 -118730 -118730 -118730 -118767 -118767 -118767 -118767 -118767 -118767 -118767 -118767 -118767 -118767 -11877 -11 | .12990669888888888888888888888888888888888 | 4746464637428781827818278185250782236963185256536396295660688987776639884466688987768343567788223789498888777868844666889877884488668898778888887788888877888888778888887788888 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(ly_{i,o}l)$ - Continued

βm=0.8

| Хo | y _{i,0} | z _o = 0.2 | Z _O = 0.4 | z _o =06 | z _o = 0.8 |
|--|---|---|---|---|---|
| .6666668888888888888888888888888888888 | .0050 .0150 | 3649559982308423098466339966882310955586128558612855612856128 | 145277223 1142239333 11308688 1125926855 1130821745 1130821745 1130821745 1130821745 1130821745 1130821745 1132384410 113538284 114359907 11653907 11653907 11653907 11663907 11663907 11663982 112926 11323844 112926 11323844 112926 11323844 112926 11323844 112926 11323844 112926 11323844 112926 11323844 112926 11323844 112926 11323844 112926 11 | .058513 .059000000 .00000000 .00000000 .00000000 .008874320 .085685 .0826851 .000000000 .00000000 .1010000 .0000000 .1021582 .0956602 .0956602 .0956602 .0853697 .0853697 .11106998 .096599 .097450000 .11159308 .09865999 .07450000 .11159308 .099758053 .097752076 .00000000 .11159308 .099758053 .097752076 .007752076 .007717076 .006184147 .000000000000000000000000000000000000 | . U U U U U U U U U U U U U U U U U U U |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $\mbox{ Fv}(ly_{i,o}l)$ - Continued

βm = 0.8

| | | | βm = 0.8 | | |
|---|---|--|---|---|---|
| Хo | y _{i,o} | z _o = 0.2 | z _o =0.4 | z _o = 0.6 | z _o = 0.8 |
| 1.6666666666668888888888888888888888888 | . 0 0 5 0 5 0 5 0 5 0 5 0 5 0 5 0 5 0 5 | .3746 .37746 .37746 .37746 .371407 .11935 .1 | .1934433443344334433443343434343434343434 | . 1 2 4 2 4 3 1 1 1 2 4 1 1 1 1 2 8 2 1 1 1 1 1 2 8 2 1 1 1 1 2 8 2 1 1 1 1 | 0 8 8 4 3 2 3 2 1 2 0 1 4 1 4 4 4 8 8 5 3 4 6 6 1 7 5 9 8 8 8 2 7 7 5 0 7 1 8 2 6 1 1 7 3 2 4 5 0 0 0 9 6 3 2 3 4 0 1 0 0 0 7 7 5 1 7 8 2 6 1 1 8 0 1 0 8 2 7 7 5 0 7 1 8 2 6 1 1 8 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(ly_{i,o}l)$ - Continued

βm = 0.8

| ×ο | y _{i,0} | z ₀ =0.2 | z _o = 0.4 | z _o = 0.6 | z _o = 0.8 |
|----|---|--|--|--|--|
| | .00 .05 .10 .15 .20 .25 .30 | .395657 .372080 .252080 .252080 .252080 .252080 .252080 .252080 .252080 .252080 .252080 .252080 .27310 .0015377 .0063240 .00777376 .004437630 .0044459 .0044459 .0019017 .00169333 .0014028881 .0019017 .00153037 .00153037 .00153037 .00153037 .00153037 .001633037 .001633037 .001633037 .001633037 .001633037 .00163303 .0017296 .0017296 .0017296 .0017296 .0017296 .0017296 .0017297 .0016308 .0017296 .0017297 .00175779 .00185664 .00196446984 .0019646984 .00196446984 .00196446984 .00196446984 .00196446984 .0019646984 .00196446984 .00196446984 .00196446984 .00196446984 .0019646984 .00196466 .00196466 .00196466 .00196466 .00196466 .001964666 .00196466 .0019666 .00196666 .0019666 .0019666 .0019666 .0019666 .0019666 .0019666 .0019666 .0019666 .0019666 .0019666 .0019666 .0019666 .0019666 .00196666 .0019666 .0019666 .0019666 .0019666 .0019666 .0019666 .001966 | .194513 .19148133 .1829992 .11849992 .11849992 .11849992 .1184992 .1184992 .1184992 .118493 .11983464 .007645988 .00569489 .00569489 .0043524469 .0043524469 .004352469 .00435294009 .002570106 .119598157 .1194129889 .1129517 .1184951197 .005815728 .1184951197 .005815728 .0076591197 .0076591197 .0076591197 .0076591197 .0076591197 .0076591197 .0076591197 .0076591197 .0076664 .0077564663 .0077564664 | . 1260478 . 1224478 . 1128478 . 11284663 . 1128478 . 11284663 . 1099579 . 0995479 . 0995458 . 0784489 . 0600765796 . 0540880 . 04421902 . 0338978 . 1264390 . 03323897 . 1264392 . 03323897 . 1264392 . 03323897 . 1264392 . 03323897 . 1264392 . 03323897 . 1224310 . 110823956 . 0087121 . 00674437 . 00564758 . 00473727 . 12854783 . 0033661715 . 00564583 . 00574736 . 015954066 . 01695707 . 016958337 . 016958337 . 016958337 . 01747465 . 01747474 . 018628766 . 0181376 . 01813766 . 01813766 . 01813766 . 01813766 . 01813766 . 018137 | .09043200 .0852490 .08526490 .08526490 .08526490 .08526490 .08526490 .08526490 .08526490 .08526490 .08526490 .08526490 .08526490 .08526490 .08526490 .08526490 .08626490 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(ly_{i,o}l)$ - Continued

 β m = 0.8

| Хo | Y _i ,o | z _o = 0.2 | z _o =0.4 | z _o = 0.6 | z _o = 0.8 |
|---|--|--|---|--|---|
| 3.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5 | 00505050505050505050505050505050505050 | 3976428 3976428 3976428 315376428 315376428 315376428 315376688 315376688 31537688 3153 | 19444594911999030611993522965442844444946333196975921991599000000000000000000000000000000 | 130086 112964100 11264100 11264100 11163485 1103485 1103485 10963363 08922664 00638428 007594666 00638428 00535880 00435880 00435880 00326618 1033536618 1033536618 11270812 11104094 11273999 11273999 11273999 11273999 11273999 11273999 11273999 11273999 11273999 11273999 11273999 11273999 11273999 11273999 1127399 1127399 1127399 1127399 11273999 1127399 1127399 1127399 1127399 1127399 1127399 1127399 112739 1110409 1096988766 1096988766 109698876 10969889 113047664 11304753 11111711 11097055983 11111711 11097055983 11111711 11097055983 11111711 11097055983 11111711 11097055983 11111711 11097055983 11111711 11097055983 11111711 11097055983 11111711 11097055983 1110409955983 11304783 11304883 11304783 | .09944613 .09944613 .09944613 .09944613 .09944613 .09944613 .0996 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(ly_{i,o}l)$ - Continued

βm = 1.0

| Χo | Yi,o | z _o = 0.2 | z _o =0.4 | z _o = 0.6 | z _o = 0.8 |
|---|---|---|--|--|--|
| .66666688888888888800000000000000000000 | .00505050505050505050505050505050505050 | .375153666537711446875138624538588723399667405588245385887233936666537711446836371266336666537711446836379966973338483841386843897888894048436666666666666666666666666666666666 | .148284 .144338 .14434858 .109997728 .1000029977.1650929128 .11770000233698 .115397500005.1165092998 .1153975000033218 .11583949666 .11390266660 .1187982613 .11390266660 .1142969959 .1142969959 .1142969959 .1142969959 .115357299 .116509266674 .1176382 .1176382 .1176382 .11897506674 .1199882 .1199882 .1199882 .1199882 .1199882 .11998999999999999999999999999999999999 | .000000 .000000 .000000 .000000 .000000 .000000 | .0000000000000000000000000000000000000 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $\mbox{ Fv}(\mbox{Iy}_{i,\,o}\mbox{I})$ - Continued

βm = 1.0

| x _o | y i,o | z _o = 0.2 | z _o = 0.4 | z _o = 0.6 | z _o = 0.8 |
|---|--------------|--|--|---|--|
| 1.8888888888888880000000000000000000000 | | 39734253123 39734253123 39734253125 39734253125 39734325333123 397344533 397344533 39734453 39734453 39734453 39734453 39734453 39734453 39734453 39734453 39734453 39734463 39734463 39734463 39734463 39734463 39734463 39734463 3973463 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 3973463 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 3973463 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 39734663 3973463 3973463 39734663 3 | .19344507 .1942 | .12444 .1241384 .1241384 .11179033655999999999999999999999999999999999 | 0897400000000000000000000000000000000000 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{v}(Iy_{i,o}I)$ - Continued

βm=1.0

| Y _ | N: al | z _o = 0.2 | Z ₀ = 0.4 | 7 0.0 | 7 00 |
|--|--|--|---|--|--|
| × _o | Vi, ol | | | Z ₀ =0.6 | Z _O = 0.8 |
| 66666666666666666666666000000000000000 | 0011223334450505050505050505050505050505050505 | .33715826594199652245839468337711000654383946833972110000397773738844727884883372110000533713899481100000397733899488339468995891177897847889928111000053371538451978998811907845895831117889988111000053371538451978998811100005337153845197899881110000533715384519789988110000533715384519789988110000533715384519789988110000503331531529784485895881110000533715384458190765458110000500000000000000000000000000000 | 11987550505084807756650522951445097234450923351446033318673065155605229537566505229514450975539266652229514450975539266652229514210985566652229514210985566652229514210985566652229514210985566652229514250976695373186770008557784000332867157157157157157157157157157157157157157 | .12845986699708444455889661122544559869644455986996444559869969999444455661122663454906534990611226634561122663456112266345611226634561122663456112266345611226634561122663456112266345611226333007064451346558859614459996112266365594494999611222634055445999611222634055445999611222634055445999611222634055445999611222634594615098826326262626365594459996112222405544599961122224055445999611222240554459996112222405544599961122224055445999611222240554459996112222405544599961122224055445999611222240554459996112223405594599961122224055945999611222240559459996112222405594599961122224055945999611222240559459996112222405594599961122224055945999611222240559459996112222405594599961122224055945999611222240559459996112222405594599961122224055945999611222240559459996112222405594599961122224055945999611222240559459996112222405594599961122224055945999961122224055945999961122224055945999961122224055945999961122224055945999961122224055945999961122224055945999996112222405594599999999999999999999999999999 | 094200044303774882555498255649909574048970998843661002999884303776683182845658498661002099884303776683182845658498661028677669528434037668318286498888610200000000000000000000000000000000 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(|y_{i,o}|)$ - Continued

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(|y_{i,0}|)$ - Continued

βm = 1.2

| Хo | y _{i,0} | z _o =0.2 | z _o =0.4 | z _o = 0.6 | z ₀ = 0.8 |
|---|---|--|---|--|--|
| .66666888888000000000000000000000000000 | . 0 0 5 0 5 0 5 0 5 0 5 0 5 0 5 0 5 0 5 | .344342083440233743364627833666278336662783366627838667388885772088299412599735511522773551522973551628832487538297355161223745520698170528194170087752451152277355162883748751522773515227735152277351522773515227735152277351522773515227735152277351522773551698899958819412597355152277351522773515227735152277351522773551522666602160989995881941259735515226677351529735557762882819412597355152973515297777575757575757575757575757575757575 | .148383 .15046800 .0008268 .13100000 .17761741 .1169259 .1000000 .117619 .1169259 .1000000 .11846923 .1000000 .11846622 .119498 .11648818 .11648818 .11648818 .11648818 .11648818 .1167744 .116382 .11892 .11892 .11892 .11892 .11892 .11892 .11892 .11892 .11892 .11892 .11892 .11892 .11892 .11892 .11892 .11892 .11892 .11893 .11 | .000000 .000000 .000000 .000000 .000000 .000000 | .000000 .000000 .000000 .000000 .0000000 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $\mbox{ Fv}(\mbox{Iy}_{i,o}\mbox{I})$ - Continued

βm=1.2

| Хo | Yi,o | z ₀ = 0.2 | z _o = 0.4 | z _o = 0.6 | z _o = 0.8 |
|--|--|---|---|---|---|
| 1.8 8.8 8.8 8.8 8.8 8.8 8.8 8.8 8.8 8.8 | 05050505050505050505050505050505050505 | .39.6.4.4.2.4.4.8.6.5.9.3.9.6.4.4.2.5.3.4.4.8.6.6.4.9.9.8.6.6.6.4.9.9.8.6.6.6.4.9.9.8.6.6.6.4.9.9.8.6.6.6.4.9.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0 | . 19 457 99 457 99 457 99 457 11 71 560 88 88 89 99 457 11 71 560 88 88 88 89 99 89 88 88 89 99 89 88 88 | . 1 2 4 2 8 9 4 9 1 5 5 6 6 8 3 7 6 1 1 2 4 2 8 8 9 0 0 0 0 0 0 0 0 9 9 2 8 1 1 2 2 1 1 1 1 1 1 1 2 2 1 1 2 2 1 1 2 2 1 1 2 2 1 2 2 1 2 2 2 3 2 2 2 2 | .09153 .0917322 .09917322 .09917322 .09868251 .088425037 .09868251 .098683600 .00774900000000 .0077790000000000 .0077990000000000 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(Iy_{i,o}I)$ - Confinued

βm = 1.2

| Хo | y _{i,0} | z ₀ =0.2 | z ₀ =Q4 | z _o = 0.6 | z ₀ = 0.8 |
|--|---|---|--|--|---|
| 6.666666666666666666666666666666666666 | 0 5050505050505050505050505050505050505 | 3 18813178558477522939 434377707397147830828275527071185688 2 18813178558477522939 434471455770739818282827552527853688 2 3 3 3 5 9 5 4 5 7 7 5 2 2 2 9 3 9 4 5 1 4 7 7 7 3 9 8 1 5 5 8 4 7 7 7 3 9 8 1 5 5 8 4 7 7 7 3 9 8 1 5 5 8 4 7 7 7 3 9 8 1 5 5 8 4 7 7 7 3 9 8 1 5 5 8 4 7 8 5 5 3 9 7 6 7 3 9 8 1 5 5 8 4 7 8 4 7 8 4 7 8 4 7 8 8 6 8 8 7 7 8 9 8 1 5 5 8 7 7 8 9 8 1 5 5 8 7 7 8 9 8 1 5 5 8 7 7 8 9 8 1 5 5 8 7 7 8 9 8 1 5 5 8 7 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 | 19 5 2 2 7 5 2 2 2 7 5 2 2 2 7 5 2 2 3 5 4 0 0 2 2 2 7 5 2 2 3 5 4 0 0 0 2 2 2 7 5 2 2 2 7 7 2 2 2 2 | .13058863 .12295923 .1127295966 .1227295966.004991024 .009991024 .009991024 .009991024 .007065994784 .004546674 .004546674 .004546674 .004546674 .11301487 .112732821 .1104597921 .11114597732829 .0070551921 .00705934928 .004540792 .00866792 .112738883 .004540792 .00876992 .008769492 .00876992 .00876992 .00876992 .00876992 .00876992 .00876992 .00876992 .00876992 .00876992 .00876992 .00876992 .00876992 .0087792 .0087692 .0087692 .008 | . 0 9 4 6 7 8 4 6 7 8 6 9 4 7 8 6 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(ly_{i,o}l)$ - Continued

βm=1.2

| Χo | Yi,0 | z _o =0.2 | z ₀ =0.4 | z _o = 0.6 | z ₀ = 0.8 |
|---|--|--|--|---|---|
| 4.0 4.0 4.0 4.0 4.0 4.0 4.0 6.0 6.0 6.0 6.0 6.0 6.0 6.0 6.0 6.0 6 | .00 50 50 50 50 50 50 50 50 50 50 50 50 5 | .397608 .37760310 .31843766 .1184376676 .129849973 .00763461377 .00763461377 .00763461377 .00763461377 .00763461377 .00763461377 .0076346661 .0076316631479 .0016577 .0016571479 .0016574409 .001657409 .001657409 .001657409 .001657409 .001657409 .0016576767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .0016576767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .00165767 .0016576 | . 19 8 3 7 7 9 9 1 9 3 7 7 9 9 1 9 5 3 6 7 7 9 1 1 7 8 5 9 5 0 7 0 7 1 1 7 5 8 5 5 0 7 0 7 1 1 7 5 8 5 5 0 7 0 7 1 1 2 9 9 7 7 2 7 9 1 2 9 9 7 2 1 0 0 6 6 0 4 2 9 9 7 1 2 9 9 7 2 1 0 0 6 6 0 4 4 4 9 9 7 1 1 1 2 9 9 7 7 8 0 0 6 6 3 3 2 2 6 1 3 9 5 5 6 2 2 7 1 3 1 5 2 2 9 2 7 1 1 2 6 2 9 1 5 1 1 2 6 2 9 1 1 1 1 2 6 2 9 1 1 1 1 2 6 2 9 1 1 1 1 1 2 6 2 9 1 1 1 1 1 2 6 2 7 7 8 0 8 7 7 6 0 5 4 8 7 7 6 0 5 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 | .131767 .13081849 .112395129 .111515599 .112395192 .098474681 .099077128431 .0060526677 .0055100884 .0040726484 .0040726484 .112842884 .112842884 .112842884 .112842884 .112842884 .11284288 .11284288 .11284288 .11284288 .11284288 .11284288 .1138576 .0055776 .0055776 .0055776 .0055776 .005374 .005374 .00334 .00334 .00334 .00334 .00334 .00334 .00334 .00334 .00334 .00334 | . 0 9 8 2 9 5 8 2 9 6 8 2 9 6 8 2 9 6 8 2 9 6 8 2 9 6 8 2 9 6 7 6 2 2 3 5 1 1 9 9 6 4 9 5 2 8 2 9 5 8 8 4 7 9 5 2 8 8 4 7 8 5 2 9 6 2 8 8 4 7 8 5 2 9 6 2 8 8 4 7 8 5 2 9 6 2 8 8 4 7 8 5 2 9 6 2 8 8 4 7 8 5 2 9 6 2 8 8 4 7 8 5 2 9 6 2 8 8 4 7 8 5 2 9 6 2 8 8 4 7 8 5 2 9 6 2 8 8 4 7 8 5 2 9 6 2 8 8 4 7 8 5 2 9 6 2 8 8 4 7 8 5 2 9 6 2 8 8 4 7 8 5 2 8 8 6 2 9 9 7 2 3 5 8 8 6 2 9 9 7 2 3 5 8 8 6 2 9 9 7 2 3 5 8 8 6 2 9 9 7 2 3 5 8 8 6 2 9 9 7 2 3 5 8 8 6 2 9 9 7 2 3 5 8 8 6 2 9 9 7 2 3 5 8 8 6 2 9 9 7 2 3 5 8 8 6 2 9 9 7 2 3 5 8 8 6 2 9 9 7 2 3 5 8 8 6 2 9 8 6 2 8 6 2 9 8 6 2 8 6 2 9 8 6 2 8 6 2 9 8 6 2 8 6 2 9 8 6 2 8 6 2 9 8 6 2 8 6 2 9 8 6 2 8 6 2 8 8 6 2 9 8 6 2 8 6 2 8 8 6 2 9 8 6 2 8 8 6 2 8 8 6 2 9 8 6 2 8 8 6 2 8 8 6 2 8 8 6 2 8 8 6 2 8 8 6 2 8 8 6 2 8 8 8 6 2 8 8 8 8 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(ly_{i,o}l)$ - Continued

| βm=1,4 | | | | , | |
|---|---|----------------------|--|--|--|
| Хo | $ y_{i,0} $ | z _o = 0.2 | z _o = 0.4 | z _o = 0.6 | z _o = 0.8 |
| 6.0666888888000000000000000000000000000 | 0.5050050505050505050505050505050505050 | 3 | 5 0 0 0 0 0 0 0 0 5 5 6 7 6 6 0 0 0 27 21 18 13 4 5 0 9 7 3 0 0 0 0 0 0 0 0 5 5 6 7 6 6 0 0 0 27 21 18 13 4 5 0 9 7 3 0 0 0 0 0 0 0 0 5 5 6 7 6 6 0 0 0 27 2 1 18 13 4 5 0 0 9 3 5 0 5 2 0 0 0 0 5 7 5 5 2 0 0 0 0 6 9 1 7 6 7 3 3 3 4 0 3 0 0 7 3 3 2 4 0 3 0 0 7 2 2 0 0 0 0 0 7 3 5 5 2 0 0 0 0 7 3 5 3 3 4 0 3 0 0 7 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 | .0000000000000000000000000000000000000 | .0000000000000000000000000000000000000 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $\mbox{ F}_{\nu}(\mbox{Iy}_{i,o}\mbox{I})$ - Continued

 β m = 1.4

| хo | Yi,0 | z _o = 0.2 | z ₀ =0.4 | z _o = 0.6 | z _o = 0.8 |
|--|---|--|--|---|---|
| 0 000000000000000000000000000000000000 | .0050 .0150 | 86705117581867052117588322266699715663991752994000111841 11297657882276188527618850228666997156639917589288957931189765788227688289579756578822768898959715663991788289597158827898959895971588957989895971588957889578 | .196613 .196648 .19749 .1179644 .1179644 .1179644 .1179644 .1189971882 .0077263042010 .0066344000 .0066344000 .006634400 .00796574 .1179988517 .1179988517 .11799880 .11879970 .11879970 .11879970 .1199880 .119980 .119980 .119980 .119980 | 131 4 4 8 13 8 4 8 13 8 4 8 13 8 4 8 13 8 8 13 8 13 | . 0 9 7 3 6 7 . 0 9 9 7 0 1 0 7 9 9 1 7 8 9 1 7 8 9 9 7 1 1 4 8 9 8 7 1 1 1 9 9 7 9 1 1 1 4 8 9 8 9 1 1 1 9 8 9 8 1 1 1 9 8 9 8 1 1 1 9 8 9 8 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(ly_{i,o}l)$ - Continued

βm = 1.4

| | | I | | | |
|--|---|---|--|--|--|
| Хo | Yi,o | z ₀ =0.2 | z _o = 0.4 | z _o = 0.6 | z _o = 0.8 |
| 0.000000000000000000000000000000000000 | .00505050505050505050505050505050505050 | 39744444468733399764454945494594598504989696969696969696969696969696969696969 | .198743291651144291.1199722033444.55162303387066149137445562311709562144993123000065444993123000065444129998789511111111111111111111111111111111 | .1314496 .1324986323 .1129880042 .1129880042 .111068914970 .0098485089 .0098485089 .0098485089 .0098485089 .0098485089 .0098485089 .0098485857 .004665567917 .004665567917 .00446256791 .004418497 .004218497 .004418497 .004418497 .004418497 .004418497 .004418497 .004418497 .004418497 .004418497 .111060997 .004449899 .007881914 .0098487 .004449899 .00782165269 .004449899 .007821111289 .008887 .0044184989 .00444989 .0044884888 .00448848888 .004488888 .004488488 .004888888 .004888888 .00488888 .00488888 .00488888 .00488888 .00488888 .004888888 .004888888 .004888888 .0048888888 .00488888 .00488888 .00488888 .00488888 .00488888 .00488888 .00488888 .00488888 .00488888 .0048888 .00488888 .00488888 .00488888 .00488888 .00488888 .00488888 .00488888 .00488888 .00488888 .00488888 .00488888 .00488888 .00488888 .00488888 .004888888 .0048888 .00488888 .00488888 .00488888 | 09975231631740 099752316332740 09975323631740 09975323650 009995336550 00999988995650 00999988995650 00999988995650 00055510256713266 000555102567132689 0005551025671333889 0005551025671333889 00099999997734568148 0009999999999999999999999999999999999 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(Iy_{i,o}I)$ - Continued

Bm = 1.4

| X ₀ 5.0 5.0 5.0 5.0 5.0 | Yi,o .00 .05 | Z ₀ =0.2 | z ₀ = 0.4 | z _o = 0.6 | z _O = 0.8 |
|---|--|--|---|--|---|
| 5.0 | .00 | 397874 | | | |
| 000000000000000000000000000000000000000 | .150505050505050505050505050505050505050 | .374499 .318297 .318297 .198933 .1252418 .0979342 .065627 .054880 .046471 .039795 .034422 .030044 .0223432 .0234632 .0218766 .0169365 | .198914 .195854 .197212 .174389 .159129 .149302 .1127302 .1127302 .0199450 .0077632 .006122 .006123 .0064699 .0048999 .00361899 .00361899 .00328655 | .132577 .131692 .128993 .124978 .119319 .119319 .1106063 .0991791 .084861 .0782667 .066323 .00518413 .00518422 .044233 .03572996 | . 09 9 38 7 . 09 9 00 0 . 09 78 58 . 09 65 43 . 09 05 48 . 08 71 40 . 08 34 50 . 07 75 52 1 . 07 15 50 0 . 06 36 62 . 05 96 37 9 . 05 30 07 . 04 98 51 . 04 4 4 0 69 . 04 4 9 9 7 3 |
| | | | | | |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(Iy_{i,o}I)$ - Continued

βm=1.6

| Χo | lV: al | z _o = 0.2 | z ₀ =0.4 | 7 -06 | 00 |
|-----|----------------|--|---------------------|--|--|
| . 6 | Yi,o . 0 0 | . 407147 | .000000 | z _o = 0.6 | z _o = 0.8 |
| | | 533401555583440556 5334040556 5334040556 5334040556 533401555583795 53340155522075 53369667555 536967555 536967555 536967555 53696755 53696755 53696755 5369675 | | .0000000000000000000000000000000000000 | .000000 .000000 .000000 .000000 .000000 .000000 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(|y_{i,o}|)$ - Continued

βm = 1.6

| Хo | Yi,0 | z _o =0.2 | z _o = 0.4 | z ₀ = 0.6 | Z _O = 0.8 |
|---|--|--|---|---|--|
| 3 . 5 . 5 . 5 . 5 . 5 . 5 . 5 . 5 . 5 . | 05050505050505050505050505050505050505 | 7970665972850881578460829952995299112771860815760 7970665972152986657747186082129952995293112371860815760 7032689352285088885193354415406660 7032689285193360954718608285193606559725166047770 7032658285193866597251660477094284601156082962962962962111298665972512986659972512986659972512986659972512986659972512986659972512986698698698698698986989898989898989898 | 991094362667759493476889168826622084454569999947710756557654485276282662209876999947688078000554837044882776596445796866220987659644599686622085449846699947656262626262626262626262626262626262626 | 135044993 11344993 11374437 110795061926 109601926 109601926 109601926 109601926 109601926 109601926 1098639428 1098639428 11333345 1130445 1130426 11350426 1101447 1101447 11000664820 11340497 11000664820 11340497 1100066447 1100066447 1100066447 1100066447 1100066447 1100066447 110006647 | ###################################### |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $\mbox{ F}_{\nu}(\mbox{Iy}_{i,o}\mbox{I})$ - Continued

βm=1.6

| ×ο | y _{i,} o | z _o = 0.2 | βm=1.6 z _o =0.4 | z _o = 0.6 | z _o =0.8 |
|--|---|--|---|--|---------------------|
| 4.0 4.0 4.0 4.0 4.0 4.0 4.0 4.0 4.0 4.0 | .05050505050505050505050505050505050505 | .3981650 .37478899 .318899 .1158202 .1158202 .1158202 .1158200 .1158200 .1158200 .115820 .1158 | 199647949 11977949 11977949 1107497194 111008899471 100749789 100749789 100749789 100749789 100749789 100749789 100744771 1008899889 1007449388 1007449388 1008898 1008898 1008898 1008898 1008898 1008898 10088988 1008898 100888 100888 100888 100888 10088 100888 100888 100888 10088 100888 10088 100888 100888 100888 100888 100888 | . 13355 .132557 .129501955 .129501955 .129501955 .129501955 .10998743 .0092742451 .0092742145 .005742461 .005742461 .00531279 .00497555 .004975555 .0049755559 .11356480 .0057484605 .00576935 .1259884605 .0078295 .11936645 .0078295 .0058888605 .00782965 .005888605 .005888605 .00588977 .005888605 .00588977 .0058898605 .00588977 .0058898605 .00588977 .0058898605 .0058896 .0058896 | . 100 51 3 8 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_v(Iy_{i,o}I)$ - Continued

βm = 1,8 $z_0 = 0.8$ Χo yi,o $z_0 = 0.2$ $Z_0 = 0.4$ $z_0 = 0.6$. 6 . 00 .423785 .000000 .000000 000000 . 6 .05 .404127 .000000 .0000000 000000 . 6 .000000 00000 . 8 . 00 .413168 000000 .390462 .05 . 230969 .000000 . 8 .000000 .000000 .15 .282858 .262303 .407744 .000000 .000000 . 8 .000000 .000000 .000000 .215184 .213508 .211724 1.0 .000000 000000 .05 .384571 . 0 .000000 1 . 0 000000 1.0 .000000 .20 .216891 .185798 .215287 1.0 000000 .000000 000000 .000000 .000000 1.0 .000000 .000000 .000000 .381440 .325634 .262761 .208576 .167847 .209209 1 1 1 . 2 .05 .136734 .000000 000000 . 10 .15 . z .000000 1 1 .186509 .000000 .000000 .25 . 2 .141325 .135227 .402927 .379573 .323579 .260282 .2 .000000 .000000 .000000 .143388 .000000 1 1 1 1 .205892 .143151 .05 .000000 .143456 .148077 .175908 . 4 .10 000000 . 4 .186220 .000000 .260282 .205226 .162669 .131779 .111015 .101198 .122482 .401746 .378370 .322295 .186220 .173334 .161889 .156337 .173122 .000000 1 . 4 .20 000000 .30 . 4 .000000 000000 1 . 4 .000000 000000 .40 1.4 .000000 .000000 000000 1.6 1.6 1.6 1.6 1.6 .142168 .142168 .140355 .138079 .136649 .139200 .157938 .203601 .195231 .182959 .168677 .05 .100324 .115484 .15 .258826 000000 .000000 .160305 .128299 .105191 .089233 . 154256 .141429 .000000 .000000 1.6 .131152 .000000 .000000 .45 .080082 .000000 .080082 .082395 .400936 .377548 .321434 .257884 .257884 .158977 .000000 .000000 .141262 .140452 .138155 .134709 .130645 .126750 .000000 .205013 .201996 .193503 .180971 .166202 1.6 .000000 .00 .107047 1.8 .05 $1\overline{5}$ 1.8 .109726 . 20 .25 1 . 8 1 . 8 .150894 .126561 000000 1.8 .102726 .123750 26364 00000 .144213 000000 1.8 . 45 .073083 . 108729 .000000 .000000 .114200 .000000 .000000 .063558 .000000 . 000000 . 60 .000000 .000000 .000000

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(|y_{i,o}|)$ - Continued

βm = 1.8

| | | | βm = 1.8 | 7 | |
|--|---|--|---|---|--|
| ×ο | Yi,0 | z _o =0.2 | Z _O = 0.4 | z _o = 0.6 | z _o =0.8 |
| 00000000000000000000000000000000000000 | .00505050505050505050505050505050505050 | -4768738 -3768827 -22726408 -372786342 -22726408 -11254056 -11254056 -11254056 -108708821 -108708821 -108708821 -108708821 -108708821 -108708821 -108708821 -108708821 -10889988 -3720359995 -1124055998 -115788798 -1157888 -1157 | - 20 38 4 38 5 20 8 5 20 8 | .139816 .138959 .136455 .13278556 .1127349 .11127577 .135285 .1127367 .1107577 .135285 .1112957 .1135285 .1112957 .1135285 .10000000 .00000000 .1386488 .1357214 .131217 .120319 .114249 .11031247 .120319 .114249 .103128 .103128 .103128 .1136119 .1136987 .137887 .0978286 .00900000 .00000000 .135900000 .00000000 .135900000 .00000000 .135900000 .00000000 .00000000 .135900000 .00000000 .00000000 .00000000 .000000 | 1077593 1077593 1077598 1060824 11060824 11072254 1133850 00000000 00000000 00000000 00000000 10068406 11047662 11047662 110477662 110477662 110477662 110477662 110477662 110477662 110477662 110477662 110477662 110477662 110477662 110477662 110477662 11047700 00000000 00000000 00000000 00000000 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{v}(ly_{i,o}l)$ - Continued

Bm = 1.8

| | | | βm = 1.8 | | |
|---|--|---|---|--|---|
| Хo | Y _{i,0} | z ₀ = 0.2 | z _o =0.4 | z _o = 0.6 | z _o = 0.8 |
| 5.55.55.55.55.55.55.55.55.50.0000000000 | 00505050505050505050505050505050505050 | 3990500780078007800912992899026781159876532331778344723 971967128148702115009912992990578111528065547022222222150997655225182727074287299059422200118876552528820655470522222222221522980655470528822222222222152298065547052882222222222222152298065547052222222222222222222222222222222222 | 5 6 8 9 8 4 8 5 5 7 5 8 9 8 4 8 5 5 7 6 8 9 8 4 8 5 5 7 7 8 9 8 4 8 5 5 7 7 8 9 8 4 8 5 5 7 7 8 9 8 5 5 7 7 8 9 8 5 5 7 7 8 9 8 5 5 7 7 8 9 8 5 5 7 7 7 8 9 8 5 5 7 7 7 9 7 8 7 8 7 8 7 8 7 8 7 8 7 8 7 8 | 1354449 137485449 1131485449 1127185499 1127185499 1127185499 1127185499 1127185499 112718598304486 11094578324223 11094578324223 11094578324223 1009873324223 1009873324223 1009873324223 1009873324223 1009873324223 1009873324223 1009873324223 100987332422223 100987332422223 100987332422223 11148098985 1009873324222223 11148098985 100987332422223 11148098985 100987332422223 1114809985 100987332422223 111499869334222223 11149986933422223 11149986933422223 11149986933422223 11149986933422223 111499869334222223 11149986933422223 11149986933422223 11149986933422223 11149986933422223 11149986933422223 11149986933422223 111499869334222223 11149986933422223 11149986933422223 11149986933422223 11149986933422223 11149986933422223 11149986933422223 11149986933422223 111499869334222223 111499869334222223 111499869334222223 111499869334222223 111499869334222223 111499869334222223 111499869334222223 111499869334222223 111499869334222223 111499869334222223 1114998693342222223 111499869334222223 1114998693342222223 1114998693342222223 1114998693342222223 1114998693342222223 11149986933422222222222222222222222222222222222 | 102217609 110313639136 1021736393136 1021736393136 10319396904 10319396904 10319396904 10319396904 10319396904 10319396904 10319396904 10319396904 10319396904 10319396904 10319396904 103193906 10319396904 10319396904 10319396904 10319396904 10319396904 103193999999999999999999999999999999999 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(|y_{i,o}|)$ - Continued

| | | | βm=20_ | | , |
|--|--|--|--|---|---|
| Χo | Yi,o | z _o = 0.2 | z _o = 0.4 | z _o = 0.6 | z ₀ = 0.8 |
| .666888880000000222222222222222222222222 | .00 .010 .010 .010 .0115 .005 .050 .050 | .4448993224343434363364433663364433663366674408324663226666666666666666666666666666666 | .0000000000000000000000000000000000000 | . 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | .0000000 .0000000 .0000000 .0000000 .000000 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(ly_{i,o}l)$ - Continued

βm=2.0

| Хo | y _{1,0} | z ₀ = 0.2 | z _o = 0.4 | z ₀ = 0.6 | z _o = 0.8 |
|----|--|--|--|---|---|
| a | 00505050505050505050505050505050505050 | .4018093 .321804981 .12024981 .12024981 .110243244 .0152374486 .0152472 .01 | .205727 .202694 .11941494 .116651432 .11535201603 .1120 | 143036 1142236 11357488 11351440 11205889 11147820 100000000 100000000 114003368 11283722 100000000 114003402 1136488 11272692 111884645 11023666 110836566 11086666 11086666 11086666 110866666 110866666 1108666666 1108666666 1108666666 11086666666 110866666666666666666666666666666666666 | 1113164 11129355 111273355 11115421 111181109792 1000000000000000000000000000000000000 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(|y_{i,o}|)$ - Continued

| r | | T | βm=2.0 | | |
|---|---|---|---|--|---|
| Χo | Yi,0 | z _o =0.2 | z _o =0.4 | zo= 0.6 | Zo= 0.8 |
| 4 . 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | .00505050505050505050505050505050505050 | .37157688976889768897689897689976897689768976 | . 201576 . 198518 . 198518 . 19708518 . 1159884 . 11618522 . 1135548 . 1024437 . 0908836 . 00585884 . 007224391 . 00452391 . 0045235 . 005057296 . 005055225 . 0041789 . 00505649 . 00505649 . 005056549 . 00505649 . 00506649 . 00506649 | .136728 .133078 .1333078 .12848957 .12848957 .1172397 .1093478 .00893378 .00893378 .0089337 .00721463 .0089337 .0072476 .006398399 .00574797 .0066677 .0066677 .00574997 .0066677 .102241594 .1092816828 .1127947997 .1109328 .0081572947 .1109328 .008157298 .00815728 .0 | .104933 .104536 .10046337 .0943424 .10016247 .099316246 .099631626 .0885950 .0885950 .075243608 .0075243608 .00663477 .006664977 .006664977 .00676394 .006664977 .00774648 .0003202743 .00991745420 .00991745420 .00991745420 .00991745420 .00991745420 .009917441742 .0076275420 .00557550 .005534291 .005575526231 .00993981 .00993981 .00993981 .00993981 .00993981 .00993981 .00993981 .0095534291 .009939885 .009939885 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_v(Iy_{i,o}I)$ - Continued

<u>βm = 2.5</u> $z_0 = 0.4$ z_o= 0.6 $Z_0 = 0.2$ zo= 0.8 Xο y_{i,o} .000000 . 00 .527857 .0000000 .000000 . 8 .05 .596011 .000000 .000000 .0000000 .000000 . 8 . 0.5 .443297 .000000 .0000000 .000000 .10 .15 .412466 .597994 .436178 . H .000000 .000000 .000000 .000000 .000000 1.0 .413916 .05 1.0 .000000 .000000 000000 . 0 . 10 . 000000 . 0 . 15 .313216 .000000 .000000 .000000 .0000000.263929.266584 $\frac{1}{1}$. 20 .314981 .0000000 .000000 .000000 . 0.5 .400499 .000000 000000 .10 .346034 .298005 1 . 2 .000000 .000000 .000000 .000000 . 2 . 20 .240176 . 000000 . 2 . 2 5 .000000 .000000 000000 .243655 .241792 .238218 .00 .416244 .000000 .000000 .416244 .393053 .337655 .275664 .223252 .186368 .170686 .249011 .411735 .388447 .05 .000000 1 . 4 000000 000000 .15 .239948 . 4 000000 000000 .000000 .000000 .25 .000000 .000000 1 . 4 .000000 000000 .000000 .000000 1 .000000 $\frac{1.6}{1.6}$.231145 .228548 .221648 .212816 .206233 .211865 .298997 .05 .193070 .000000 . 6 .332682 .000000 . 0000000 .15 .269851 .215652 .174673 .146947 1.6 .000000 .000000 000000 .25 .000000 1 . 6 .000000 000000 .134070 .000000 .000000 .161588 .000000 .000000 000000 1.6 . 40 .00 1.8 .385384 .220481 .176496 .000000 1.8 .10 .212652 .180470 .000000 .266251 .198670 · s o .189462 368190 1 000000 1.8 . 25 .000000 .000000 1.8 .30 .138381 .176352 .000000 .000000 1.8 .107906 .120473 .406599 .195371 .000000 .000000 .218089 .215157 .206958 1.8 .40 .000000 000000 .000000 . Óú .166305 2.0 2.0 .05 .000000 .327212 5 .10 .165087 000000 .195018 .181301 .167817 .156608 .165240 .169538 .189077 .357336 2.0 . 15 . 000000 2.0 .20 .208598 .000000 .165657 . 0000000 .30 .133980 .000000 .156608 .150342 .157491 .249107 .0000000 .214417 .211435 .203060 .111360 2.0 .000000 . 35 .000000 40 .000000 .088568 .095095 .405050 4 5 5 0 .000000 2.0 .000000 .000000 .000000 .135519 .137491 .150064 2.0 .00 .159180 .381673 . 0.5 2.2 .150064 2.2 .10 2.2 1.5 .262117 .190751 .154185 .20 .151975 .000000 2.2 .163488 .131315 .107846 .091062 .074736 .25 .161631 .151700 2.8 . 0000000 .000000 . 35 .136981 .184555 . 0000000 .000000 .000000 2.2 .45 . 000000 2.2 .131469 000000 .000000 .000000 .000000 .000000 .077588 .000000 . 60 .184820 .000000

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(ly_{i,o}l)$ - Continued

 β m = 2.5

| Хo | y _{i,0} | z ₀ =0.2 | z _o =0.4 | z _o = 0.6 | z _o = 0.8 |
|---|---|--|---|--|---|
| 8.6.6.6.6.6.6.6.6.6.6.0.000000000000000 | . 0 0 1 1 2 2 3 3 4 4 5 0 5 0 5 0 5 0 5 0 5 0 5 0 5 0 5 0 | .40297988336367936883784488899119759728889363369579110848278405299799110775271578888914779597957288933635220330960556781575688293528635220330960556789157568829352863522033096055678915756882950688200688295068829506882950688295068829506882950688295068829506882950 | 2209445340880304879006155779070885311004756800 - 2198756004880304880308887990844888030888755758740832574083257460 - 219875600488853408887758879086469877558740832574986646888775587758740832574986646977787110098769887799088877978787878787878787878787878 | .154441 .14471441 .14471441 .14471441 .143445 .133884637 .12252166 .1236216 .1236216 .1236216 .1247216 .1236216 .000000000 .1445966 .124727 .1377968 .12788772 .1141977 .1132788772 .1132788772 .1132788772 .11341428 .11044448 .11044916 .10049916 .10040000000 .1441678 .110948761 .11094986 .11094986 .11094986 .11094986 .11094986 .11094986 .11094986 .11094986 .11094986 .11094986 .110998755 .11109986 .1109986 .109986 .109986 .00908 | 128349 112899544 1128995543 112873280000000000000000000000000000000000 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(ly_{i,o}l)$ - Continued

 β m = 2.5

| Хo | у _{і,} о | z _o = 0.2 | βm = 2.5 z _o = 0.4 | z ₀ =0.6 | Z _O = 0.8 |
|--|---|---|---|--|---|
| 4.0 4.0 4.0 4.0 4.0 4.0 4.0 4.0 | .05 0.10 1.10 1.20 1.20 1.20 1.20 1.20 1.20 | .400017 .376014 .320449 .2568117 .1574747 .115746220 .00819247 .00819247 .00819247 .00819247 .00819247 .00819247 .00819247 .00819247 .00819247 .008193189 .008193189 .008193189 .00823189 .00823189 .0082318443 .00823189 .00823189 .00823189 .00823189 .00823189 .00823189 .00823189 .00823189 .00823189 .00823189 .00823189 .00823189 .00823189 .00823189 .00823189 .00823189 .00823189 .008473 .0082879 .00829 .00829 .00829 .00829 .00829 .00829 .00829 .00829 .00829 .00829 .00829 | .203344 .191844 .103844 .10379712 .110789914 .1032237991 .00364500 .00364500 .004454 .0044443 .0044443 .0044443 .004771 .11305598 .0071 | . 13 9 4 1 9 . 13 8 5 1 4 . 13 1 7 0 7 . 12 6 3 0 7 5 5 . 13 1 7 2 4 . 12 3 3 5 5 5 . 09 9 4 8 5 5 . 09 7 1 5 6 5 . 09 7 1 5 6 5 . 09 7 1 5 6 5 . 00 6 2 5 9 8 6 . 00 6 2 5 9 8 6 . 00 6 2 5 9 8 . 12 9 5 6 6 8 6 . 13 3 6 9 9 8 . 12 9 6 8 4 9 1 . 10 6 1 6 8 6 7 . 12 9 6 8 4 9 1 . 10 1 3 3 3 9 8 . 12 9 6 8 4 9 1 . 10 1 3 6 9 5 9 7 . 12 9 6 8 4 9 1 . 10 1 3 6 9 5 9 7 . 12 9 6 8 6 9 5 . 12 9 6 8 6 9 5 . 12 9 6 8 6 9 5 . 13 3 6 9 5 7 . 12 9 6 8 6 9 5 . 12 9 6 8 6 8 6 7 . 12 9 6 8 6 8 7 . 12 9 6 8 6 8 6 7 . 12 9 6 8 6 8 7 . 12 9 6 8 6 8 6 7 . 12 9 6 8 6 8 7 . 12 9 6 8 8 9 9 8 . 12 9 7 8 8 8 9 9 8 . 12 9 8 9 8 9 8 | .109044 .100673 .1007818 .1007818 .1007818 .10078120 .0977509 .0977509 .0977509 .0977509 .097752661 .0778271 .0778271 .078814550 .0000323 .10049814 .10199628664 .099628664 .0996628664 .099896664 .09989628664 .09989628664 .098818669 .098818669 .098818669 .098818669 .098818669 .098818669 .098818680 .098818680 .098818680 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(ly_{i,o}l)$ - Continued

 β m = 3.0

| | | | βm = 3.0 | | |
|---|--|--|--|---|---|
| Хo | y _{i,o} | z _o =0.2 | z ₀ = 0.4 | z _o = 0.6 | z _o = 0.8 |
| 8 8 8 9 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | 00500505050505050505050505050505050505 | 533773884553788415992533982228838733935985518195560 521618992499253598445945317079447723073598429944953170794495315799966683372288387340835456118255667 5216189944559470166433885546153916615888249944953170799967228388554667 5216189471075671707661707660 521618947107661796660 52161894717001707996668377285117456118567728511744582893777660 52161894717851178511785117851178511785117851178 | .0000000000000000000000000000000000000 | . 0 0 0 6 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | . 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $\mbox{ Fv(ly}_{i,o}{\mbox{\scriptsize I}})$ - Continued

βm= 3.0

| хо | Уі , о | z ₀=0.2 | z ₀ =0.4 | z _o =0.6 | z ₀ =08 |
|--|--|--|---|---|--|
| 3.0 3.0 3.0 3.0 3.0 3.0 3.0 3.0 | .050 .0150 .1205 .2305 .3405 | .404221 .384714 .2832 .3247151 .2051599 .1029551 .10295561 .0877998 .0658684 .055824512 .0746186 .055824512 .3729350 .20601770 .10850799 .0402512 .3729350 .20601770 .1085079 .047470 .1085079 .047470 .1085079 .047470 .1085079 .047470 .1085079 .047470 .1085079 .047470 .1085079 .047470 .1085079 .0443409 .05335682 .158618018 .0697851 .1083980 .033389 .033389 .033338 | .212567 .2095445 .20910445 .10910471 .11784608 .11784608 .1178475 .110922614 .110922614 .110922614 .110922614 .110922614 .11108429 .100006991 .2096076 .118492461 .1138991 .00849445 .007684842 .1113771 .00849445 .007684842 .11135910 .00849445 .00768482 .11135910 .0086961 .1207682 .00966961 .1207682 .009669680 .0078247 .0086968680 .0078247 .0086968680 .0066273297 .00664445 .008696800 .0086968000 .008696800000000000000000000000000000000 | .1562884 .152884 .149883 .1449883 .1449883 .135750 .1351948 .1351948 .13519466 .161896 .00000000 .00000000 .148733 .1418335 .136488 .11418385 .1184986 .1124386 .11244649 .1049877 .254449 .100798 .1144338 .11244649 .1049877 .2546449 .109986 .11449877 .2546449 .109986 .11449877 .2546449 .109986 .112856 .112856 .112856 .112856 .1128576 .112856 .113156 | .138440 .138451 .139454 .142328 .150177 .0000000 .0000000 .0000000 .0000000 .0000000 .0000000 .124394 .123289 .123289 .120608 .119183 .118189 .1273399 .1273399 .1273399 .1273399 .1273400 .0000000 .0000000 .0000000 .0000000 .1146680 .115958 .114069 .1114069 .1114069 .11152900 .1098851 .1098851 .0998851 .0998851 .0998851 .0998851 .0998851 .0998851 .0998851 .0998851 .0998851 .0998851 .0998851 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(ly_{i,o}l)$ - Continued

<u>βm = 3.0</u> $z_0 = 0.2$ x_{o} z₀= 0.4 z₀= 0.8 |Yi,0| $z_0 = 0.6$ 5.0 .00 .400134 .376731 .32055 .256914 .201226 .157578 .1100312 .081993 .058102 .057419 .042508 .037251 .033251 .022582 .024582 .024582 .022756 .021414 .020502 .400134 .109738 .203551 .139847 .05 .10 .15 .203551 .200495 .191867 .179066 .163640 .147794 .132120 .117552 .104447 5.0 5.0 5.0 .138940 .136294 .132118 .126718 .109363 .106480 .104110 .104253 .098027 .094555 .067316 .063767 .0772277 .074218 .0772218 .070529 .07988 .07988 .07988 .07988 .07988 .07988 .07988 .07988 .07988 .07988 .07988 5.0 .126718 .120446 .113650 .106644 .099684 .25 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 .40 .45 .55 .60 .65 .70 .75 .85 .90 .95 .092907 .082884 .074253 .066865 .060568 .086625 .080754 .075408 .070621 .006413 .002811 .059852 .057615 .056258 .056111 .057950 .0505223 .050729 .046985 .043939 .041573 5.0 5.0 .039151 .102054

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $\mbox{ Fv}(\mbox{Iy}_{i,\,o}\mbox{I})$ - Continued

 β m = 3.5

| хо | Yi,0 | z ₀ = 0.2 | βm = 3.5 z ₀ =0.4 | z _o = 0.6 | z ₀ = 0.8 |
|---|---|---|--|---|----------------------|
| . 8 8 0 0 0 0 2 2 2 2 2 4 4 4 4 4 4 4 6 6 6 6 6 6 6 6 | 0 5 0 5 0 0 5 0 5 0 5 0 5 0 5 0 5 0 5 0 | .64 84 55 36 76 10 9 5 3 3 9 0 4 5 5 15 6 8 6 7 1 8 8 7 7 9 8 2 8 7 8 2 7 8 2 8 7 8 2 8 7 8 2 8 7 8 2 8 7 8 2 8 7 8 2 8 7 8 2 8 2 | 00000000000000000000000000000000000000 | .0000000 .0000000 .0000000 .0000000 .000000 | |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(|y_{i,o}|)$ - Continued

 β m = 3.5 z_o = 0.2 Xο $|y_{i,o}|$ $Z_0 = 0.4$ zo= 0.6 Zo= 0.8 00 . 0 .172211 .171570 .169841 .167510 .219941 .2169616 .208616 .196334 .181951 .153491 .14337962 .131115 .140768 .220535 3.0 .05 .383895 .363693 .327826 .264354 .208949 .165720 .133512 182335 .10 . 0 303496 3.0 .165390 .164866 .168754 .185230 .266436 3.0 000000 .30 .109947 .092936 .081967 .073762 .071973 .083402 .404716 .381327 .325208 .261642 .206085 000000 .0 .40 .45 .50 000000 00000 . 0 .000000 .000000 .000000 .158508 .157693 .155349 .151743 .147267 .142408 .137746 .134599 .147005 .134599 .147005 .134599 .147005 000000 .220535 .0000000 .213742 .210723 .202216 .189636 .174756 .159217 .144264 .130713 .119057 .109633 .102847 .102429 .123618 . 0 000000 .60 3 3 .000000 . 5 0.5 .144739 .144828 .145531 .147788 . 5 .10 3.53.53.53.55 . 2.0 . 2.5 . 3.0 .206085 .162625 .130070 .105982 .0881661 .059268 .0584210 .053265 .059216 .059216 .32583 .403084 .373546 .153654 .000000 . 40 3.5 3.5 .50 .000000 .60 .65 .70 .000000 .5 .000000 .000000 .000000 .000000 .000000 .151138 .150270 .147751 .1438071 .133027 .126980 .121021 .115535 .1107743 .1106854 .1106854 .1244441 .199594 .000000 .000000 .00 .129158 4 . 0 .05 . 0 .128884 .128113 .126967 .125633 .124379 .123604 .123941 .126565 .134178 .155688 .323546 .198376 .0 .15 . 185680 . 170614 . 154797 . 139438 .204315 . 25 .0 .160759 .128066 .103783 .085684 .072084 .061791 .053992 .048157 .043992 . 0 .125296 . 0 4.0 .112765 .102002 .093049 .085932 .080779 .078009 .078892 . 0 4 5 0 5 5 . 0 . ŏ 266716 .60 .65 .70 . 0 .000000 .0 .041460 .040992 .044566 .067996 .401190 .377789 .321628 .257987 .000000 .000000 .00000 .143633 .142733 .140112 .135980 .130646 .124465 000000 .0 80 .148016 .000000 .205804 .202752 .194136 .181358 000000 .000000 .000000 .115747 .115387 .114332 .112641 .110407 . H 5 .00 . 0 05 .15 . 0 .181358 .166166 .150166 .134554 .120066 .107063 .095652 .085793 .077373 .202314 .158686 .125895 .101479 .0832047 .059752 .050507 .044036 .034870 .031685 .029242 . 0 .107742 .104780 .101659 .098526 .095535 .092853 .090680 . 0 3 5 .11094 .110948 .104198 .097750 .091763 .086355 .081627 .077682 .074663 4 0 4 5 . 0 5 0 5 5 5 . 0 6 0 6 5 7 0 7 5 . 0 064317 059455 055617 .089122 5 . 0 . 0 5.0 5.0 5.0 5.0 .75 .80 .85 .90 .0969 .052823 .072633 .113443 .051224 .051262 .054234 .065376 .027491 . 19446 .084400 .000000 .026418 .121305 000000 .000000

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_v(|y_{i,o}|)$ - Continued

βm = 4.0 $z_0 = 0.4$ z₀= 0.6 z_o=0.8 $z_0 = 0.2$ Χo $|y_{i,o}|$ 596831 000000 000000 1.0 000000 .000000 606590 . 0.5 1.0 1.870071 .10 000000 000000 000000 $\frac{1}{1} \cdot \frac{2}{0}$.000000 .000000 .000000 .491176 .466934 .630983 .470583 .05 1.2 .000000 000000 1.2 . 000000 .000000 .000000 .000000 .000000 000000 1.4 . 0.5 .449434 000000 .402657 .367461 .468103 . 000000 . 10 000000 .000000 .000000 000000 1.4 . 15 .000000 1.4 . 50 .000000 .000000 .450064 427726 .375608 .321883 .292468 .38888 .437437 .414614 .301540 .2557301 .353278 .429023 .05 .000000 1.6 000000 .000000 000000 . 6 .000000 1 .000000 .000000 1.6 000000 . 20 1.6 .000000 1.6 1.8 1.8 1.8 .000000 .000000 .000000 .00 .000000 000000 .000000 .468723 .000000 .000000 .15 000000 .000000 .000000 1.8 1.8 2.0 . 25 .000000 .000000 .000000 .000000 .00 .429023 .405967 .351013 .289895 .239067 .205261 .197443 .298438 .303295 .335913 .935035 .05 .000000 .000000 2.0 5.0 .000000 000000 .20 .000000 . ŏ .000000 .000000 .000000 2.0 . ŏ .000000 .000000 .000000 2.0 .364760 .423099 .399917 .344506 .282375 .229420 .190711 .16723 .270851 .00 .000000 .000000 2.2 3.3 .000000 .000000 .264466 2.2 .15 .000000 .000000 .25 2.2 .000000 .000000 .000000 5 . z .168954 .000000 .000000 .000000 .000000 .562297 .415459 .3925459 .336333 .218745 .176860 .146926 .119356 .11935721 .387522 .368210 . 2 2.6 .00 .243132 000000 .000000 .233214 .311024 2 .6 .15 .213180 .000000 .000000 2 . 6 .25 .212198 .000000 . 6 .000000 .000000 .6 . 35 2 4 0 000000 000000 .000000 .0000000 .0000000.229483.226597.218539 2.6 .45 .000000 .05 . 0 . 198877 . 199335 . 202197 . 212207 . 246981 .000000 - 0 .268210 .213050 .170204 .206834 . 000000 .000000 . 0 .180375 . 000000 .138592 .115985 .100620 . 000000 .30 . () .163600 .000000 . 000000 3.0 .000000 .000000 3.0 . 40 .000000 .000000 3.0 .50 .092452 .000000 .128012 .000000 .000000 . 000000

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(ly_{i,o}l)$ - Continued

| | 1 | | β m = 4.0 | | |
|---|---|--|---|---|---|
| Хo | y _i ,o | z _o = 0.2 | z _o = 0.4 | z _o = 0.6 | z _o =0.8 |
| 3.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5 | .00 .115050505050505050505050505050505050505 | . 4073048 .3839448 .32648354 .2648354 .1653294 .092311 .0929493 .00716421 .009403485 .4051629 .009403485 .4051629 .260649348 .10629408 .110629408 .110629408 .110629408 .110629408 .110629408 .110629408 .110629408 .110629408 .110629408 .110629408 .110629408 .110629408 .110629408 .110629408 .110629408 .110629408 .110623986 .110629408 .11062948 .1106 | 220051 .217086342 .19868428 .1981848 .1507567 .13154368 .14627567 .13254348 .144687 .4570001 .2144983 .126382 .129293 .1293939 .129393 .129393 .12939 .12939 .129393 .129393 .129393 | . 172639 . 171958 . 170973 . 167381 . 162434 . 1624752 . 1689441 . 192312 . 0000000 . 0000000 . 0000000 . 160156 . 1593491 . 153367 . 1439974 . 13322544 . 13322544 . 13322544 . 13322544 . 1332256 . 1440785 . 144078 . 1447945 . 1449893 . 123227 . 11695581 . 129227 . 11695581 . 1099581 . 1099581 . 099581 . 099581 . 099581 . 099581 . 099699 . 099261 . 0000000 . 00000000 . 000000000000000 | . 18 6 2 6 0 . 18 8 2 1 5 . 19 7 6 5 8 . 23 2 9 3 0 1 . 5 2 7 9 5 8 . 23 2 9 3 0 . 0000000 . 00000000 . 00000000 . 00000000 . 00000000 . 00000000 . 14 9 2 1 9 . 14 9 7 8 6 . 15 16 3 9 1 . 16 7 9 5 6 . 20 0 7 8 8 . 46 7 5 1 8 . 0000000 . 0000000 . 0000000 . 0000000 . 0000000 . 12 4 0 7 7 . 12 2 8 0 3 . 12 13 3 1 4 . 11 1 7 1 7 6 . 10 9 8 5 8 . 11 0 8 7 6 . 10 9 8 5 8 . 11 0 8 7 6 . 10 9 8 5 8 . 11 0 8 7 6 . 10 9 8 5 8 . 11 0 8 7 6 . 10 9 8 5 8 . 11 0 8 7 6 . 10 9 8 5 8 . 11 0 8 7 6 . 10 9 8 5 8 . 11 0 8 7 6 . 10 9 8 5 8 . 11 0 8 7 6 . 10 9 8 5 8 . 11 0 8 7 6 . 10 9 8 5 8 . 11 0 8 7 6 . 10 9 0 0 0 0 0 . 0000000 . 0000000 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION Fv(Iyi, oI) - Continued

 β m = 4.5 $z_0 = 0.8$ $z_0 = 0.6$ $Z_0 = 0.4$ $z_0 = 0.2$ y_{i,0} Хo .000000 .000000 .000000 .754066 .00 1.0 000000 1.074833 00000005 $\begin{array}{c} \mathbf{1} \cdot \mathbf{0} \\ \mathbf{1} \cdot \mathbf{2} \end{array}$ 000000 000000 .00 000000 .000000 .000000 .558090 1 . 2 1 . 2 1 . 4 1 . 4 .05 000000 U U U U U U620842 .000000 .501984 .000000 .0000000 000000 . 000000 .483250 . 05 .000000 .448708 .000000 .10 . 4 . 000000 . 0000000 .478950 . 900000 . 4 000000 1.4 .0000000 .0000000 . 0.0 . 0000000 .449105 .000000 . 05 1.5 .000000 . 6000000 . 10 . ບບບບບົດບົ .401035 .360009 .394555 .452000 .429649 .377403 .000000 1.6 . 1 5 .000000 . 8888888 1.8 . 20 .000000 . 0000000 .000000 υαυσου. .05 1.8 . 000000 . טטטטטטט 1.8 . 10 .000000323083 .0000000 1.8 . 15 . 5000000 .000000 . 0000000 .20000000 .000000 1.8 .346432 .000000 .0000000 .440031 .417238 \$.0 8.0 .00 .537448 .000000005 . 000000 .000000 2.0 .363255 $0 \ 0 \ 0 \ 0 \ 0 \ 0$.000000 • 0 .15 .20 .258708 .239739 .0000000 . 000000 2.0 . 600000 .000000 .000000 .25 .000000 . 0000000 .334648 .431759 .408738 .353900 .314558 .315364 .323909 .372978 .0000000 .000000 2.2 .00 . 000000 2.2 .05 . 000000 .293006 .242577 $\frac{1}{5}$ 2.2 . 000000 .000000 .0000000 3.2 . 20 209542 .0000000 . 0000000 .009000 3.2 .25 .30 .350000000 .000000 .402709 .0000000 .000000 :8888888 2.2 2.6 .00 .0000000 . 000000 .261519 .398046 .05 .000000 . 0000000 .342465 000000 .0000000 .250095 . 15 2.5 .226238 .185932 .159080 .146913 .166179 .0000000 . 0000000 . 20 .0000000 .269809 2.6 .25 .0000000 . 0000000 . 000000 .000000 .0000000 .35 .0000000 0040000 .0000000 3 .6 .000000 .00 . 254636 . 272095 . 358294 .000000 .239238 .391750 . 05 3 . 0 . 0 . 10 000000 .221211 .272806 . 0 . 15 .000000 . 209988 .000000 .218042 . 0 .20 .000000 000000 .200990 .25 . 0 . 000000 . 0 .145304 . 000000 .124606 .815806 .0 .000000 . 000000 .113114 .000000 4.5 5.0 . 0 .000000 .194328 .194004 .193406 .000000 .183571 . 0 .227925 .410298 . 5 0.0 . 0000000 .330922 . 0.5 3.5 3.5 3.5 3.5 .204891 .000000 . 10 .19356U .196534 . 0000000 .267542 . 15 .191064 .237342 .212281 .169257 .137376 .114289 .098035 .000000 . ão . 000000 . 206599 . 25 . 000000 .104911 .241363 30 .000000 .155813 3.5 3.5 000000 3.5 000000 .161066 .000000 .087472 3.5 .45 .000000 . 0000000 .082810 . 000000 .000000 .0000000 5.5 .0000000 . 000000 .60 .169767 .000000

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(ly_{i,o}l)$ - Continued

 β m = 4.5

| | | · · · · · · · · · · · · · · · · · · · | <i>β</i> m = 4.5 | | |
|---|--|--|--|--|---|
| Хo | Yi,o | z _o = 0.2 | z ₀ = 0.4 | z ₀ =0.6 | z _o = 0.8 |
| 4.0 4.0 4.0 4.0 4.0 4.0 4.0 4.0 4.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5 | .00 .0150 .1150 .330 .3450 .330 .450 .660 .700 .1150 .330 .340 .550 .660 .770 .885 .885 .885 .885 .885 .885 .885 .88 | .407286 .387821 .2083149 .12648520 .11331515 .10918377 .00792437 .0079242 .00719835 .20384293 .20631985 .324429 .206158489 .110454797 .006259933 .00648793 .00648793 .0044315 .0044315 .0044315 | . 220015 . 217027 . 20827 . 196227 . 1865148 . 1521889 . 129351 . 129399 . 1265124 . 000000 . 2186849 . 1000000 . 2186849 . 2000000 . 2186849 . 1273563 . 147115 . 114612 . 1034930 . 00779516 . 07796037 . 11450 | . 172624 . 1771917 . 169934 . 167926 . 163732 . 160821 . 159441 . 161657 . 17239 . 213176 . 0000000 . 0000000 . 0000000 . 0000000 . 1544440 . 153579 . 151081 . 147173 . 142184 . 1365027 . 124652 . 1114734 . 111586 . 113457 . 124938 . 1705030 . 0000000 . 00000000 . 0000000000000 | . 188516 .189782 .195311 .211455 .268721 .000000 .000000 .000000 .000000 .000000 |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $\mbox{ Fv}(\mbox{Iy}_{i,\,o}\mbox{I})$ - Continued

 β m = 5.0

| Хo | Yi,o | z ₀ =0.2 | βm = 5.0 z _o = 0.4 | z _o = 0.6 | z ₀ =0.8 |
|--|--|--|--|---|---------------------|
| 1.2 | .00 | .659822 | .000000 | .000000 | .000000 |
| 1.44446666888BBBB0000000000000000000000000 | .05 .00 .00 .00 .00 .00 .00 .00 .00 .00 | 6895788 5545788 5545788 55324456 49763776 44370884 44785956 44780559 447855339 447855339 445310889 445310899 445310899 445310899 445310899 4465444 466107012 47836 478 | . 0000000 .000000 .000000 .000000 .000000 .000000 | .0000000 .0000000 .0000000 .0000000 .000000 | |

TABLE IV - TABULATION OF THE SIDEWASH FUNCTION $F_{\nu}(Iy_{i,o}I)$ - Continued

<u>βm = 5.0</u> x_{o} z₀=0.4 $z_0 = 0.2$ y,0 z_o= 0.6 $z_0 = 0.8$.405416 .382028 .325907 .206770 .2067770 .103292 .130706 .106565 .075312 .065374 5.0 .00 .215424 .154780 5.0 5.0 5.0 .05.10 .10.15 .20.25 .30.35 .40.45 .55.5 .605 .75.80 .154780 .154733 .154736 .155130 .156516 .ih0018 .168051 .187338 .212405 .203893 .191301 .176393 .160799 .145748 .132028 .120079 .110139 .102392 .097155 .095228 .0995228 .12000000 5.0 5.0 5.0 5.0 5.0 5.0 .000000 5.0 5.0 5.0 5.0 5.0 .058085 .053025 .050150 .050104 . 000000 . 000000 .000000 .056026 .000000 .0000000

TABLE IV.- TABULATION OF THE SIDEWASH FUNCTION $F_{\mathbf{v}}(|\mathbf{y}_{1,o}|)$ - Continued

 $m = \infty$

| , | | | | | | | | | | | |
|----------|------------------|----------------------|----------------------|----------------------|--------------------|------------|------------------|-----------------------------|----------------------|----------------------|----------------------|
| - | y _{i,0} | z _o = 0.2 | z _o = 0.4 | z _o = 0.6 | $z_0 = 0.8$ | x | y _{1,0} | z _o = 0.2 | z _o = 0.4 | z _o = 0.6 | z _o = 0.8 |
| 0.6 | 0 | 0.422023 | 0.266911 | 0 | 0 | 1.4 | 0 | 0.402011 | 0.207597 | 0.146794 | 0.121211 |
| .6 | .05 | 398759 | .264463 | 0 | 0 | 1.4 | .05 | .378610 | .204546 | 145895 | .120854 .119801 |
| .6 | .10 | .343021 | .257736 | 0 | 0 | 1.4 | .10 | .322450 .258808 | .195931 .183152 | .143275 .139140 | .119001 |
| .6 | .15 | .280123 | .248393 | 0 | 0 | 1.4 | .15 .20 | .203132 | .167955 | .133797 | .115850 |
| .6 | .20 | .225581 | .238732 .231483 | 0 | 0 | 1.4 | .25 | .159500 | .151945 | 127595 | .113098 |
| .6 | .25 .30 | .183594 .153167 | .230393 | ő | ŏ | 1.4 | .30 | .126701 | .136314 | .120884 | .110086 |
| .6 | .35 | .132231 | .242847 | ő | ő | 1.4 | •35 | .102273 | 121795 | .113975 | .106815 |
| .6 | .40 | .119366 | 298415 | 0 | 0 | 1.4 | .40 | .083977 | .108744 | .107124 | .103440 |
| .6 | .45 | .114879 | 0 | 0 | 0 | 1.4 | .45 | .070112 | .097263 | .100524 | .100072 |
| .6 | .50 | .124458 | 0 | 0 | 0 | 1.4 | •50 | 059455 | .087303 | .094313 | .096811 .093747 |
| .6 | •55 | .210762 | 0 | 0 | 0 | 1.4 | •55 | .051152 .04 4 599 | .078230 .071416 | .088579 .083373 | .090965 |
| | | 1.2076 | .229720 | .200516 | 0 | 1.4 | .60 .65 | .039369 | .065183 | .078724 | .088545 |
| .8 .8 | .05 | .410936 .387572 | .226778 | .199727 | 0 | 1.4 | .70 | .035156 | .059900 | .074643 | .086575 |
| .8 | .10 | •331523 | 218495 | 198677 | ŏ | 1.4 | •75 | .031741 | .055446 | .071139 | .085159 |
| .8 | .15 | .268074 | .206292 | .196794 | 0 | 1.4 | .80 | •028962 | .051720 | 068223 | .084439 |
| .8 | .20 | .212680 | .191948 | 194924 | 0 | 1.4 | .85 | .026704 | .048647 | 065920 | .084657 |
| .8 | .25 | .169433 | .177126 | . 193854 | 0 | 1.4 | .90 | .024881 | .046173 | .064279 | .086071 .089424 |
| .8 | .30 | .137146 | .163105 | 194734 | 0 | 1.4 | 1.95 | .023437 | .044272 | .063397 .063453 | .096070 |
| 8. | •35 | 113389 | .150759 | +199477 | 0 | 1.4 | 1.00 | .022337 | .042951 | , | 10,000,0 |
| .8 | .40 .45 | .095974 .083278 | .140674 .133352 | .212050 .243926 | 0 | 1.6 | ١ ، | .401033 | .205468 | .143070 | .114860 |
| 8.8 | .50 | .005270 | 129507 | .361527 | ő | 1.6 | .05 | .377630 | .202413 | .142164 | .114488 |
| .8 | -55 | 068156 | .130686 | 0 | 0 | 1.6 | .10 | .321465 | .193786 | .139520 | .113389 |
| .8 | .60 | .064975 | .141366 | 0 | 0 | 1.6 | .15 | .257815 | .180987 | .135348 | .111615 |
| .8 | .65 | .065343 | .182310 | 0 | 0 | 1.6 | .20 | .202127 | .165762 | 129949 | .109248 |
| .8 | .70 | 075969 | 0 | 0 | 0 | 1.6 | .25 | .158478 | .149715 | .123675 | .106387 |
| .8 | •75 | .109128 | 0 | 0 | 0 | 1.6 | •30 | .125659 .101206 | .134037 .119460 | .109848 | .099638 |
| ١,, | | 1.06000 | 013066 | .165786 | 0.165786 | 1.6 1.6 | •35 •40 | .082881 | .106340 | 102859 | .095974 |
| 1.0 | .05 | .406092 .382703 | .217065 .214045 | 164966 | .165718 | 1.6 | .45 | .068979 | .094776 | .096094 | .092253 |
| 1.0 | .10 | .326579 | 205524 | .162581 | .165551 | 1.6 | .50 | .058281 | .084716 | .089684 | 088563 |
| 1.0 | .15 | 262999 | 192905 | 158852 | .165408 | 1.6 | •55 | 049928 | .076034 | .083712 | .084976 |
| 1.0 | .20 | .207413 | .177941 | .154101 | .165499 | 1.6 | .60 | .042738 | .068573 | .078220 | .081553 |
| 1.0 | .25 | .163900 | .162244 | .148709 | .166146 | 1.6 | .65 | .038017 | .062175 | .073227 | .078341 |
| 1.0 | •30 | .131255 | .147021 | .143070 | .167832 | 1.6 1.6 | .70 | .033722 | .052002 | .064715 | .072702 |
| 1.0 | •35 | .107022 | .133021 | •137559 | .171320 .177941 | 1.6 | .80 | .027312 | .047987 | .061164 | .070337 |
| 1.0 | .40 .45 | .088970 | .120627 | .132531 .128330 | .190401 | 1.6 | .85 | .024910 | .044558 | .058059 | .068317 |
| 1.0 | .50 | .065132 | .101074 | 125337 | .215672 | 1.6 | .90 | .022910 | .041639 | .055335 | .066676 |
| 1.0 | .55 | .057308 | .093875 | .124056 | .281686 | 1.6 | 95 | .021244 | .039170 | .053122 | .065465 |
| 1.0 | .60 | 051367 | .088354 | .125323 | 0 | 1.6 | 1.00 | .019860 | .037106 | .051278 | .064753 |
| 1.0 | .65 | .046937 | .084604 | .130836 | 0 | | _ | .400366 | .204046 | .140674 | .111042 |
| 1.0 | -70 | .043802 | .082776 | .145036 | 0 | 1.8 | .05 | .376963 | 200988 | .139765 | .110663 |
| 1.0 | •75 •80 | .041898 | .083634 .088970 | 185919 | 0 | 1.8 | .10 | 320795 | .192355 | .137111 | 109544 |
| 1.0 | .85 | .041375 .042830 | .105224 | 0 | l ŏ | 1.8 | .15 | 257140 | .179546 | .132920 | .107738 |
| 1.0 | .90 | 048345 | 189460 | o | ō | 1.8 | .20 | .201446 | 164307 | .127495 | .105323 |
| 1.0 | •95 | .070421 | 0 | 0 | 0 | 1.8 | -25 | •157789 | .148241 | .121187 | .102401 |
| | 1 | | i | | | 1.8 | .30 | .124959 | .132540 | .114340 | .099082 .095479 |
| 1.2 | 0 | .403531 | .211012 | .153147 | •133455 | 1.8 | •35 •40 | .100494 | .104781 | 100213 | .091700 |
| 1.2 | .05 | .380134 | .207968 | 152267 | .133144 .132231 | 1.8 | .45 | .068234 | .093177 | .093374 | 087842 |
| 1.2 | .10 | •323984 960361 | .199380 .186644 | .149702 .145664 | .130775 | 1.8 | .50 | .057515 | .083070 | .086877 | 083990 |
| 1.2 | .15 | .260361 | .171510 | .140458 | .128868 | 1.8 | .55 | .049138 | .074333 | .080803 | .080213 |
| 1.2 | .25 | .161113 | 155585 | 134440 | .126629 | 1.8 | .60 | .042498 | .066809 | .075194 | .076565 |
| 1.2 | .30 | .128358 | .140061 | .127965 | .124197 | 1.8 | .65 | .037167 | .060338 | .070062 | .073088 |
| 1.2 | • 35 | .103984 | .125676 | .121355 | .121721 | 1.8 | .70 | .032835 | .054772 | .065403 | .069812 .066760 |
| 1.2 | .40 | .085755 | .112790 | .114875 | .119366 | 1.8 | •75 | .029278 | .049980 | .057424 | .063946 |
| 1.2 | •45 | .071970 | .101511 | .108737 | 117307 | 1.8 | .80 .85 | .026335 | 042285 | .054052 | .061380 |
| 1.2 | •50 | .061412 | .091797 | .103099 | .115742 .114917 | 1.8 | 1 :90 | .021801 | 039205 | .051056 | .059069 |
| 1.2 | •55 •60 | .053228 .046819 | .076583 | .093783 | ,115169 | 1.8 | 95 | .020053 | .036544 | .048409 | .057019 |
| 1.2 | .65 | .041767 | .070814 | .090301 | .117024 | 1.8 | 1.00 | .018572 | .034248 | .046089 | .055239 |
| 1.2 | .70 | .037775 | .066116 | .087756 | .121423 | II | 1 | 1 | 1 | | i |
| 1.2 | 75 | .034638 | .062414 | .086338 | .130360 | I | 1 | | 1 | | 1 |
| 1.2 | .80 | .032217 | .059683 | .086377 | .149208 | 1 | | | | | |
| 1.2 | .85 | .030430 | .057969 | .088523 | .201407 | 1 | 1 | | | | |
| 1.2 | .90 | .029252 | .057440 | .094244 | 0 | | | | 1 | 1 | 1 |
| 1.2 | 1.00 | .028729 | .058512 | .107/19 | 0 | 1 | 1 | 1 | 1 | l | |
| | 1.00 | 1 | .002229 | 1 | <u> </u> | 1 | 1 | 1 | <u> </u> | | l |
| | | | • | | • | | | | | | |

TABLE IV.- TABULATION OF THE SIDEWASH FUNCTION $\mathbf{F_v}(|\mathbf{y_{i,o}}|)$ - Concluded

m = w

| ī | lv. I | z. = 0.2 | z. = 0.4 | z. = 0.6 | z_ = 0.8 | ş | lv. I | z = 0.2 | z = 0.4 | 2 = 0.6 | 2 = 0 B |
|--|---|--|--|---|---|---|---|--|--|---|---|
| 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 | 0 .05 .10 .20 .20 .20 .20 .20 .20 .20 .20 .20 .2 | z _o = 0.2 0.399892 .376488 .320318 .25661 .200963 .127302 .124466 .099994 .081645 .056986 .041941 .036992 .032241 .025690 .025690 .025690 .025690 .025690 .025690 .025690 .025690 .025690 .025690 .02501 .021100 | 2 ₀ = 0.4 0.205046 .199987 .191551 .178557 .105290 .147214 .131500 .116879 .105707 .092081 .081950 .073185 .055628 .059119 .048671 .04485 .040857 .057704 .034999 | z _o = 0.6 0.159055 .138122 .135462 .151261 .125825 .115496 .112628 .105525 .098442 .098442 .098565 .095024 .078300 .073252 .068034 .065299 .099007 .0551355 .051046 | 2 ₀ = 0.8 0.108555 .108151 .107022 .105199 .102762 .099809 .096452 .092804 .088970 .085049 .081122 .077258 .0775511 .069919 .066511 .065309 .066511 .057941 .054989 .052655 | 3-5 3-5 3-5 3-5 3-5 3-5 3-5 3-5 3-5 3-5 | y ₁ ,0 0 0 11 -2 -2 -2 -2 -2 -2 -2 -2 -2 -2 | z ₀ = 0.2 0.398539 375210 318962 295500 199596 155927 123082 098598 080235 066290 0555542 040455 035080 030701 027090 024083 021554 | 2 ₀ = 0.4 0.200256 .197195 .188554 .175730 .166470 .144578 .128643 .113998 .100797 .089138 .078969 .070161 .062556 .055993 .050524 .045416 .041155 .037445 .031445 | z _o = 0.6 0.134622 .13708 .131039 .126823 .121564 .115010 .108108 .10965 .093833 .086901 .080298 .074102 .068354 .063065 .053825 .046196 .042310 | 2 _o = 0.8 0.102177 .101790 .100648 .096802 .096352 .096358 .089929 .086218 .082311 .078304 .074280 .070305 .066431 .066298 .079319 .0967748 |
| | 1.00 0 .05 .10 .20 .20 .30 .30 .40 .40 .50 .70 .80 .70 .80 .90 .90 .90 .90 .90 .90 .90 .9 | .017790 .017790 .359542 .376137 .319967 .296508 .200608 .200608 .156-44 .124109 .09623 .081274 .067340 .096603 .046206 .041342 .036184 .051822 .028231 .025246 .022741 .020622 .018818 .017271 | .02516 .032566 .202516 .199257 .190619 .107801 .161549 .116116 .102953 .091295 .081150 .072568 .064793 .05852 .047766 .047766 .047550 .059888 .036698 .055911 .051470 | .045715 .045215 .137854 .136745 .136745 .136075 .124027 .114029 .104291 .097189 .097289 .097289 .097287 .066642 .066642 .066642 .066642 .057550 .055664 .057550 .05666 .046865 .045865 .045865 | .052655 .052655 .106782 .106588 .105265 .105455 .105455 .058014 .059457 .050963 .087101 .083145 .075271 .071272 .064548 .061688 .057592 .0545461 .050002 .047740 | 3.5 4.0 4.0 4.0 4.0 4.0 4.0 4.0 4.0 4.0 4.0 | 0 .00 .10 .20 .20 .20 .20 .20 .20 .20 .20 .20 .2 | .017576 .0175997 .398386 .374981 .318808 .255147 .199443 .155773 .122927 .098445 .080080 .066134 .055385 .046974 .040296 .034921 .0205399 .025919 .025919 .015242 .017407 .015826 | .028840 .199946 .196885 .188244 .175420 .160159 .144066 .128330 .175651 .069841 .062233 .076651 .069981 .049997 .049086 .049997 .049086 .040822 .037107 | .039933 .037235 .134147 .135232 .130563 .1265847 .126887 .114532 .107628 .100483 .093350 .086415 .073610 .067859 .062867 .053318 .049312 .049312 .042388 .039406 | .044145 .041711 .101525 .101136 .099994 .0986147 .098672 .092672 .08268 .085555 .077655 .077657 .069627 .069627 .069627 .069627 .069627 .069627 .069627 .069627 .069627 .069627 .069621 .098839 .095050 .096641 .046641 .042637 .049975 |
| 2.6 2.6 2.6 2.6 2.6 2.6 2.6 2.6 2.6 2.6 | 0 .05 .10 .10 .50 .50 .35 .40 .20 .55 .60 .60 .70 .86 .86 .90 .90 | .599070 .575665 .919494 .295833 .205131 .196464 .125621 .096761 .086761 .096697 .047692 .041021 .035653 .031280 .027678 .024679 .02160 .02025 .04187 .0316537 | .201341 .196:91 .189641 .1768:20 .161563 .1454:75 .129746 .115107 .101913 .0902:63 .080104 .071306 .063713 .057164 .051510 .046618 .042375 .058682 .035458 .035653 .030149 | .136308 .135395 .132728 .128316 .128316 .128368 .116746 .109822 .1098569 .088651 .075884 .070156 .064689 .060076 .05597 .051725 .048129 .044877 .042108 | .104544 .104158 .105122 .1051179 .098747 .099735 .092556 .088640 .084750 .086763 .076762 .072812 .068967 .005265 .061735 .058369 .05289 .05289 .05289 .05289 .05289 .05289 .05289 .05289 .05289 .05289 .05289 .05289 .05289 | 5.00 5.50 5.50 5.50 5.50 5.50 5.50 5.50 | 0 .K .IX .Z .Z .X .X .X .X .X .X .X .X .X .X .X .X .X | .398206 .374801 .318629 .254967 .199263 .155592 .122746 .098261 .079298 .065952 .046790 .040111 .054735 .026740 .021730 .021739 | .199583 .196523 .187581 .175056 .159795 .145702 .127965 .115318 .100115 .088453 .078281 .069469 .061860 .055293 .049620 .04441 .056723 .053471 .056723 | .135594 .132680 .132680 .1326793 .120333 .120333 .120333 .120333 .120731 .092790 .089894 .073045 .067291 .061996 .057152 .052740 .048731 .045095 .041799 | .1007/70 .100383 .097240 .097393 .094920 .091923 .088510 .080859 .076870 .072839 .068856 .064252 .051050 .094862 .094862 .094862 .094862 .094862 .04528 .04528 .04528 .04528 .04528 .04528 .04528 |
| 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 | 0 .05 .10 .15 .20 .20 .30 .50 .40 .55 .65 .70 .70 .70 .70 .70 .80 .85 .90 | . 398774 . 575570 . 519198 . 255537 . 199834 . 196165 . 125521 . 098838 . 090477 . 060933 . 050787 . 047579 . 040704 . 035532 . 030955 . 027347 . 01857 . 01857 . 019676 . 017847 . 016272 | .200736 .1976-76 .189035 .176212 .160993 .144862 .129130 .114487 .101288 .089635 .070468 .070663 .056505 .05695 .05695 .0569468 .037979 .041684 .037979 .034741 .031901 | .135,564 .134450 .131782 .127568 .122111 .115759 .108860 .101721 .094594 .087666 .081068 .074879 .069158 .069857 .059029 .054653 .050643 .0497026 .0497026 | .105209 .10:85.3 .10:1682 .09:95.8 .09:95.8 .09:75.7 .08:75.9 .07:95.9 .07:95.9 .07:95.9 .07:95.9 .07:95.9 .07:95.9 .07:95.9 .07:95.9 .07:95.9 .07:95.9 .07:95.9 .07:95.9 .07:95.9 .07:95.9 .07:95.9 .06:96.9 .06: | | | | | | |

TABLE V.- ILLUSTRATION OF USE OF TABLES TO CALCULATE ANGLE-OF-ATTACK

DOWNWASH IN PLANE OF SYMMETRY BEHIND WING OF FIGURE 8

$$[M = 1.64; x_0 = 2.2; y_0 = 0; z_0 = 0; \beta_m = 2.0]$$

| 9 | $-\frac{v}{V_{\infty}\alpha} (eq. (25)$ nondimensionalized by $V_{\infty}\alpha$) | -0.238 + 0.126 = -0.112 |
|----------|---|--|
| (3) | $F_{\mathbf{w},0}$ from table III | o.144686 |
| (| $egin{array}{c} F_{\mathbf{w}}ig(ar{\mathbf{y_{i,o}}}ig) \ from \ 	ext{table II} \end{array}$ | -1.553695 75150 489023 354408 217364 176978 145812 145812 080882 063801 046973 |
| © | $\frac{\Gamma y_{i+1} - \Gamma y_{i-1}}{V_{\infty} ab/2}$ | 0 .043 .034 .023 .018 .018 .010 .002 .018 .018 .018 .018 .019 .019 .0179 .179 |
| @ | $\frac{\Gamma_{\mathbf{y_i}}}{V_{\mathbf{x}}ab/2}$ | 888. 114. 14. 14. 16. 16. 16. 16. 16. 16. 16. 16. 16. 16 |
| Θ | yi,o | 0 2011888834488666558888889901 |

TABLE VI.- ILLUSTRATION OF USE OF TABLES TO CALCULATE ROLLING SIDEWASH

IN PLANE OF SYMMETRY BEHIND WING OF FIGURE 8

$$[M = 1.64; x_0 = 2.0; y_0 = 0; z_0 = 0.2; \beta_m = 2.0]$$

| (1) | 2 | 3 | (4) | <u>(5)</u> |
|---|---|--|--|--|
| уі,0 | $\frac{\Gamma_{y_i}}{p(b/2)^2}$ | $\frac{\Gamma_{y_{i+1}} - \Gamma_{y_{i-1}}}{p(b/2)^2}$ | Fv Yi,o) from table IV | $\frac{v/V_{\infty}}{pb/2V_{\infty}} \text{ (eq. (27)}$ nondimensionalized by $pb/2$) |
| 0 .05 .10 .15 .20 .25 .30 .35 .40 .45 .50 .55 .60 .65 .70 .75 .80 .85 .90 | 0 .035 .064 .098 .133 .172 .208 .245 .283 .320 .360 .395 .432 .504 .543 .556 .527 .464 .358 | 0.035 .064 .063 .069 .074 .075 .073 .076 .075 .077 .072 .072 .072 .072 .076 .052 016 092 169 464 358 | 0.401906 .378518 .322402 .258849 .203320 .159916 .127465 .103564 .086080 .073514 .065098 .061233 .066861 | 0.294 |

TABLE VII.- ILLUSTRATION OF USE OF CHARTS TO CALCULATE ANGLE-OF-ATTACK DOWNWASH OFF PLANE OF SYMMETRY BEHIND WING OF FIGURE 8

 $[M = 1.64; x_0 = 2.2; y_0 = 0.15; z_0 = 0; \beta m = 2.0]$

| (3) | $\frac{\mathrm{d}\epsilon}{\mathrm{d}\alpha} = - \sum_{1=n_1}^{0} \stackrel{\leftarrow}{\oplus} \stackrel{\rightarrow}{\otimes} +$ $\sum_{1=0}^{n_2} \stackrel{\rightarrow}{\otimes} \stackrel{\rightarrow}{\otimes} \stackrel{\rightarrow}{\otimes}$ $\sum_{1=0}^{n_2} \stackrel{\rightarrow}{\otimes} \stackrel{\rightarrow}{\otimes} \stackrel{\rightarrow}{\otimes}$ (a) | o.w3 |
|----------|--|---|
| (3) | n 2 2 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | 9,00 |
| (6) | Fw(Y ₁ ,o) from figure 6 | 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 |
| (1) | Y _{1,0} = 0.15 - ① | 6.1.1.1.1.1.1.1.1.0 88666888833388338 833 |
| (-) | y1,0 | 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.0 |
| 9 | $\downarrow \qquad \downarrow \qquad$ | 0.045 |
| 9 | $\frac{\Gamma_{\mathbf{y_{i+1}}} - \Gamma_{\mathbf{y_{i-1}}}}{V_{\mathbf{odb}}/2}$ | |
| (| Fw(Y1,o) from fligure 6 | 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 |
| \odot | $\overline{x_1} = 1.1 + \frac{\overline{0}}{2}$ | 6.6 6.6 6.6 6.7 6.7 6.7 6.8 6.8 6.8 6.8 6.7 6.0 6.0 6.0 6.0 6.0 6.0 6.0 6.0 6.0 6.0 |
| @ | Y _{1,0} = 0.15 - ① | 11111 11101 1101 10 |
| Θ | y1,0 | 0.88886566888338888398 |

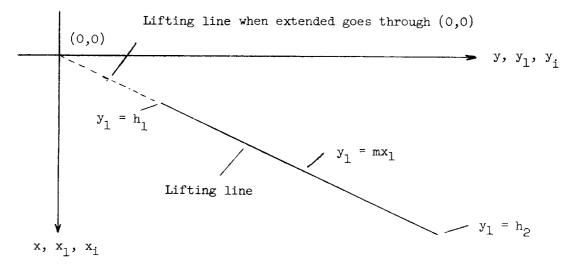
 $^{\rm B}{\rm Equation}$ (15) nondimensionalized by ${\rm V}_{\omega}\alpha.$

TABLE VIII.- ILLUSTRATION OF USE OF CHARTS TO CALCULATE ROLLING SIDEWASH OFF PLANE OF SYMMETRY BEHIND WING OF FIGURE 8

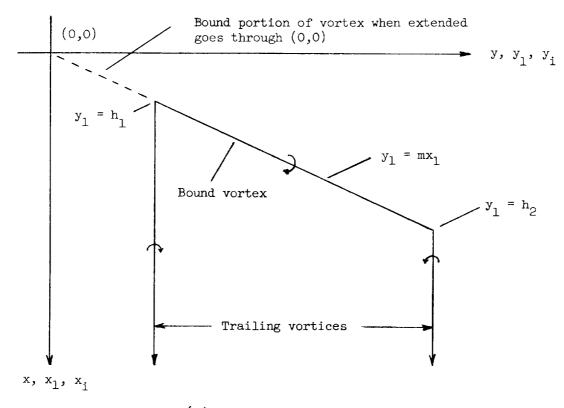
 $[M = 1.64; x_0 = 2.0; y_0 = 0.15; z_0 = 0.20; \beta m = 2.0]$

| (1) | $\frac{\sqrt{\frac{\sqrt{pb}}{2V_{\infty}}}}{1-n_{1}} = \frac{\sqrt{\frac{pb}{2V_{\infty}}}}{1-n_{1}} = \frac{\sqrt{\frac{pb}{2V_{\infty}}}}{\sqrt{\frac{pb}{2V_{\infty}}}} = \frac{\sqrt{\frac{pb}{2V_{\infty}}}}}{\sqrt{\frac{pb}{2V_{\infty}}}} = \frac{\sqrt{\frac{pb}{2V_{\infty}}}}{\sqrt{\frac{pb}{2V_{\infty}}}} = \frac{\sqrt{\frac{pb}{2V_{\infty}}}$ | 0.309 | |
|------------|---|--------------------------------------|---|
| (D) | h2 ∑ | 0.224 | |
| 0 | Fv(Y1,0) from figure 7 | 000 | 000 1000 111 128 128 128 128 128 128 128 128 128 |
| @ | Y _{1,0} = 0.15 - ① | 6 8. 8 | |
| (L) | У1,0 | 0.1 .95 | \$\\ \\$\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\ |
| 9 | ° | -0.085 | |
| (5) | $\frac{\Gamma_{y_{1+1}} - \Gamma_{y_{1-1}}}{p(b/2)^2}$ | 494. | |
| | Fv(Y _{1,0}) from figure 7 | 000 | 000000 86.66.66.66.66.66.66.66.66.66.66.66.66.6 |
| 9 | ايخا | 0 2 2 2 3 3 3 3 | £883666 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 |
| 8 | Y1,0 = 0.15 - ① | 1.15 1.10 1.05 | 828286866666628432883 |
| (1) | ۷,1,0 | 0.69. | \$\$£6668553388336 |

^aEquation (16) nondimensionalized by pb/2.

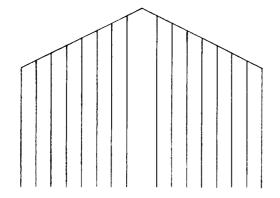


(a) Lifting line.

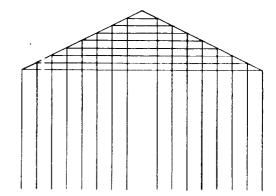


(b) Yawed horseshoe vortex.

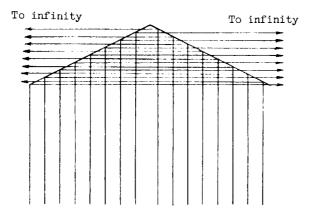
Figure 1.- Sketch of lifting line and yawed horseshoe vortex showing symbol notation and axis system used in text.



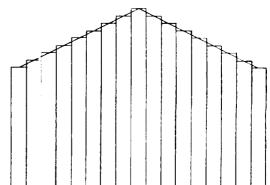
(a) Swept lifting line approximated by a series of semiinfinite yawed horseshoe vortices.



(b) Swept lifting line approximated by a series of seminifinite unswept horseshoe vortices. Symmetrical loading and symmetrically distributed points.

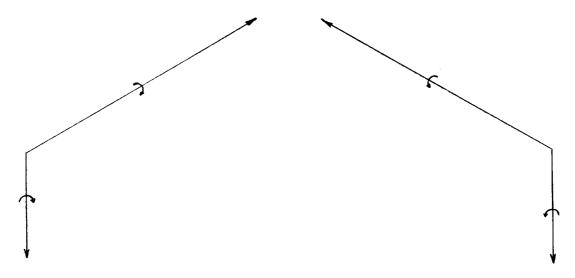


(c) Swept lifting line approximated by a series of semiinfinite unswept horseshoe vortices. Unsymmetrical loading and/or unsymmetrically distributed points.

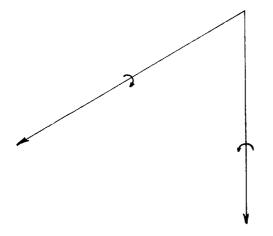


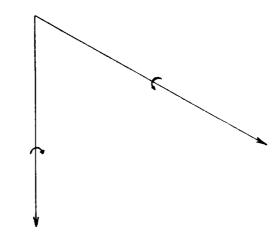
(d) Swept lifting line approximated by a series of finite rectangular horseshoe vortices.

Figure 2.- Swept lifting line approximatel by distributions of various types of vortices.



- (a) Type of semi-infinite yawed horseshoe vortex described by first terms of equations (1) and (2) with Γy_{i+1} - Γy_{i-1} negative.
- (b) Type of semi-infinite yawed horseshoe vortex described by second terms of equations (1) and (2) with Γ_y - Γ_y_{i-1} negative.





- (c) Type of semi-infinite yawed horseshoe vortex described by first terms of equations (1) and (2) with $\Gamma_{y_{i+1}} \Gamma_{y_{i-1}}$ positive.
- (d) Type of semi-infinite yawed horseshoe vortex described by second terms of equations (1) and (2) with Γ_y - Γ_y - Γ_j-1 positive.

Figure 3.- Types of semi-infinite yawed horseshoe vortices represented in equations (1) and (2).

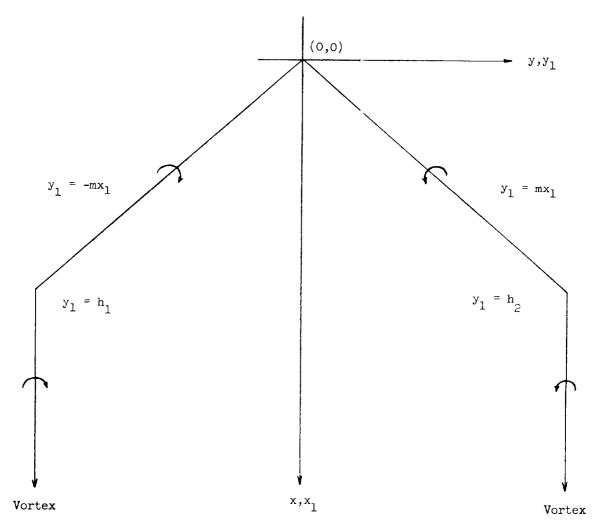


Figure 4.- Swept horseshoe vortex.

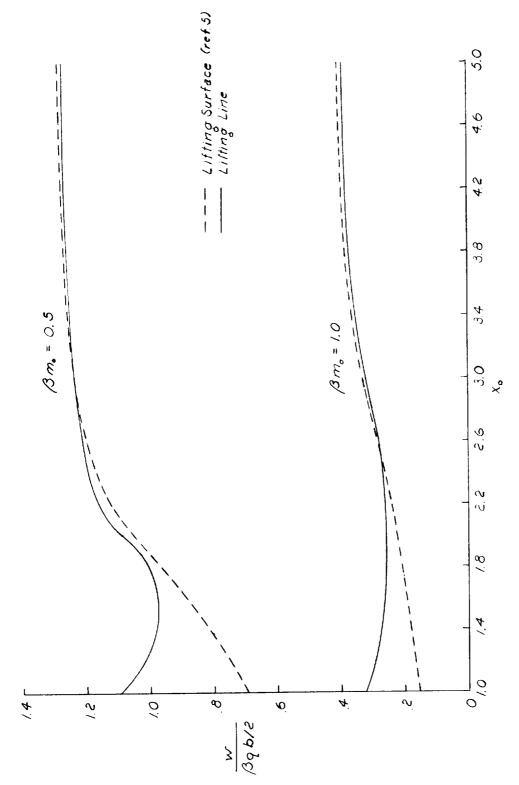


Figure 5.- Variation along longitudinal axis of downwash due to pitching behind triangular wings with β_{m_0} values of 1.0 and 0.5. Pitch axis is located at the apexes of the triangular wings and the lifting lines are the midchord lines. x_0 is measured from the point of intersection of lifting line with root chord.

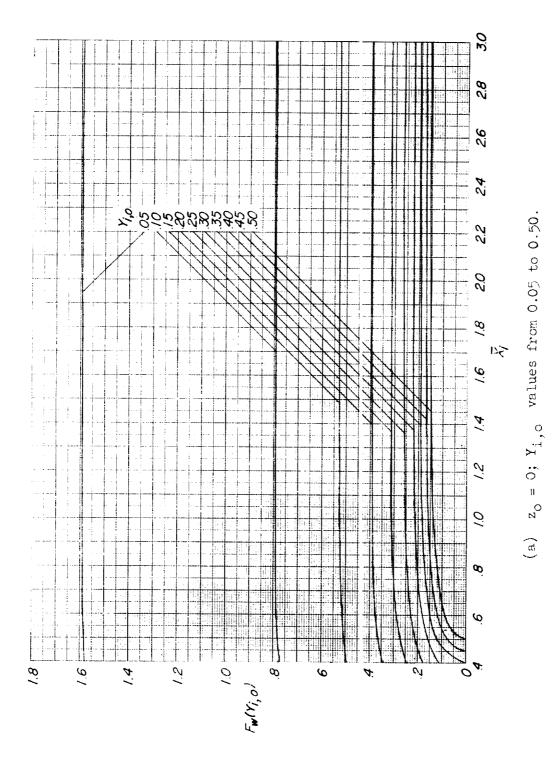


Figure 6.- Variation of $F_w(Y_{i,o})$ function with \overline{X}_i for $Y_{i,o}$ values from 0.05 to 1.45 and z_o values from 0 to 0.8.

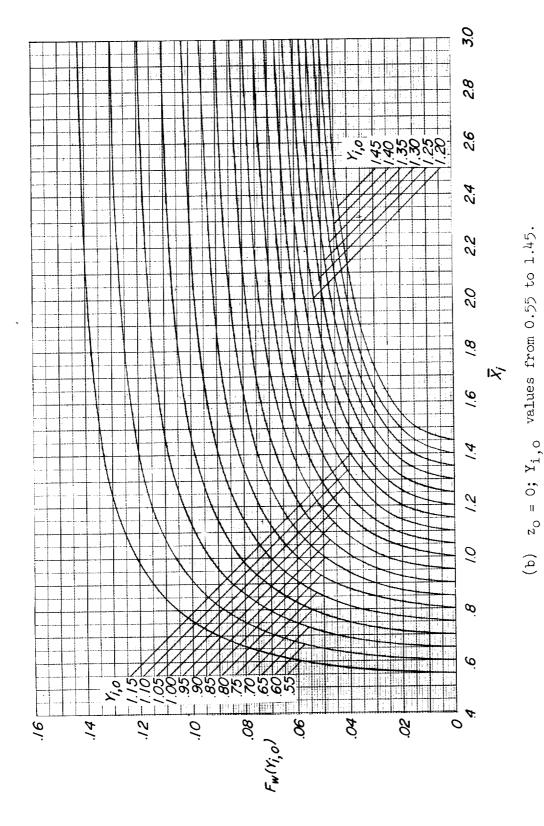


Figure 6.- Continued.

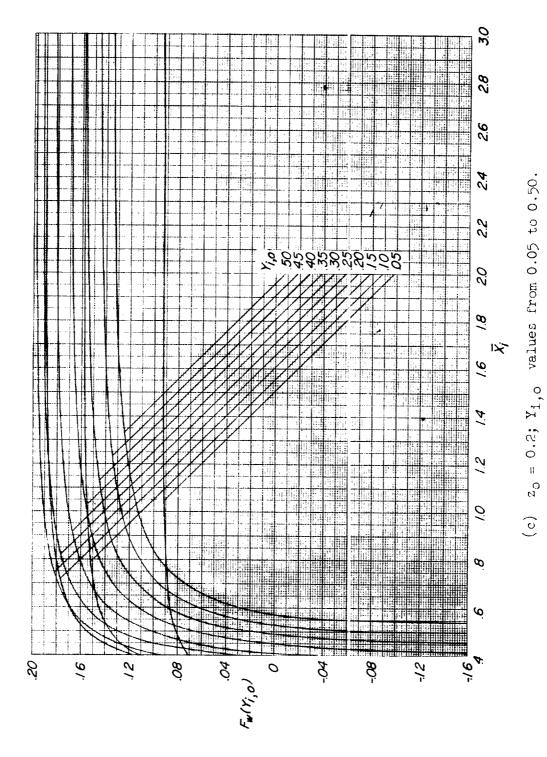
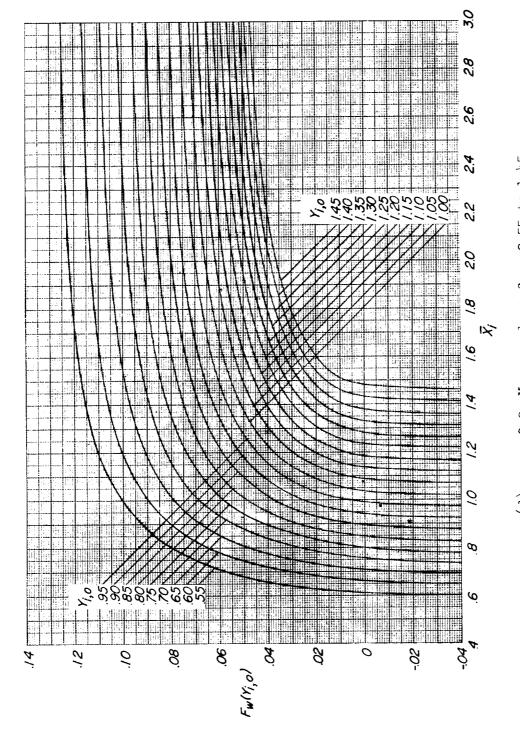
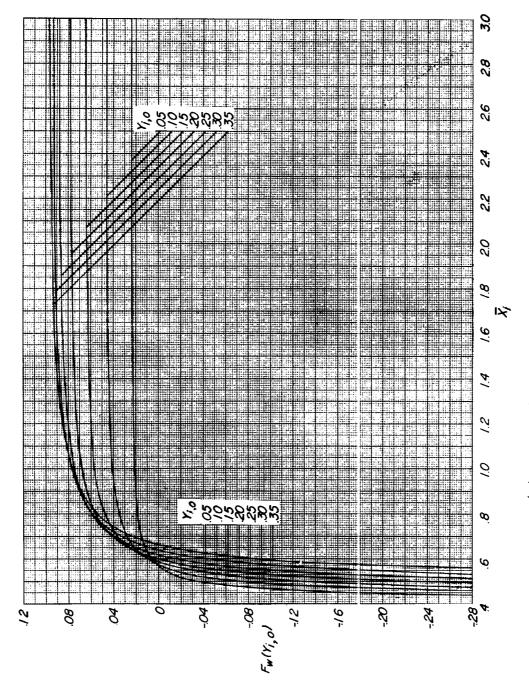


Figure 6.- Continued.



(d) $z_0 = 0.2$; $Y_{i,0}$ values from 0.55 to 1.45.

Figure 6.- Continued.



(e) $z_0 = 0.4$; $Y_{i,0}$ values from 0.05 to 0.35.

Figure 6.- Continued.

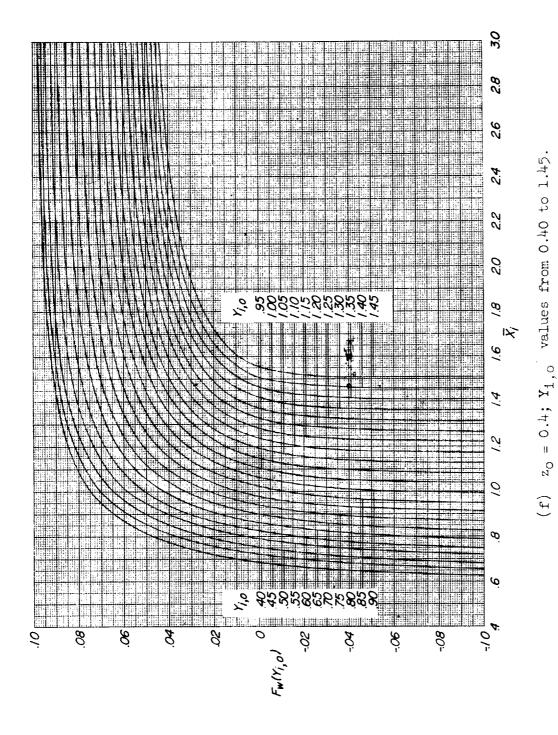
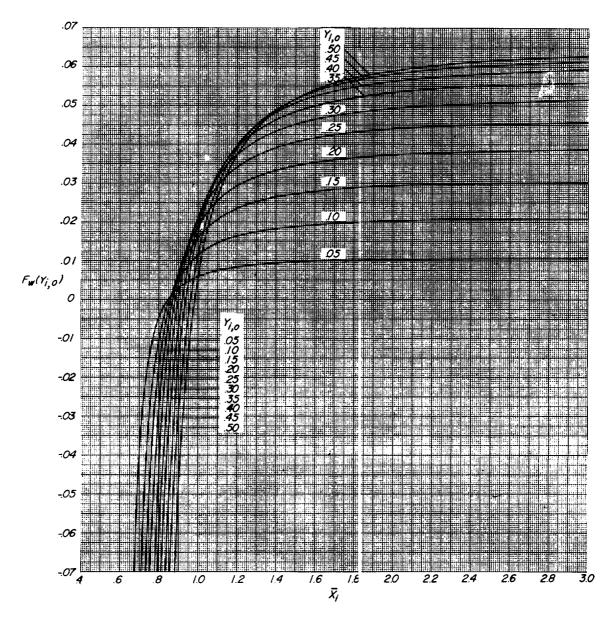
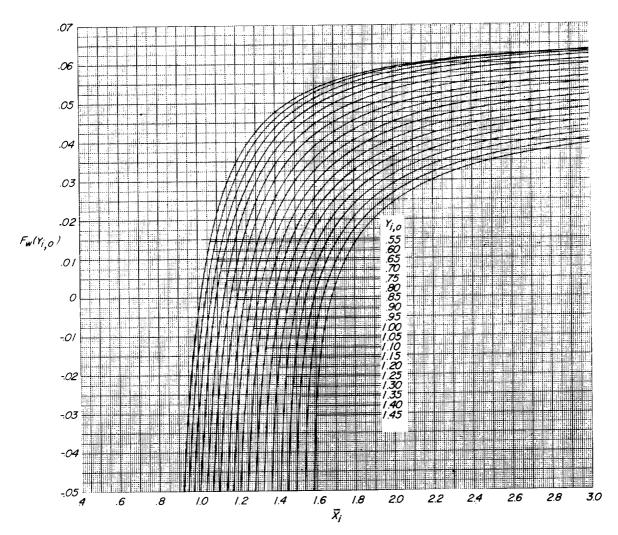


Figure 6.- Continued.

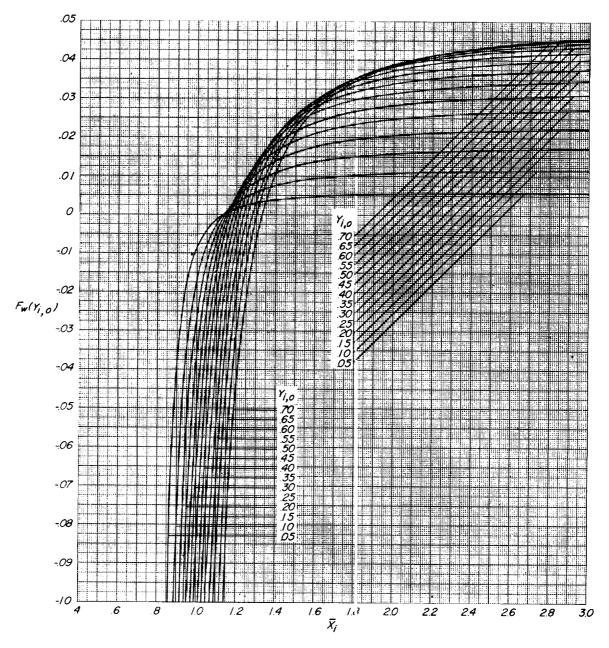


(g) $z_0 = 0.6$; $Y_{i,0}$ values from 0.05 to 0.50. Figure 6.- Continued.



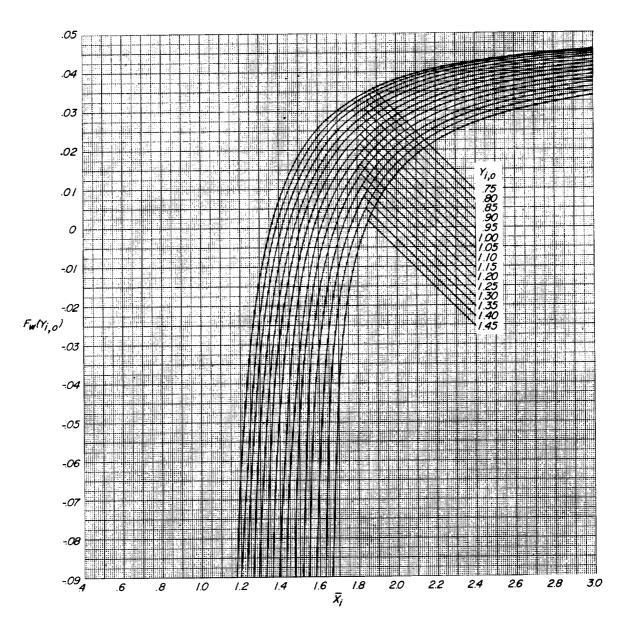
(h) $z_0 = 0.6$; $Y_{i,0}$ values from 0.55 to 1.45.

Figure 6.- Continued.



(i) $z_0 = 0.8$; $Y_{i,0}$ values from 0.05 to 0.70.

Figure 6.- Continued.



(j) $z_0 = 0.8$; $Y_{i,0}$ values from 0.75 to 1.45.

Figure 6.- Concluded.

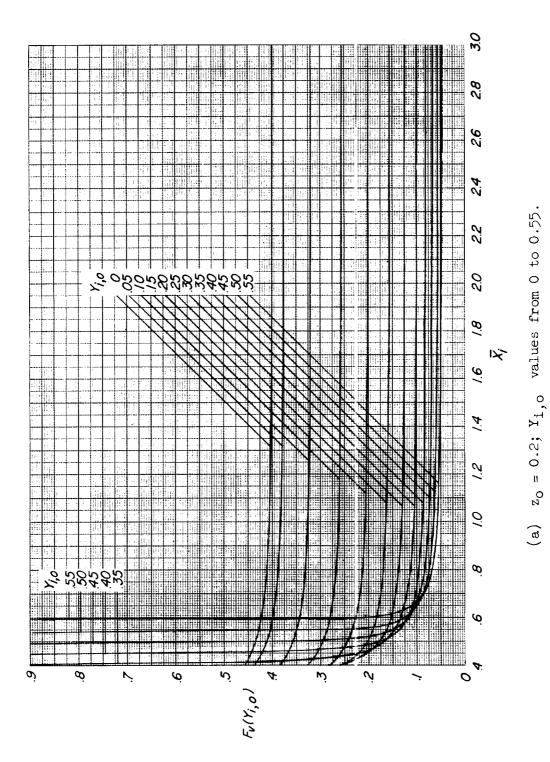


Figure 7.- Variation of $F_v(Y_{i,o})$ function with \overline{X}_i for $Y_{i,o}$ values from 0 to 1.45 and values from 0.2 to 0.8.

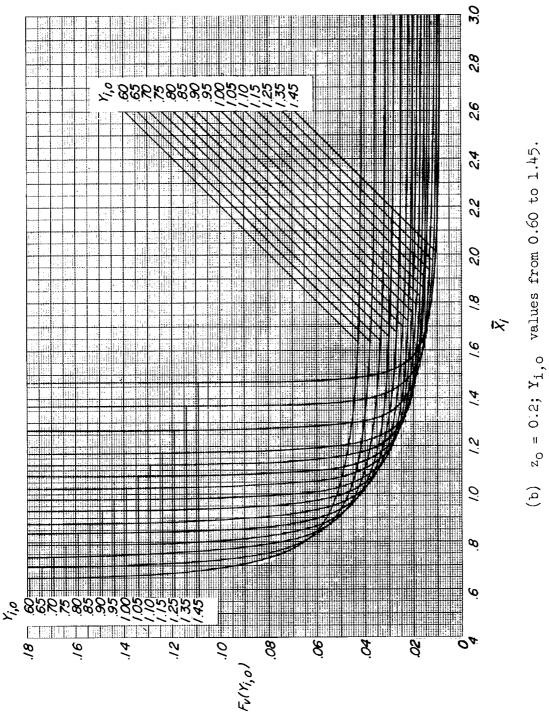
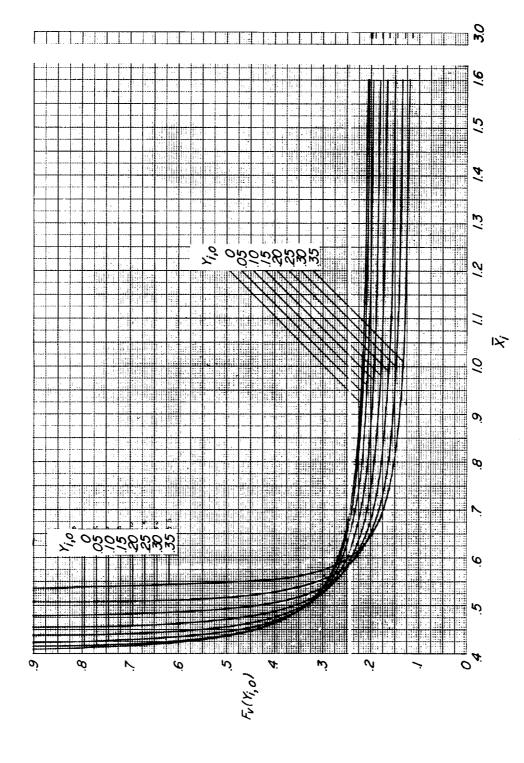


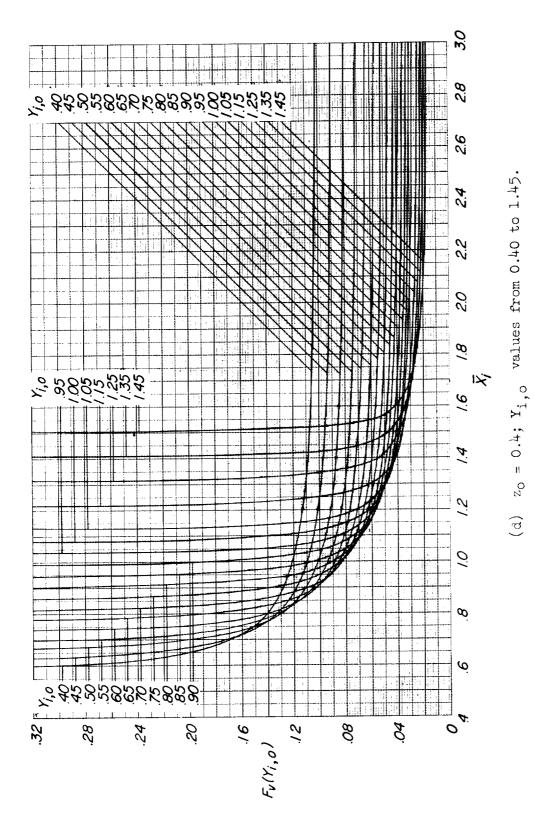
Figure 7.- Continued.

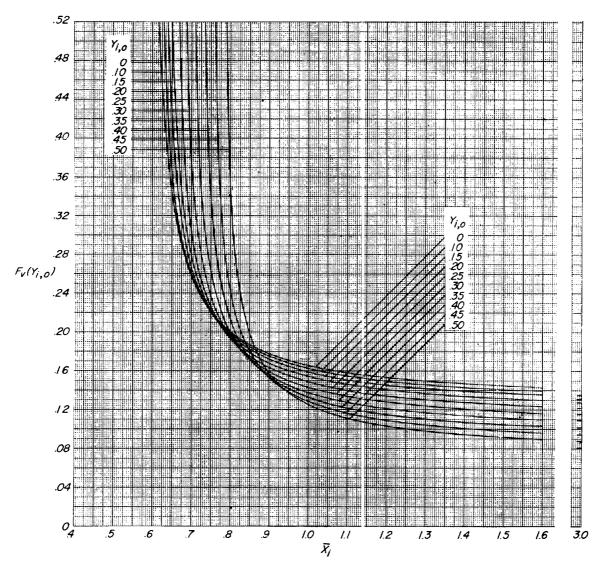


 $z_0 = 0.4$; Y_1, o values from 0 to 0.35.

Figure 7.- Continued.

Figure 7.- Continued.





(e) $z_0 = 0.6$; $Y_{i,0}$ values from 0 to 0.50.

Figure 7.- Continued.

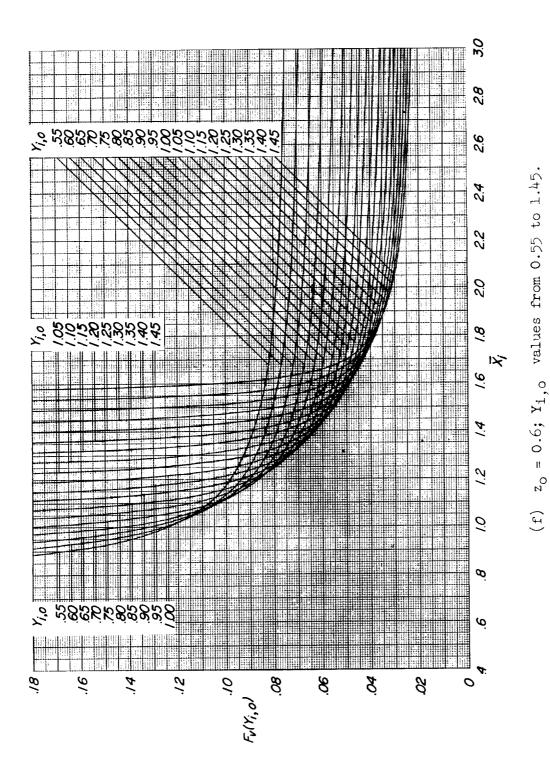
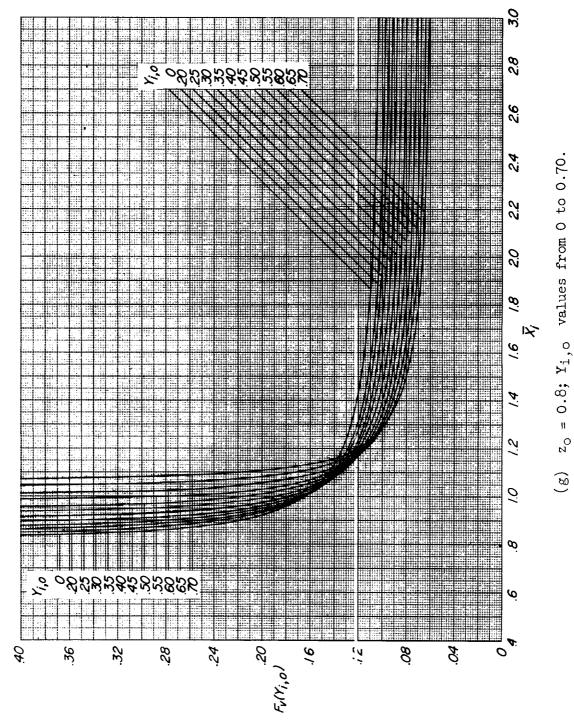
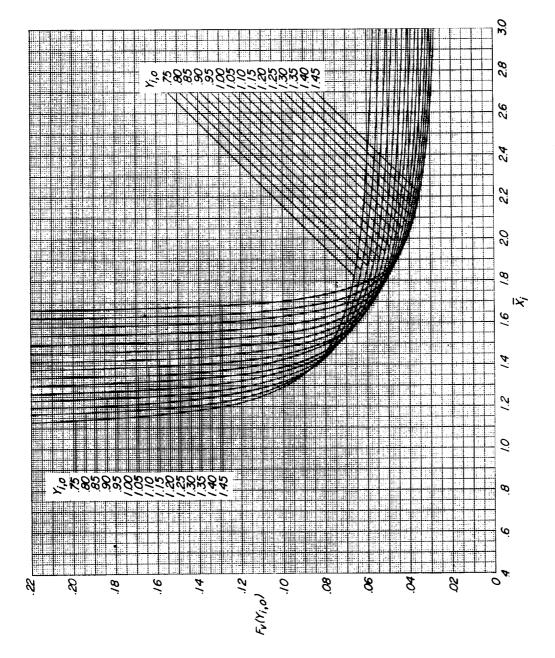


Figure 7.- Continued.

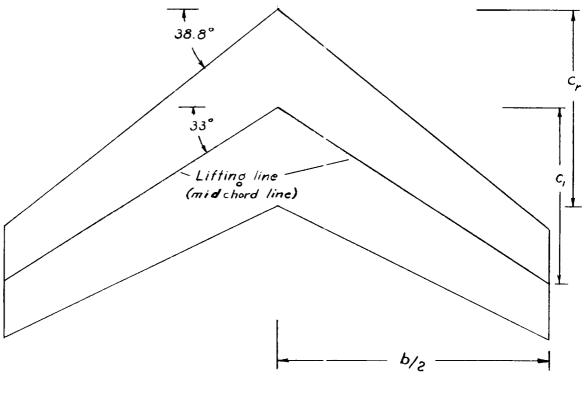


.



(h) $z_0 = 0.8$; $Y_{i,0}$ values from 0.75 to 1.45.

Figure 7.- Concluded.



$$A = 3.57$$

 $\lambda = 0.565$
 $m_o = 1.244$
 $m = 1.54$

| M | ß | BA | /3m _o | βm |
|------|------|--------------|------------------|-----|
| 1.35 | 0.9/ | 3.2 4 | 1.13 | 1.4 |
| 1.64 | /.30 | 4.6 4 | 1.62 | 2.0 |
| 2.19 | /.95 | 6.96 | 2.43 | 3.0 |

Figure 8.- Wing plan form, Mach numbers and geometric quantities used to illustrate computing procedure. $h=3.57; h=0.565; m_0=1.244; m=1.54$.

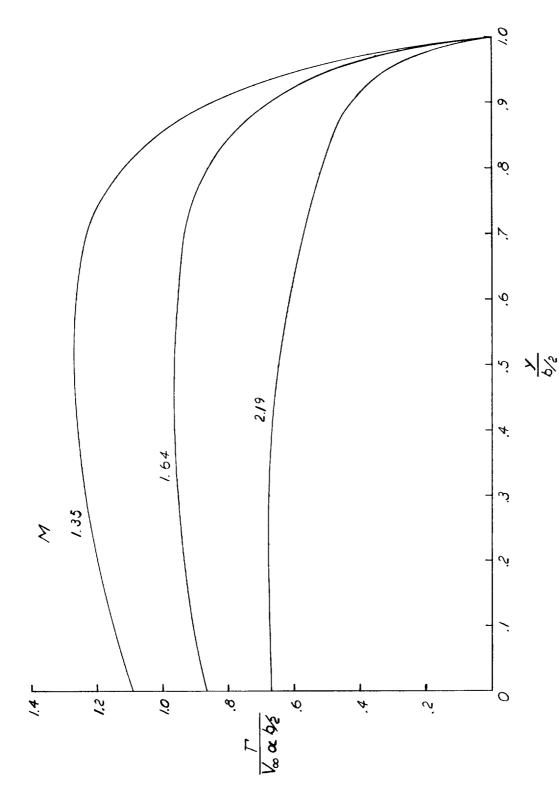


Figure 9.- Nondimensional spanwise distributions of circulation due to angle of attack for wing and Mach numbers given in figure 8.

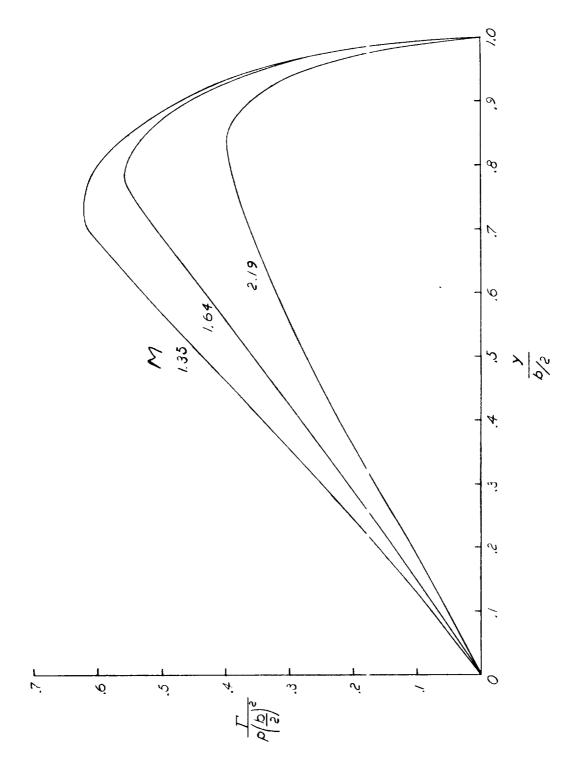


Figure 10.- Nondimensional spanwise distributions of circulation due to steady rolling for wing and Mach numbers given in figure θ .

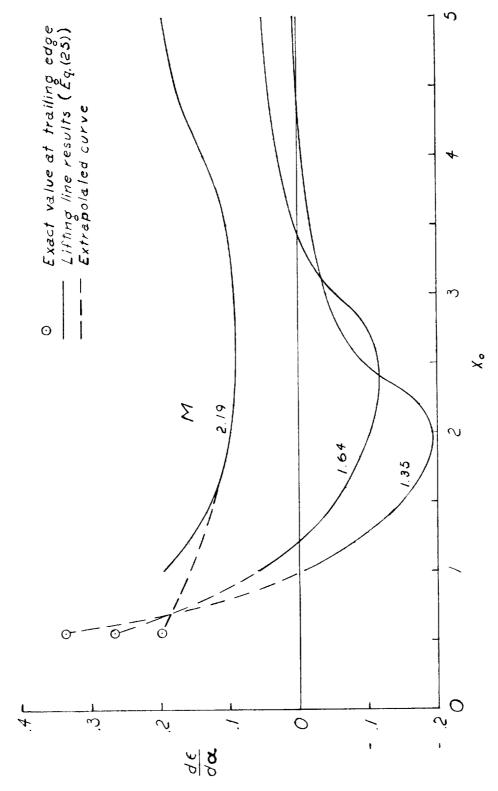


Figure 11.- Variation at three Mach numbers of the change in downwash angle with angle of attack $d\varepsilon/d\alpha$ along the longitudinal axis for wing in figure 8.

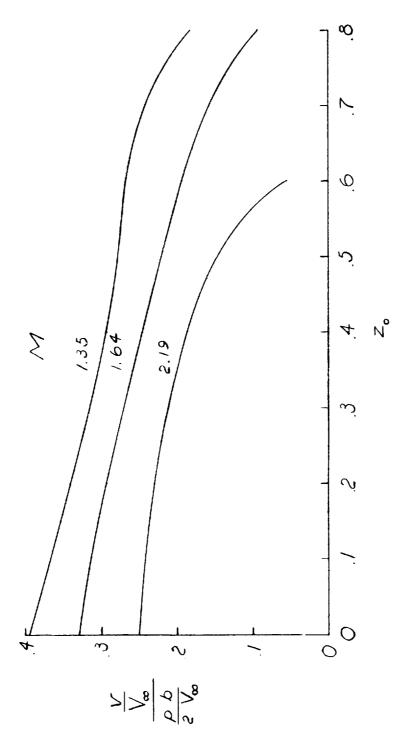
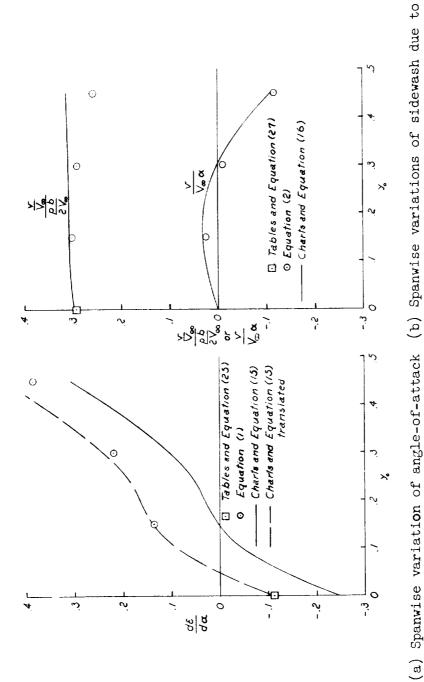


Figure 12.- Variation at three Mach numbers of the nondimensional sidewash parameter $\frac{v}{V_\infty}/\frac{pb}{2V_\infty}$ with vertical height for wing in figure 8. Nondimensional longitudinal distance behind lifting-line apex for which variations are shown is $x_{\rm o}=2.0$.



rolling and angle of attack at $x_0 = 2.0$ $z_0 = 0.2$. and $z_0 = 0$. and $x_0 = 2.2$ downwash at

Figure 13.- Spanwise variations of downwash and sidewash due to angle of attack and sidewash due to rolling for wing of figure 8. M=1.64.